



Computer Animation

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(601.457/657)



Overview

- Some early animation history
 - <http://web.inter.nl.net/users/anima/index.htm>
 - <http://www.public.iastate.edu/~rllew/chrnearl.html>
- Computer animation



Thaumatrope

Q: Why does animation work?

A: Persistence of vision

- 1824 John Ayerton invents the *thaumatrope*
- Or, 1828 Paul Roget invents the *thaumatrope*

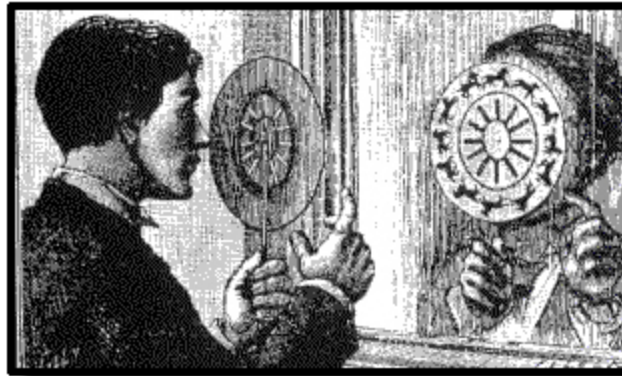


Thaumatrope



Phenakistoscope

- Invented independently by 2 people in 1832
- Disc mounted on spindle
- Viewed through slots with images facing mirror
- Turning disc animates images





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Zoetrope (1834)

- Images arranged on paper band inside a drum
- Slits cut in the upper half of the drum
- Opposite side viewed as drum rapidly spun
- Praxinoscope is a variation on this





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Mutoscope (1895)

- Coin-operated “flip-book” animation
- Picture cards attached to a drum
- Popular at sea-side resorts, etc.





Animation History

First known example of animation:

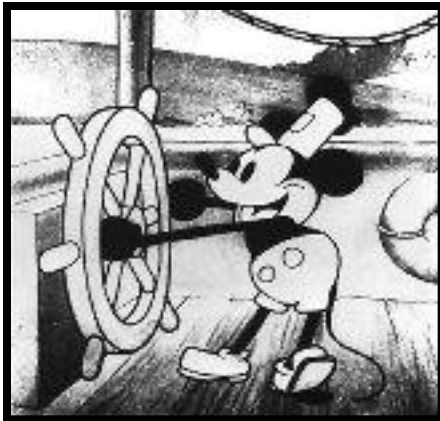
- “Humorous Phases of Funny Faces” (1906)

Humorous phases of funny faces



Key Developments

- Plot
- Creation of animation studios
- Inking on cels



“Steamboat Willie”
Walt Disney (1928)



“Felix the Cat”
Otto Messmer (1921)

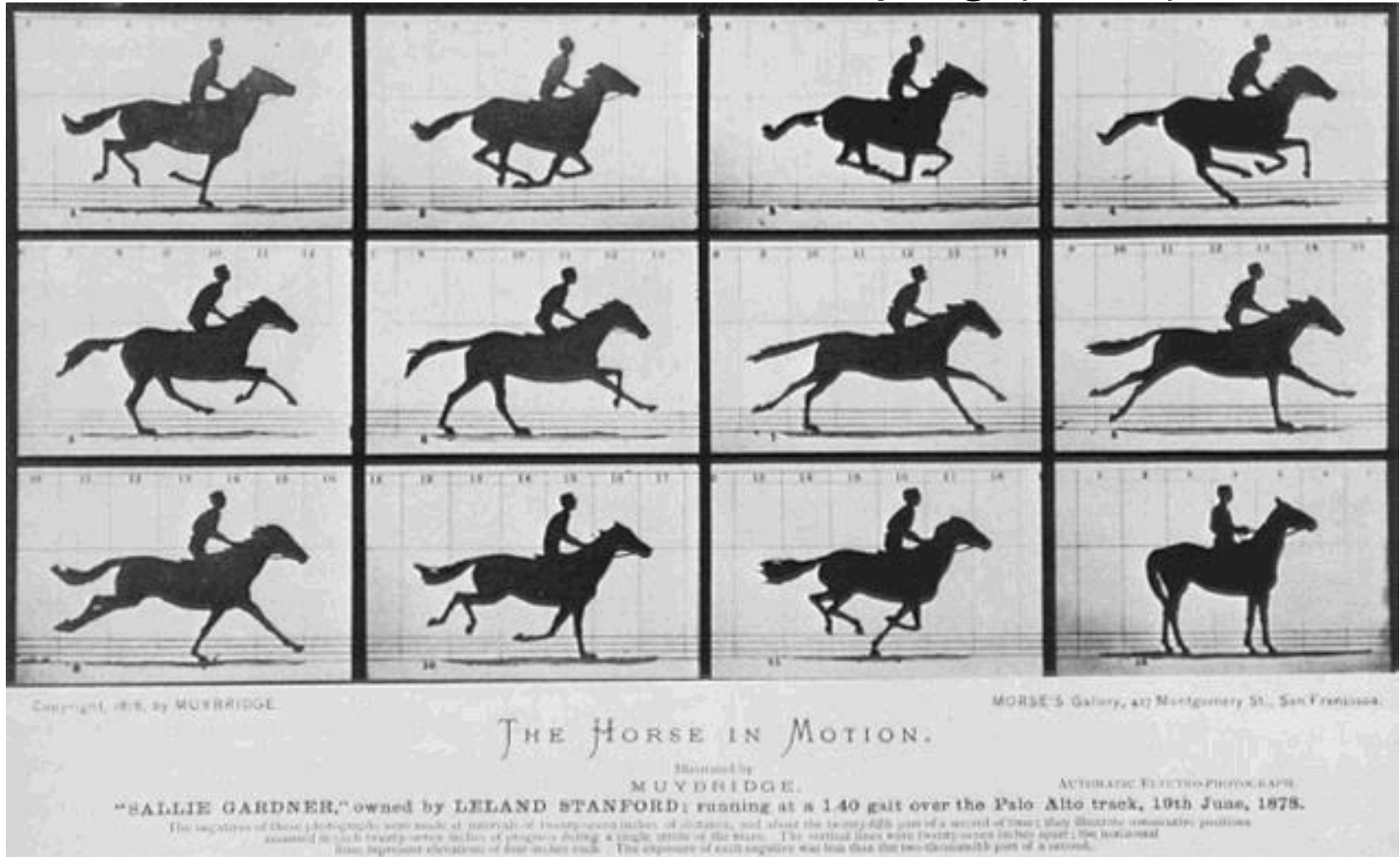


“Gertie the Dinosaur”
Windsor McCay (1914)



Key Developments

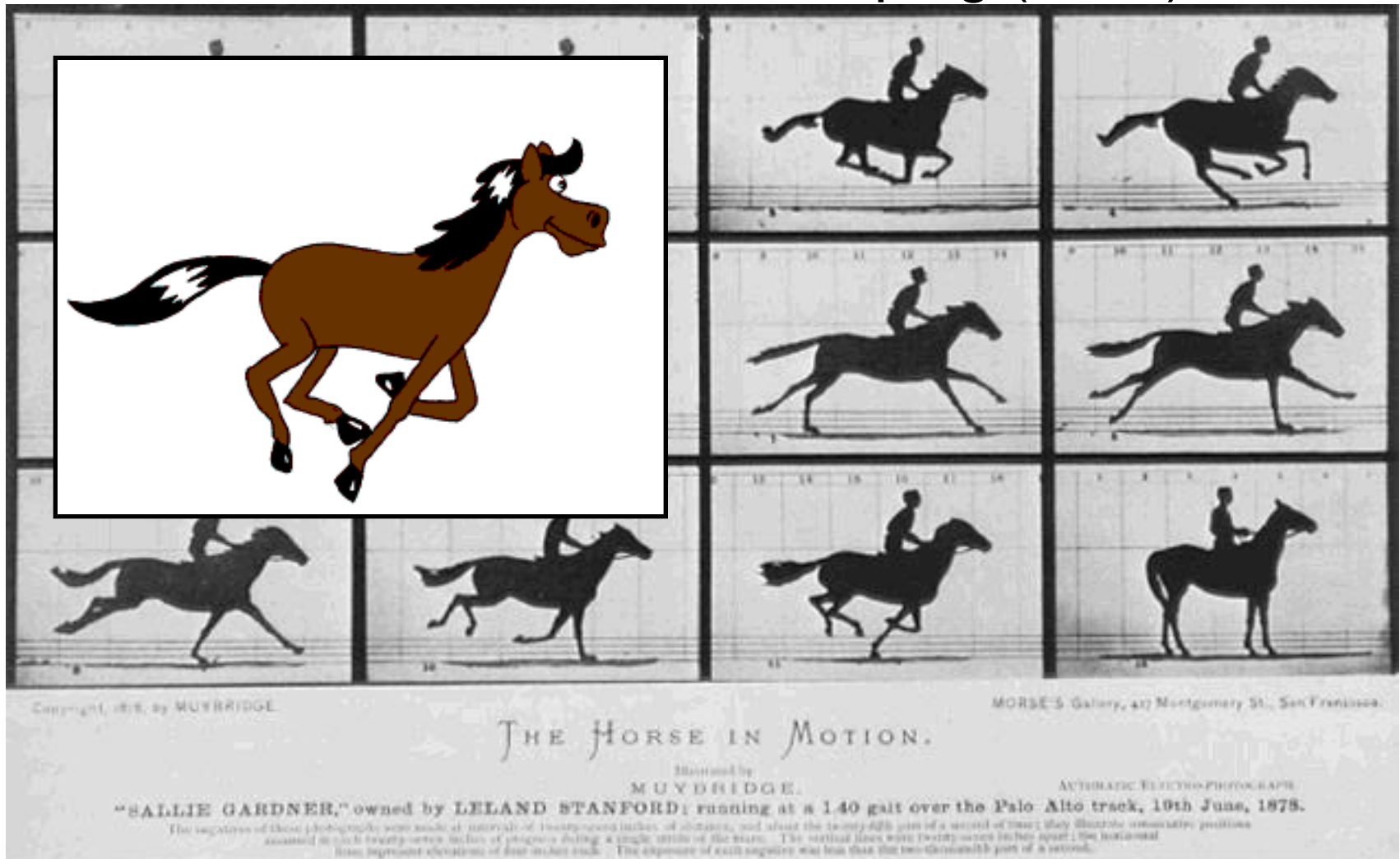
- Max Fleischer invents rotoscoping (1921)





Key Developments

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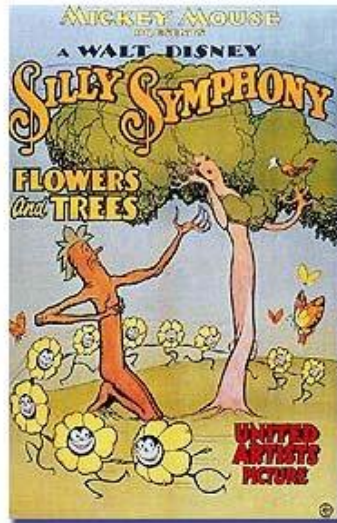




Key Developments

- “Flowers and Trees”, 1932:
 - Uses color, wins Academy Award
- “Snow White” (aka “Disney’s Folly”), 1937:
 - \$1.4 million to make
 - 750 artists
 - Highest grossing (\$8 million)

“Flowers and Trees”
Walt Disney



“Snow White”
Walt Disney

Animation Uses

- Entertainment
- Education
- Propaganda



Principles of Traditional Animation



How do we communicate aspects of the animation that are not strictly visual?

- Rigidity
- Weight
- Mood
- Intent
- Focus
- Etc.

See, for example, *The Illusion of Life: Disney Animation* for Disney's 12 basic principals of animation.

Luxo Junior



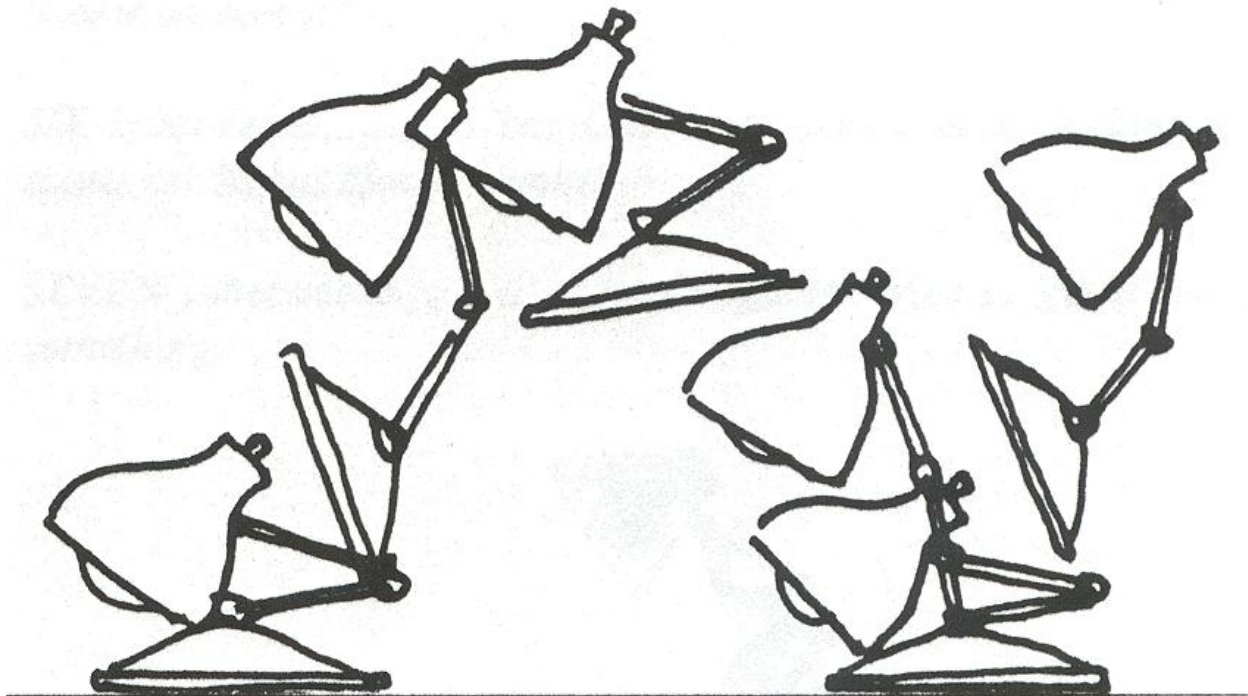
Overview

- Some early animation history
- Computer animation
 - Keyframe animation
 - Articulated figures
 - Kinematics and dynamics



Keyframe Animation

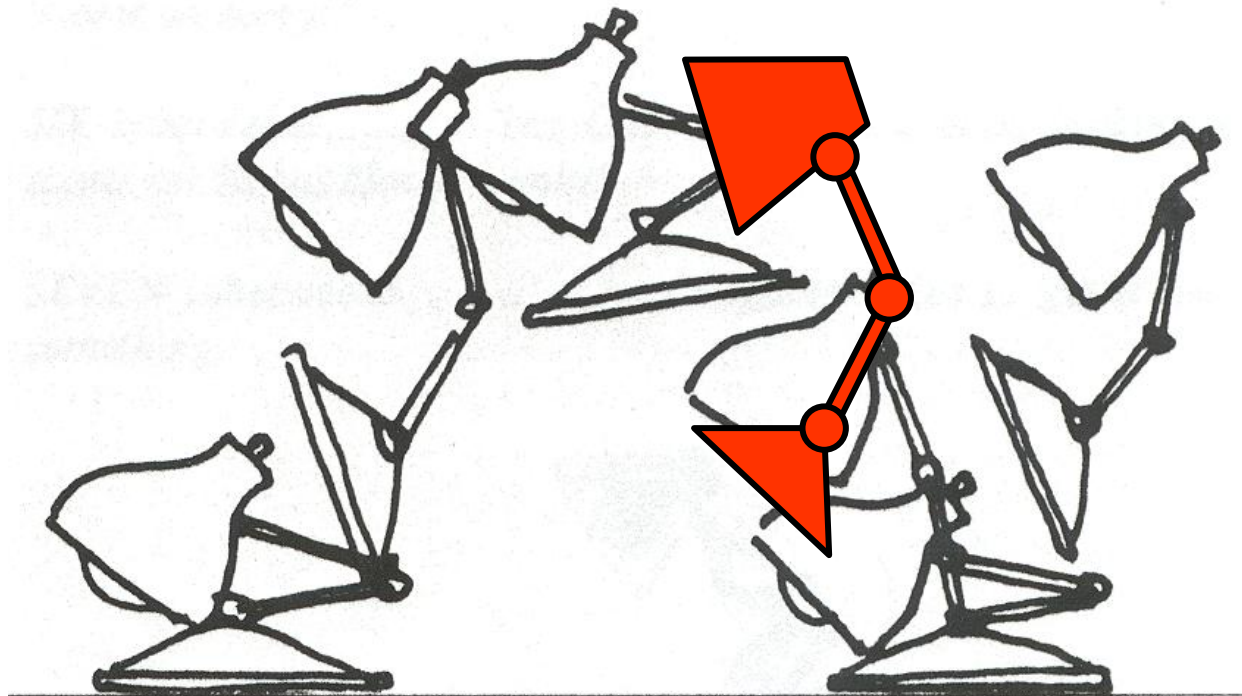
- Define character poses at specific time steps called “keyframes”





Keyframe Animation

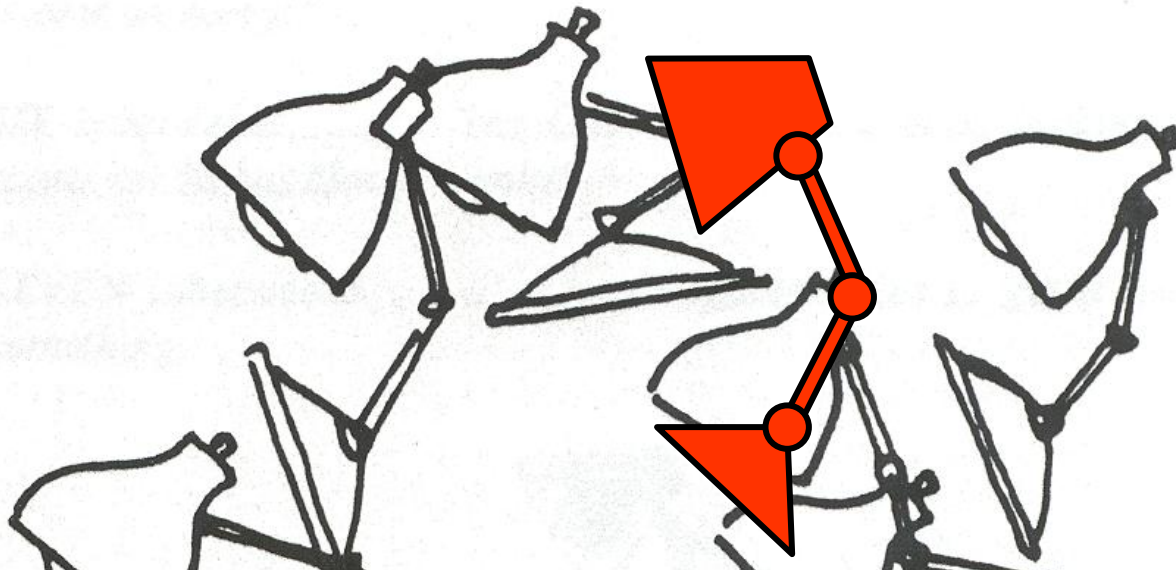
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- Interpolate/blend variables describing keyframes to determine poses for character “in-between”





Keyframe Animation

- Define character poses at specific time steps called “keyframes”
- Interpolate/blend variables describing keyframes to determine poses for character “in-between”



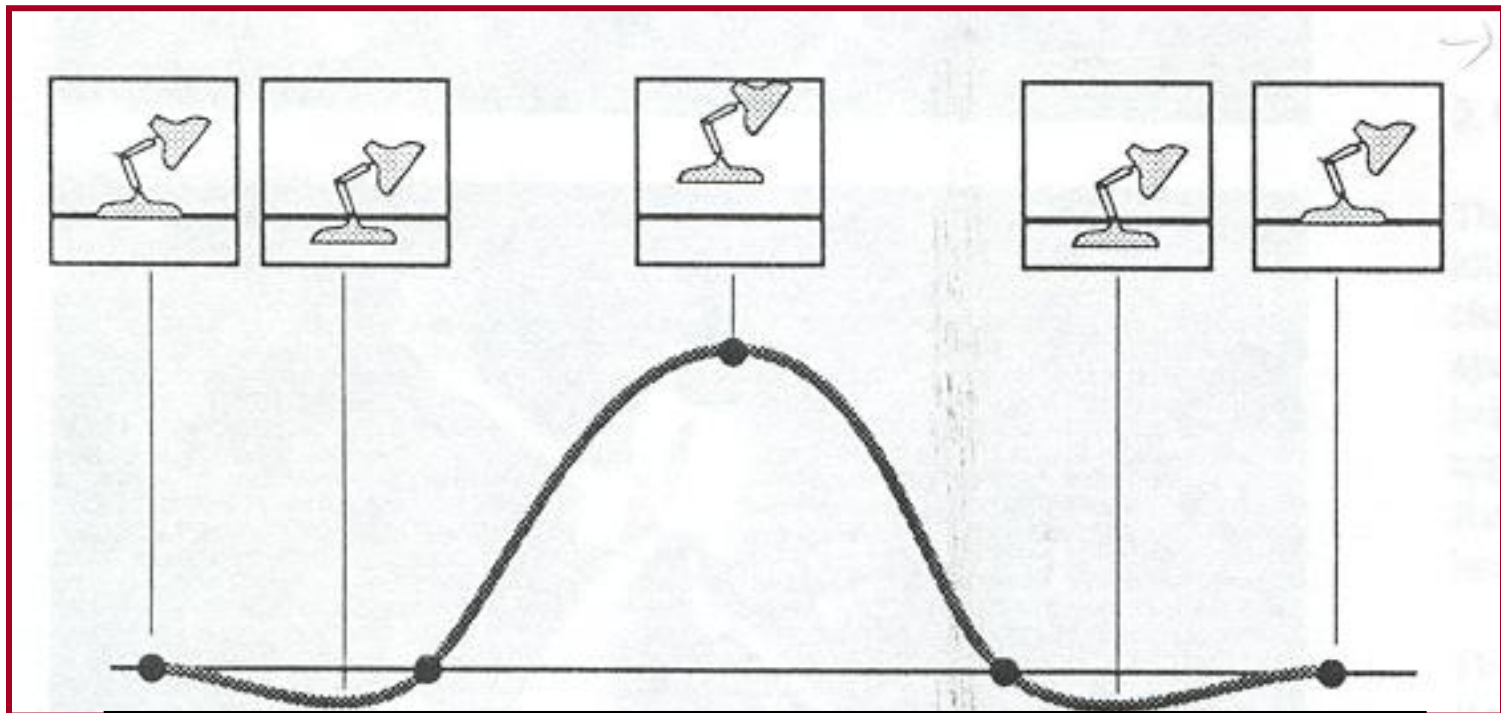
Can use your favorite spline to blend (assuming it satisfies required conditions, smoothness/convex-hull-containment/etc.)



Keyframe Animation

Note:

If you don't choose the “right” spline for blending, you may get problematic results.



Recall: Convex hull containment

assetter '87



Keyframe Animation

Q: Why interpolate/blend joint parameters instead of interpolating/blending vertices directly?

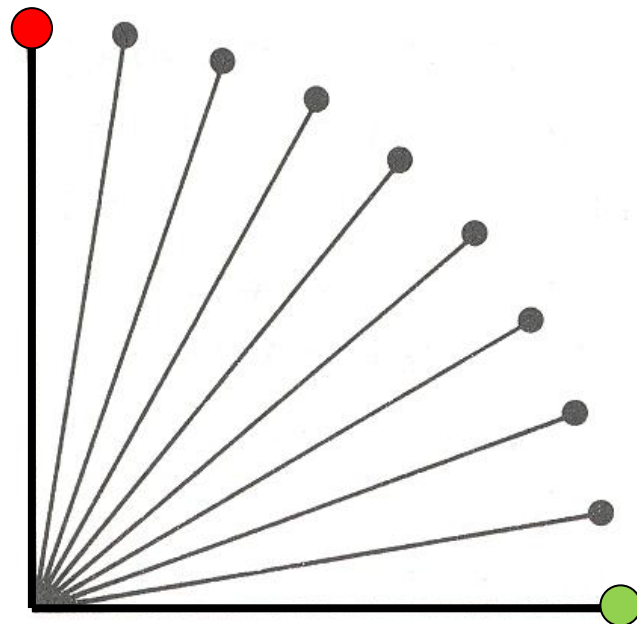
A: For translations, it doesn't make a difference (assuming the blend is translation equivariant).



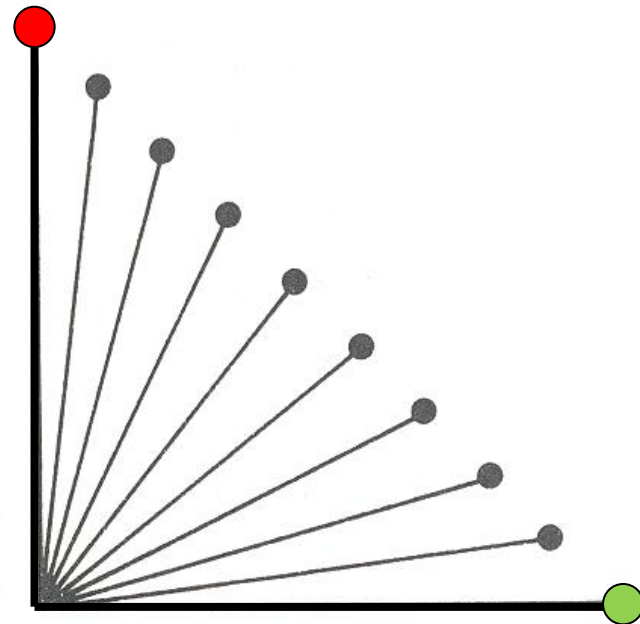
Keyframe Animation

Q: Why interpolate/blend joint parameters instead of interpolating/blending vertices directly?

A: For rotations, it could lead to geometric distortion.



Good arm



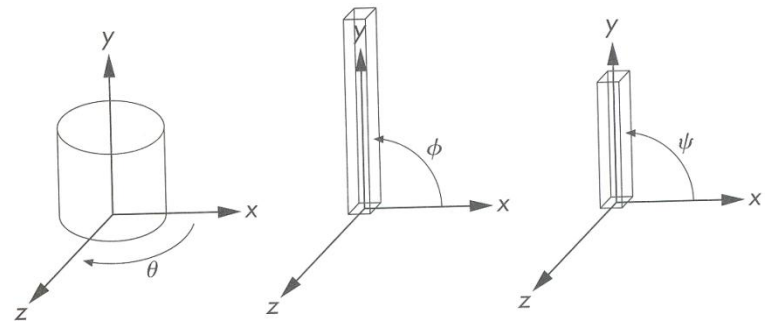
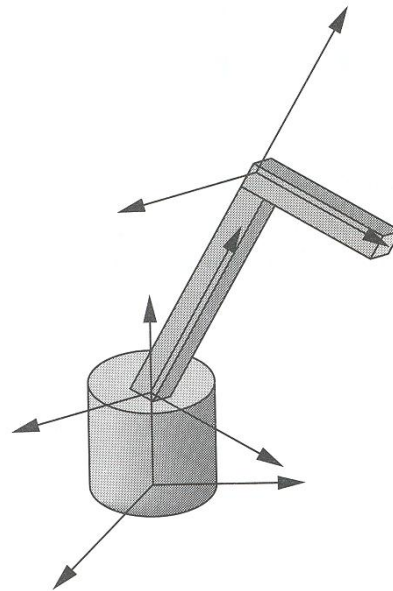
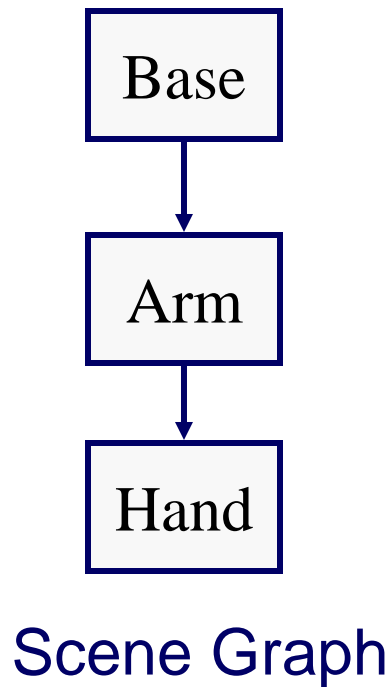
Bad arm

Watt & Watt



Articulated Figures

- Character poses described by set of rigid bodies connected by “joints”

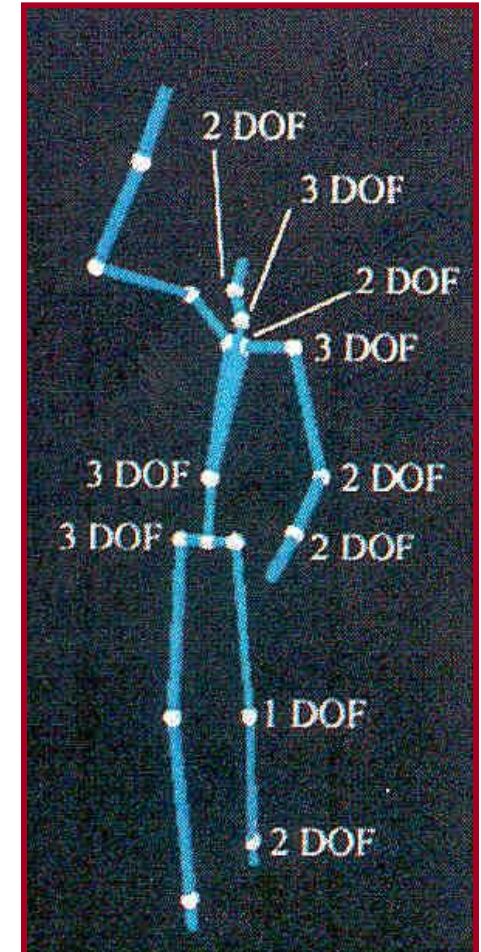
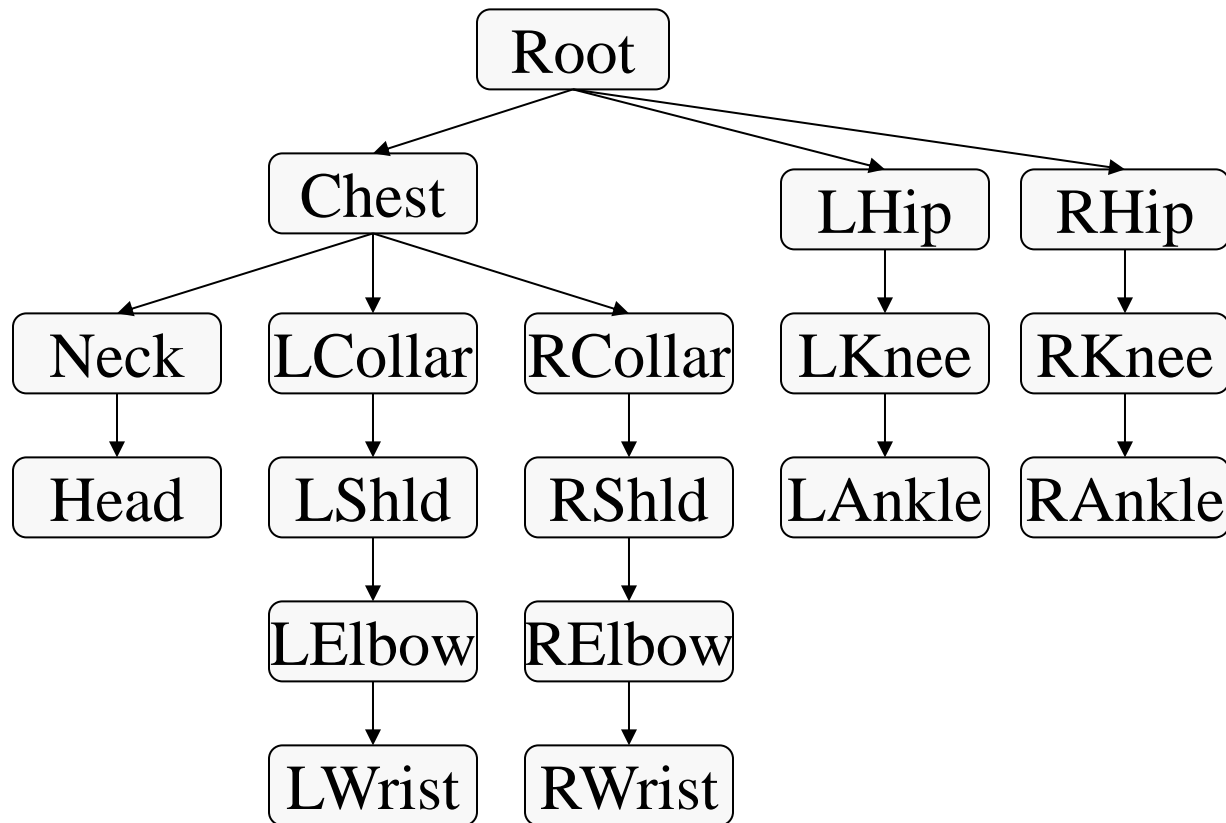


Angel Figures 8.8 & 8.9



Articulated Figures

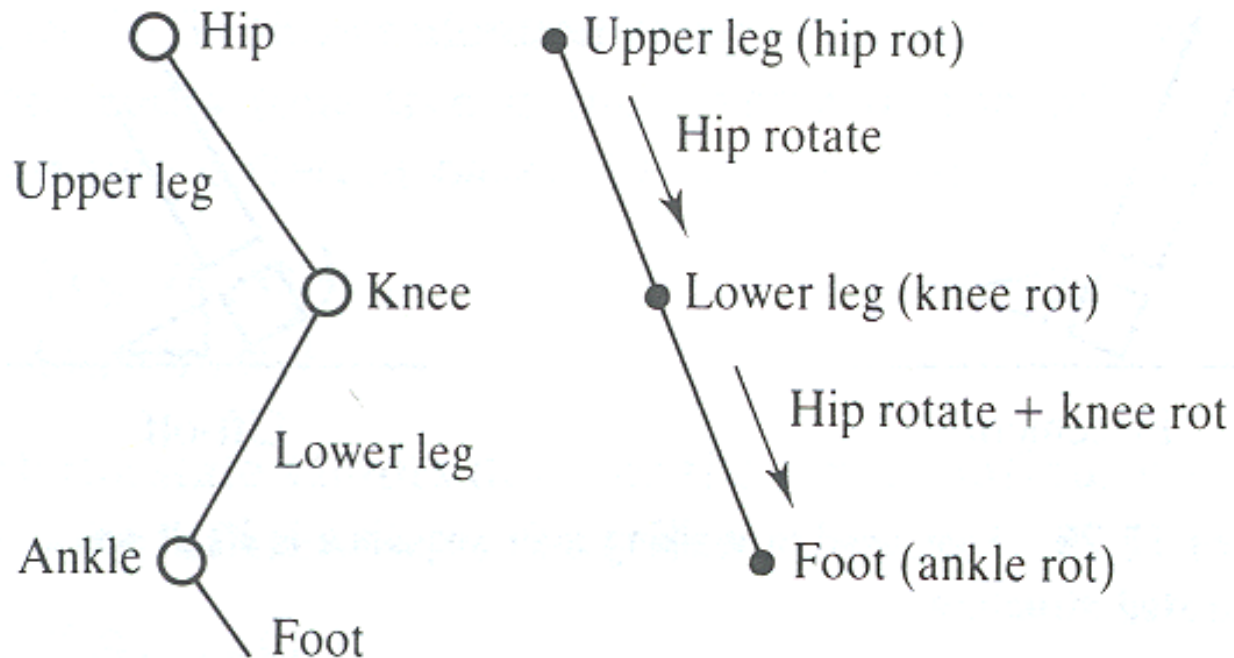
- Character poses described by set of rigid bodies connected by “joints”





Example: Walk Cycle

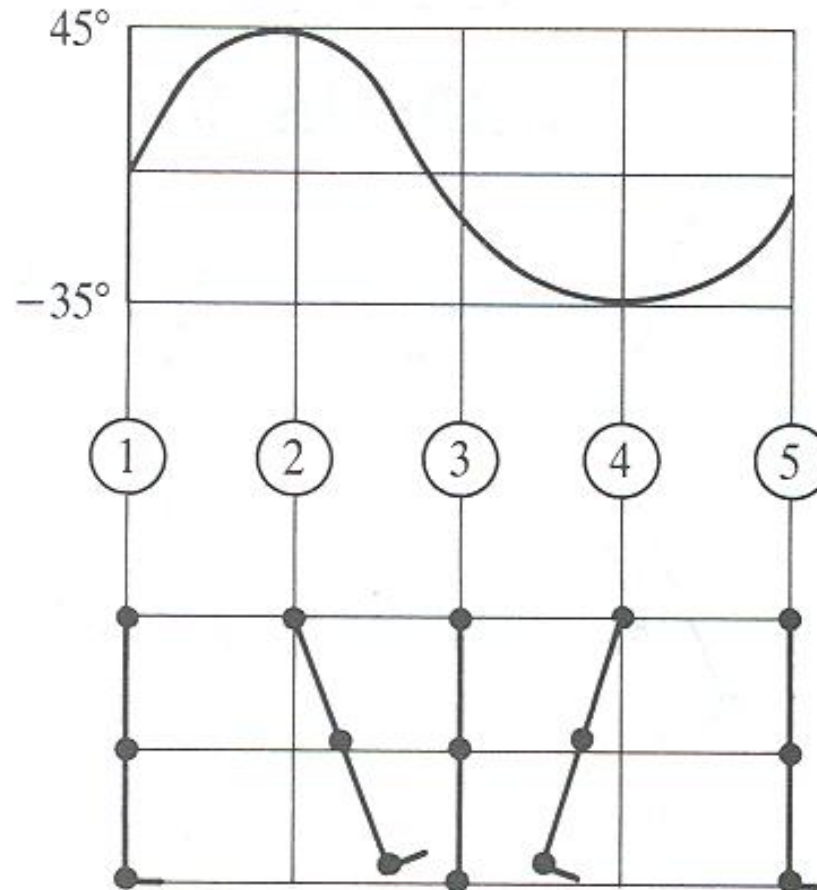
- Articulated figure:





Example: Walk Cycle

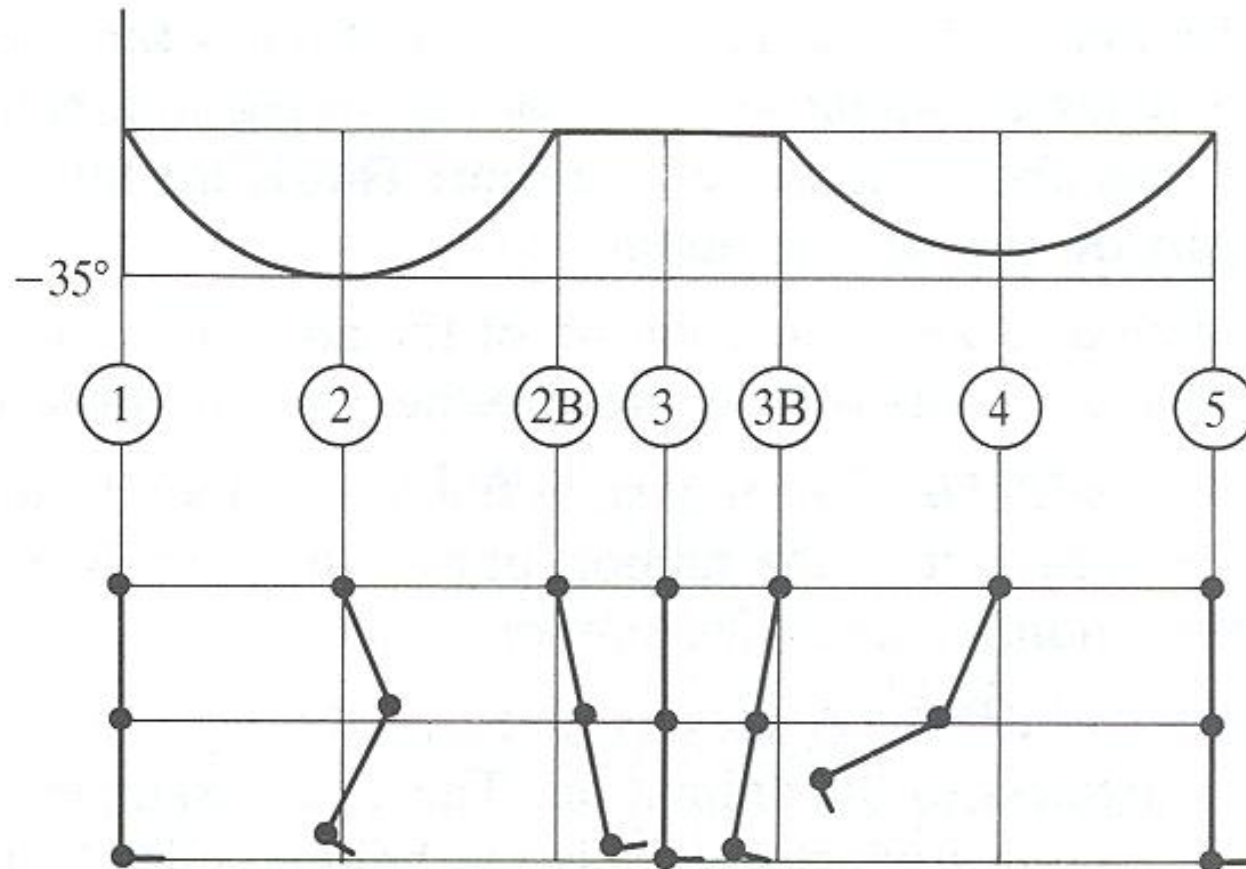
- Hip joint orientation:





Example: Walk Cycle

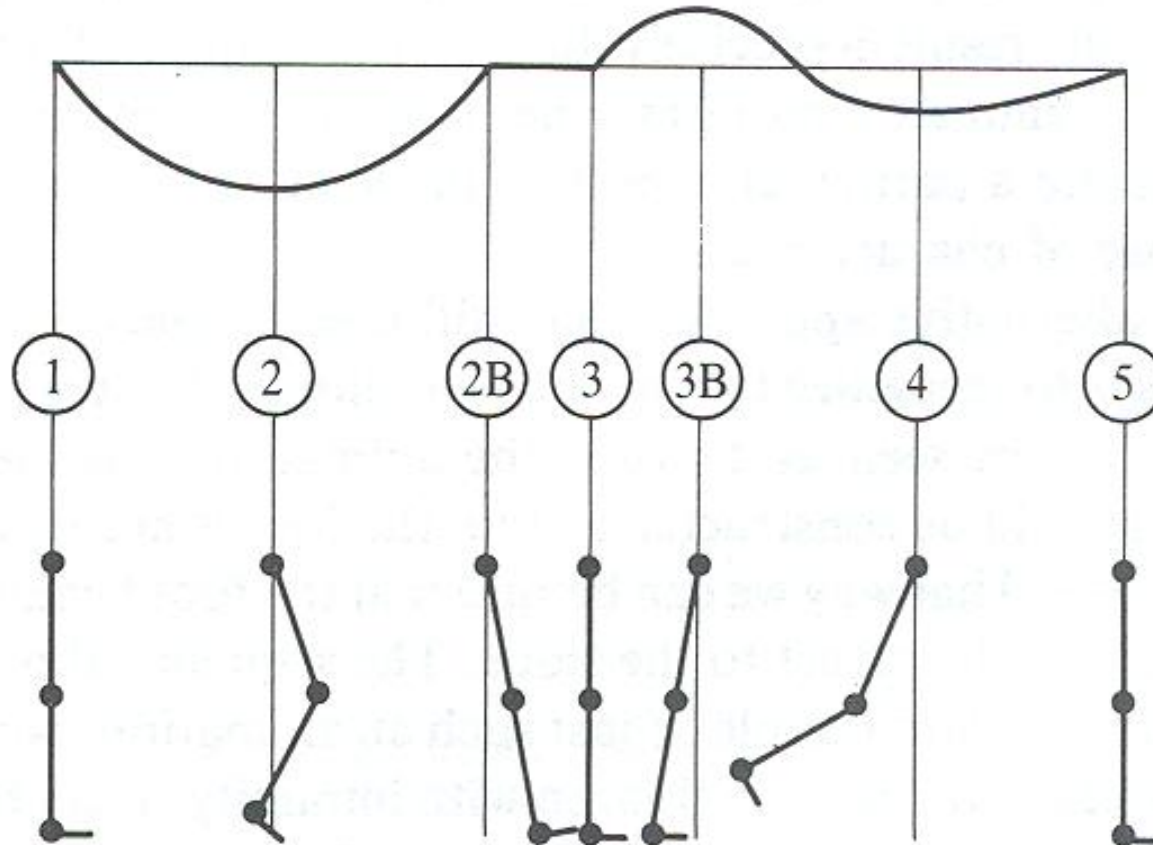
- Knee joint orientation:





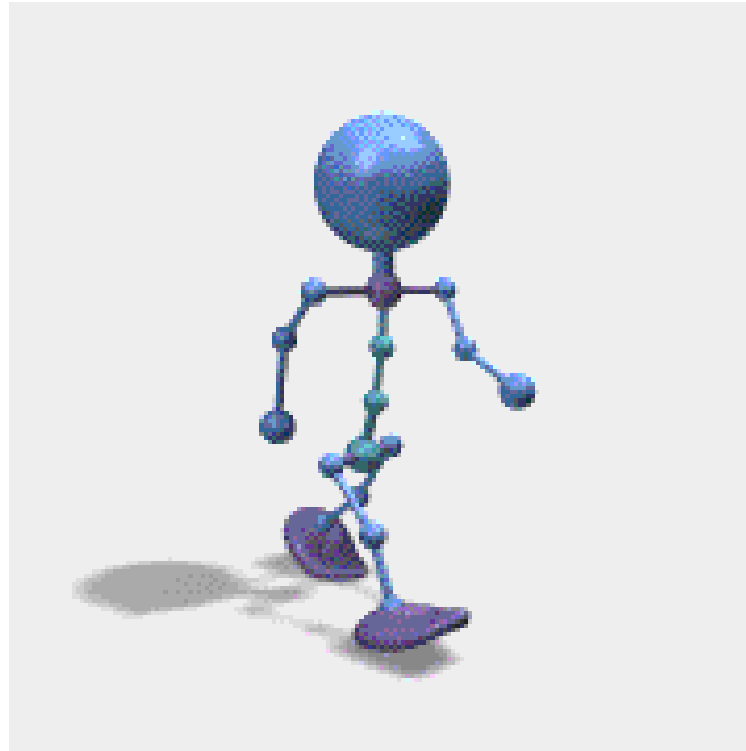
Example: Walk Cycle

- Ankle joint orientation:





Example: Walk Cycle



<http://www.ischool.utexas.edu/~luna73/architecture/>

Will discuss the how of blending joint parameters next time.



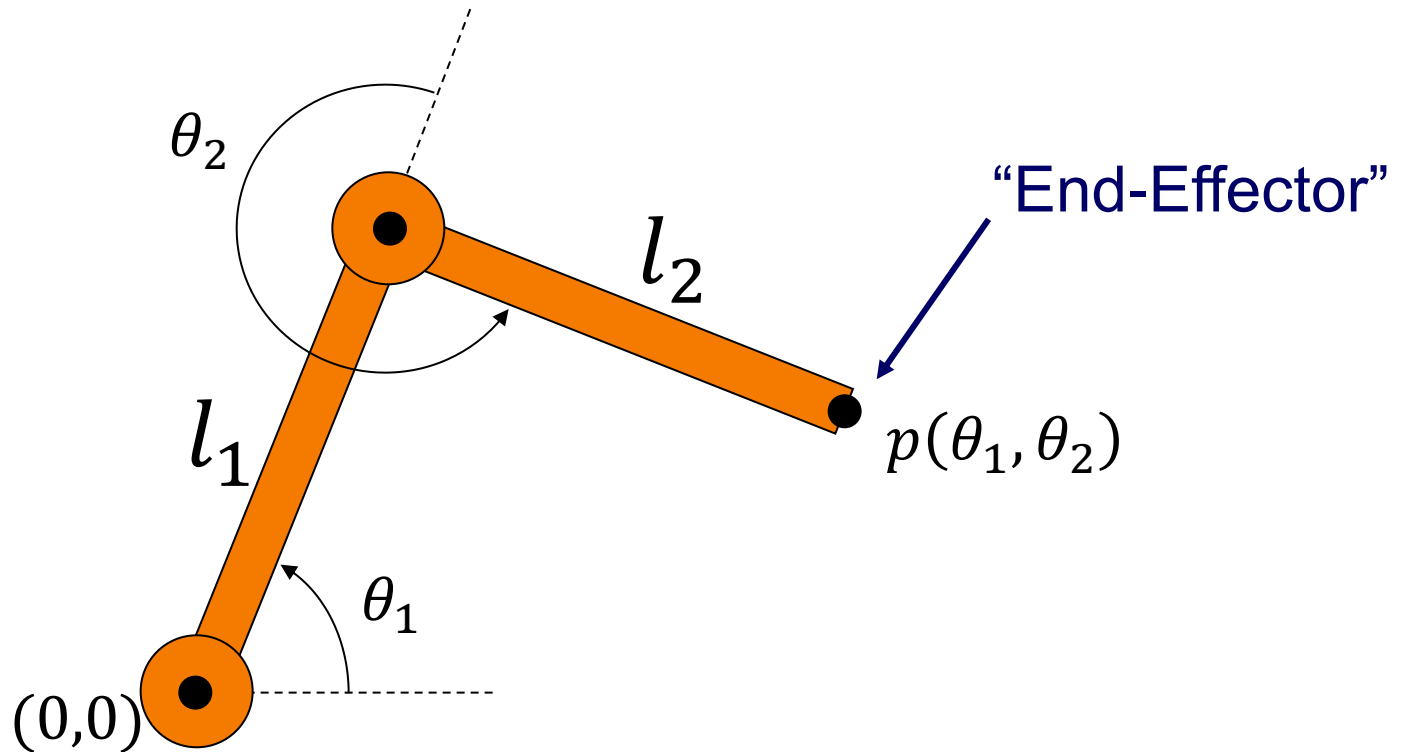
Kinematics and Dynamics

- Kinematics: *Study of motion w/o regard for the cause*
 - Considers only motion
 - Determined by positions, velocities, accelerations
- Dynamics: *Study of the cause of motion*
 - Considers underlying forces and interactions
 - Compute motion from initial conditions and physics



Example: 2-Link Structure

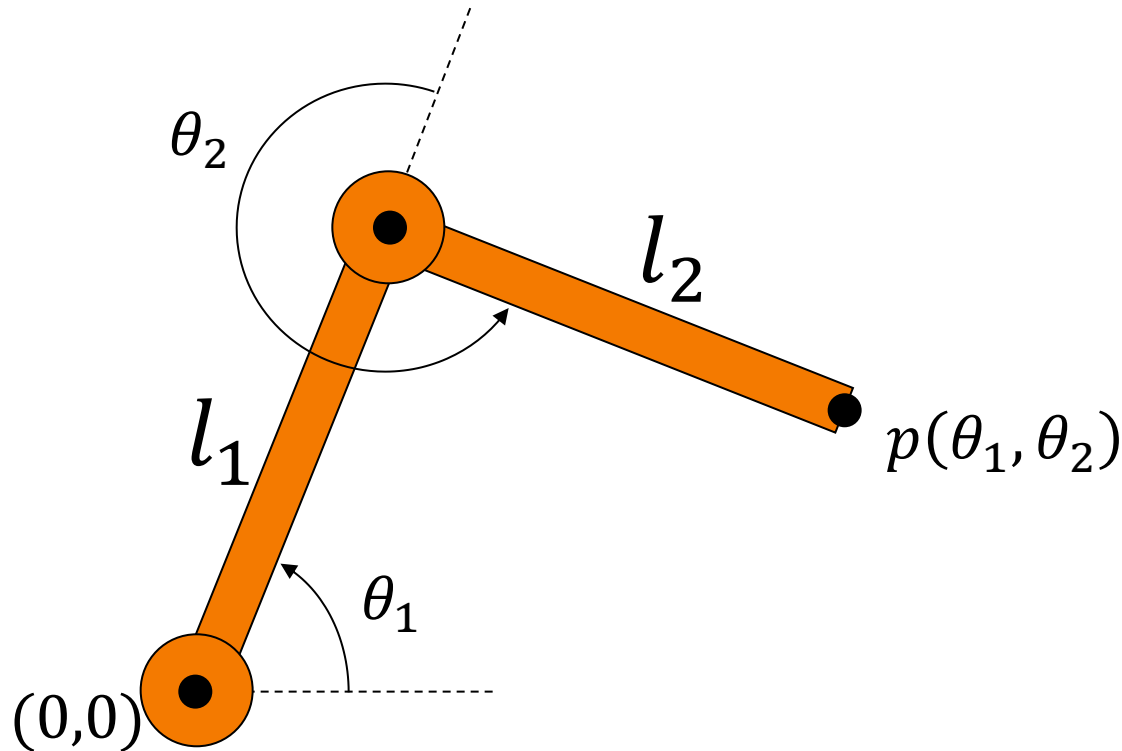
- Two links connected by rotational joints





Forward Kinematics

- Animator specifies joint angles: θ_1 and θ_2
- Computer finds positions of end-effector: $p(\theta_1, \theta_2)$

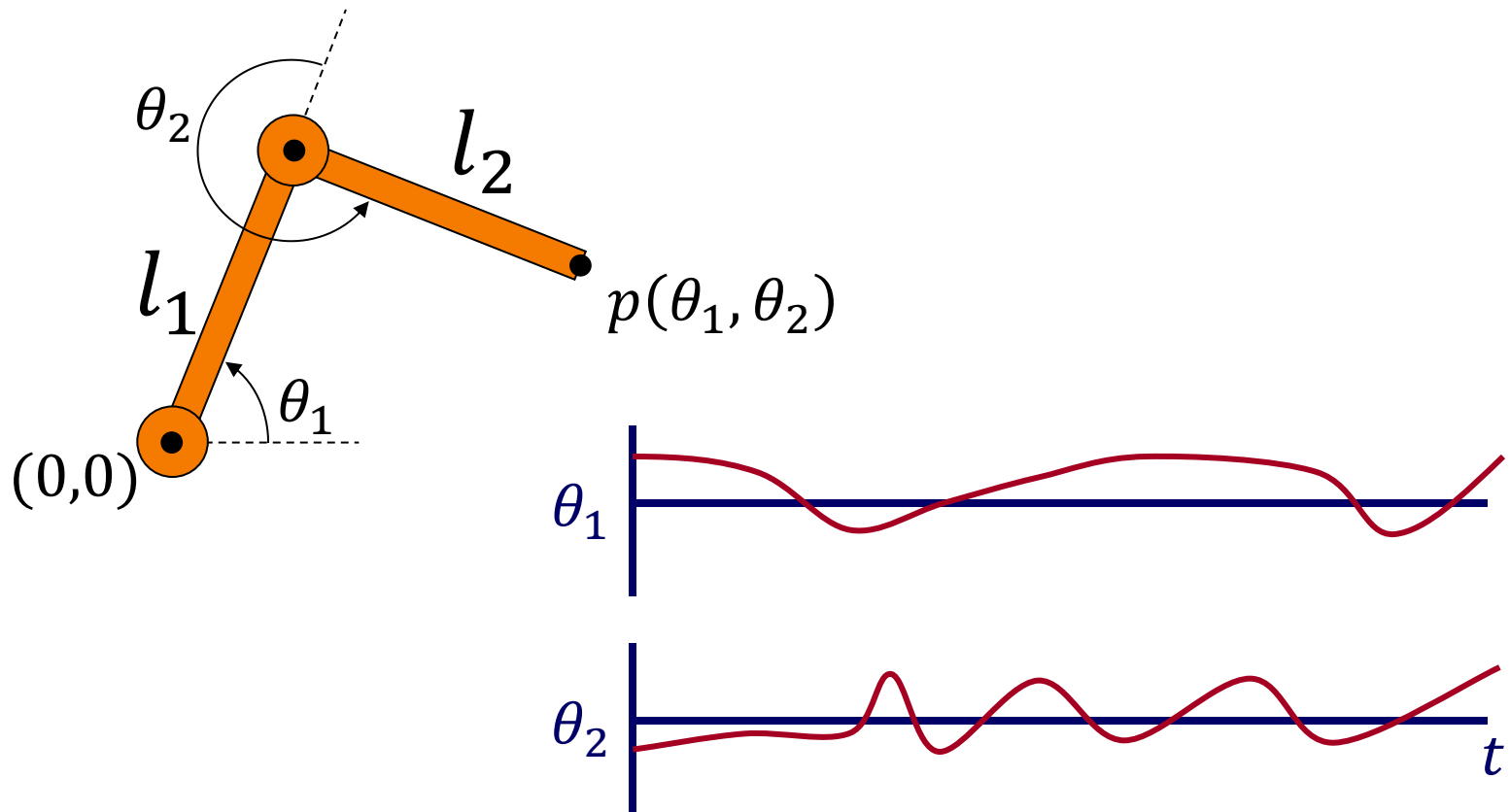


$$p(\theta_1, \theta_2) = (l_1 \cos \theta_1 + l_2 (\cos(\theta_1 + \theta_2)), l_1 \sin \theta_1 + l_2 \sin(\theta_1 + \theta_2))$$



Forward Kinematics

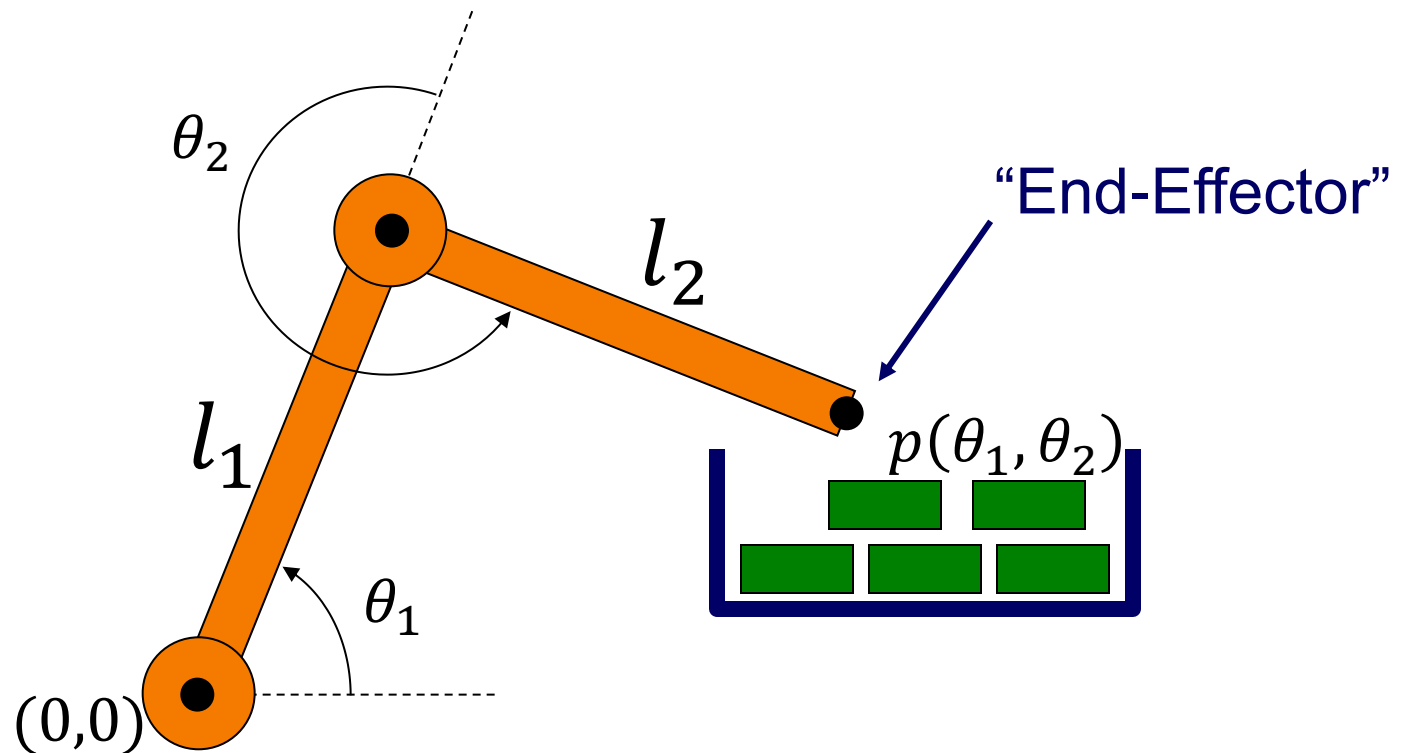
- Joint motions can be specified by spline curves





Example: 2-Link Structure

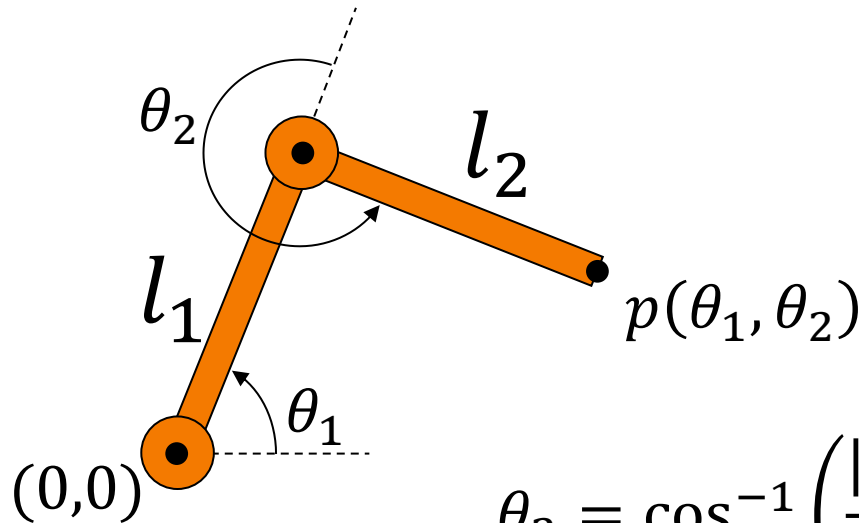
- What if animator knows position of “end-effector”





Inverse Kinematics

- Animator specifies end-effector positions: p
- Computer finds joint angles: θ_1 and θ_2



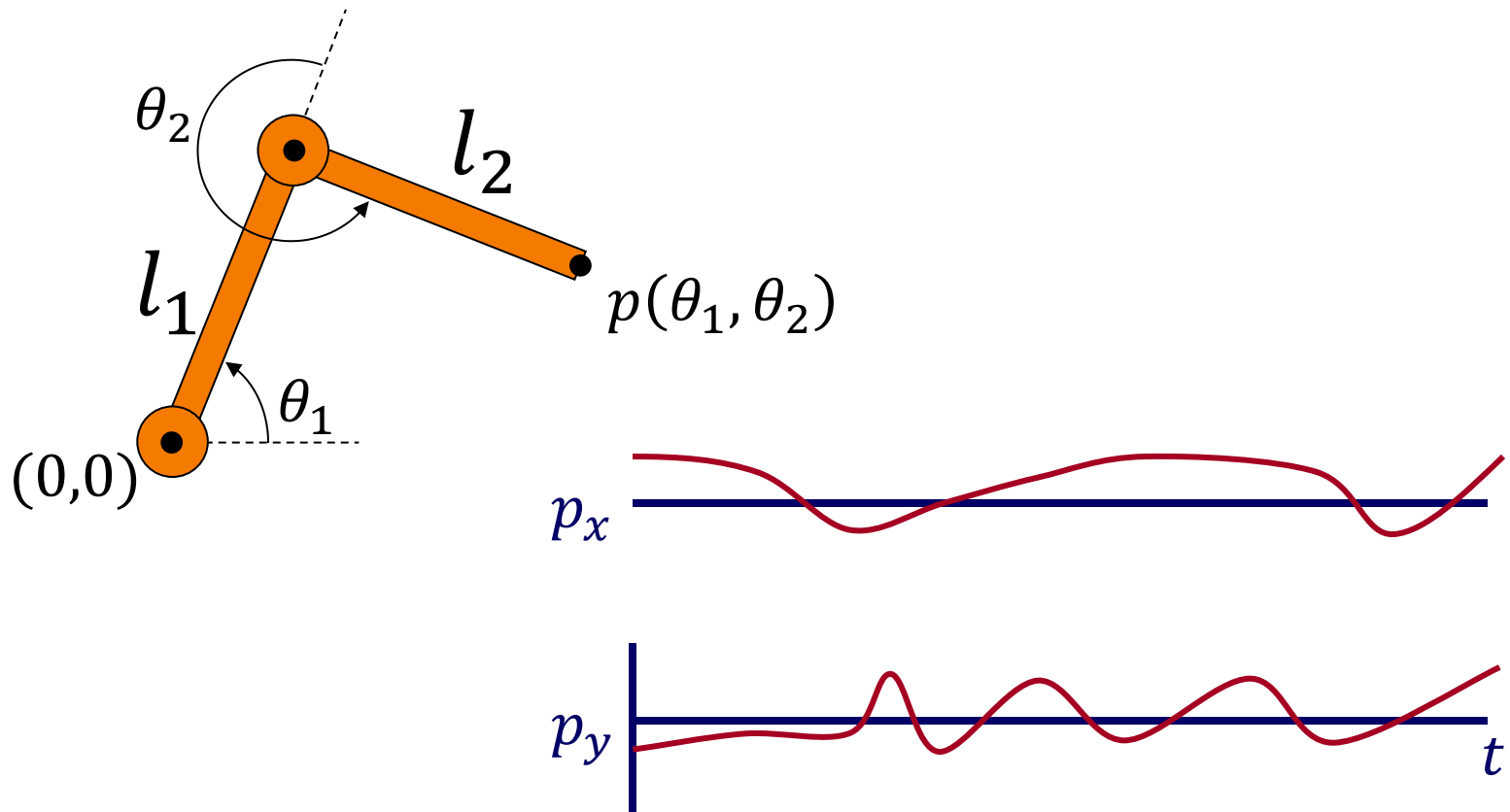
$$\theta_2 = \cos^{-1} \left(\frac{|p|^2 - l_1^2 - l_2^2}{2l_1 l_2} \right)$$

$$\theta_1 = \tan^{-1} \left(\frac{p_y}{p_x} \right) - \tan^{-1} \left(\frac{l_2 \sin \theta_2}{l_1 + l_2 \cos \theta_2} \right)$$



Inverse Kinematics

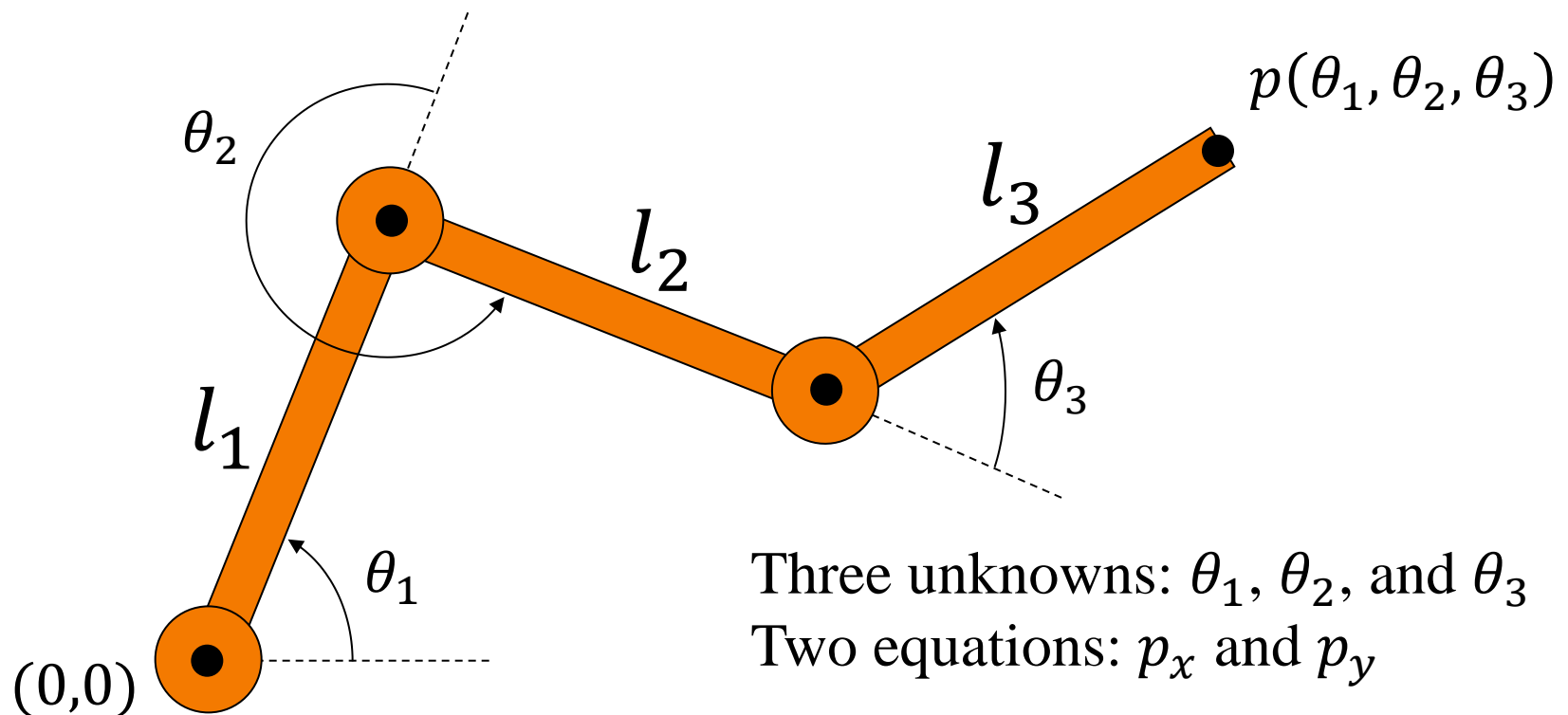
- End-effector positions can be specified by splines





Inverse Kinematics

- Challenges for more complex structures
 - Not guaranteed to have one solution
 - » May be able to find best/closest solution
 - System can be non-linear (i.e. hard to solve)





Summary of Kinematics

- Forward kinematics
 - Specify conditions (joint angles)
 - Compute positions of end-effectors
- Inverse kinematics
 - “Goal-directed” motion
 - Specify goal positions of end effectors
 - Compute conditions required to achieve goals

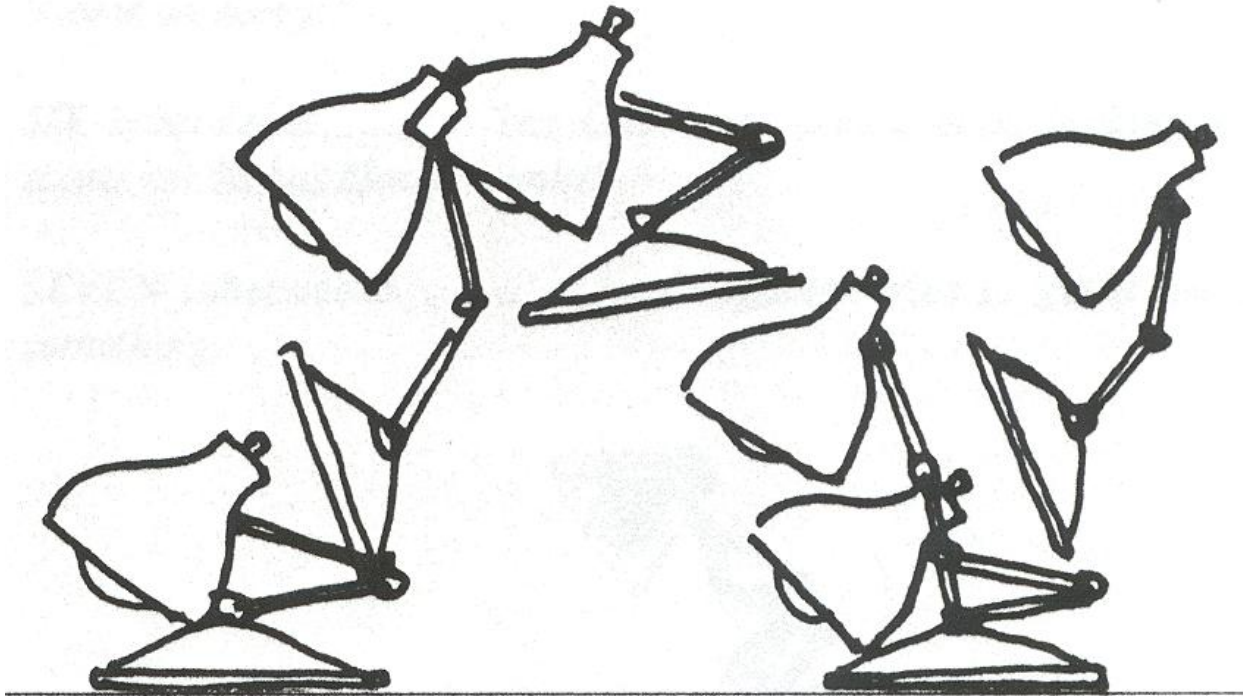


Inverse kinematics provides easier specification for many animation tasks, but it is computationally more difficult



Dynamics

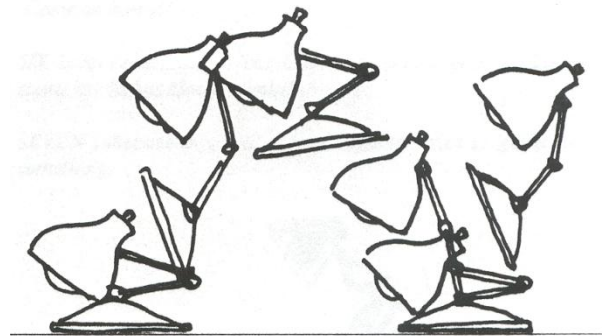
- Simulate physics to obtain motion that is responsive / realistic





Dynamics

- Animator specifies constraints:
 - What the character's physical structure is
 - » e.g., articulated figure
 - What the character has to do
 - » e.g., jump from here to there within time t
 - What other physical structures are present
 - » e.g., floor to push off and land
 - How the motion should be performed
 - » e.g., minimize energy





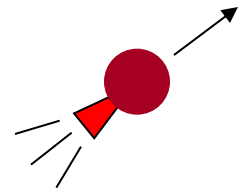
Dynamics

Computer finds the “best” physical motion satisfying the constraints (e.g. by minimizing some objective)

Example: particle with jet propulsion

- $\mathbf{x}(t)$ is position of particle at time t
- $\mathbf{f}(t)$ is the directional force of jet propulsion at time t
- Particle's equation of motion is:

$$0 = m(\ddot{\mathbf{x}} - \mathbf{g}) - \mathbf{f}$$



- In a unit of time, move from \mathbf{a} to \mathbf{b} minimizing

$$E(\mathbf{x}) = \int_0^1 \|\mathbf{f}(t)\|^2 dt = \int_0^1 \|m(\ddot{\mathbf{x}} - \mathbf{g})(t)\|^2 dt$$

$$\begin{aligned}\dot{\mathbf{x}} &= \frac{\partial \mathbf{x}}{\partial t} \\ \ddot{\mathbf{x}} &= \frac{\partial^2 \mathbf{x}}{\partial t^2}\end{aligned}$$

Such that:

$$\mathbf{x}(0) = \mathbf{a}, \dot{\mathbf{x}}(0) = \mathbf{0}, \mathbf{x}(1) = \mathbf{b}, \text{ and } \dot{\mathbf{x}}(1) = \mathbf{0}$$



Dynamics

Turn into a discrete problem by partitioning time into N uniform intervals (of size $h = \frac{1}{N}$) giving discrete positions $\{\mathbf{x}_0, \dots, \mathbf{x}_N\}$, with $\mathbf{x}_i = \mathbf{x}(i \cdot h)$:

$$\dot{\mathbf{x}}_i = \frac{\mathbf{x}_i - \mathbf{x}_{i-1}}{h}$$

$$\ddot{\mathbf{x}}_i = \frac{\dot{\mathbf{x}}_{i+1} - \dot{\mathbf{x}}_i}{h} = \frac{\mathbf{x}_{i+1} - 2\mathbf{x}_i + \mathbf{x}_{i-1}}{h^2}$$

$$\mathbf{f}_i = m(\ddot{\mathbf{x}}_i - \mathbf{g}) = m \left(\frac{\mathbf{x}_{i+1} - 2\mathbf{x}_i + \mathbf{x}_{i-1}}{h^2} - \mathbf{g} \right)$$



Dynamics

Turn into a discrete problem...

$$\mathbf{f}_i = m \left(\frac{\mathbf{x}_{i+1} - 2\mathbf{x}_i + \mathbf{x}_{i-1}}{h^2} - \mathbf{g} \right)$$

Optimization \Rightarrow minimizing a quadratic energy:

$$\begin{aligned} E(\mathbf{x}) &= \int_0^1 \|m(\ddot{\mathbf{x}} - \mathbf{g})\|^2 dt \\ &\approx h \sum_i \|m(\ddot{\mathbf{x}}_i - \mathbf{g})\|^2 \\ &= hm^2 \sum_i \left\| \frac{\mathbf{x}_{i+1} - 2\mathbf{x}_i + \mathbf{x}_{i-1}}{h^2} - \mathbf{g} \right\|^2 \end{aligned}$$

subject to $\mathbf{x}_{-1} = \mathbf{x}_0 = \mathbf{a}$ and $\mathbf{x}_N = \mathbf{x}_{N+1} = \mathbf{b}$.



Dynamics

Turn into a discrete problem...

$$\mathbf{f}_i = m \left(\frac{\mathbf{x}_{i+1} - 2\mathbf{x}_i + \mathbf{x}_{i-1}}{h^2} - \mathbf{g} \right)$$

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$$E(\mathbf{x}) = \int_0^1 \|m(\ddot{\mathbf{x}} - \mathbf{g})\|^2 dt$$
$$\approx h \sum_i \|m(\ddot{\mathbf{x}}_i - \mathbf{g})\|^2$$

$$\approx \frac{m}{2} \sum_i \|\mathbf{x}_{i+1} - 2\mathbf{x}_i + \mathbf{x}_{i-1} - h^2 \mathbf{g}\|^2$$

To minimize, need to find where the gradient is zero.
Since the energy is quadratic, the gradient is linear.

Reduces to solving a *linear* system of equations.

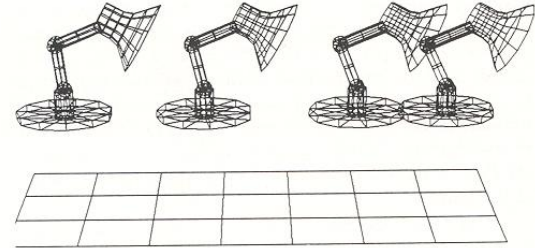
Dynamics



For simple scenarios:

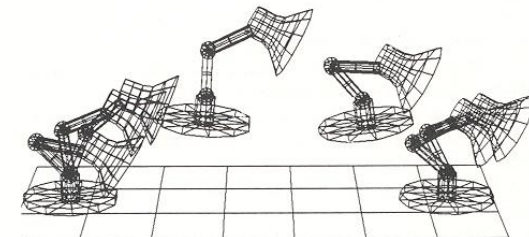
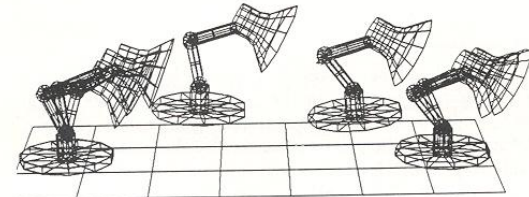
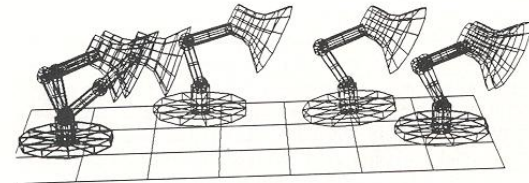
- Solve a linear system

$$\mathbf{Ax} = \mathbf{b}$$



For complex scenarios:

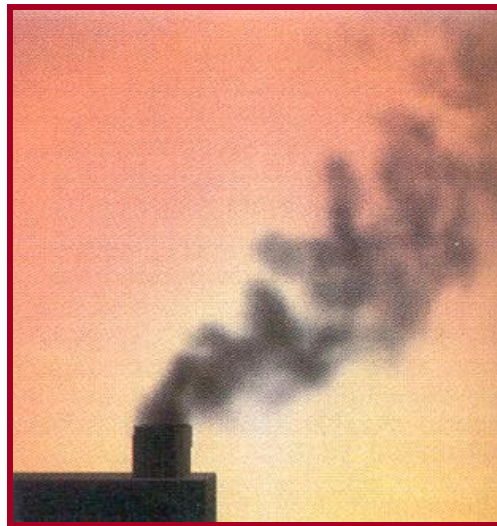
- Solve using iterative optimization techniques



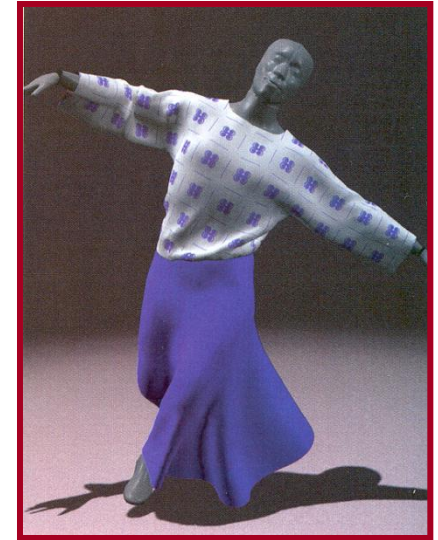
Dynamics



- Other physical simulations:
 - Rigid bodies
 - Soft bodies
 - Cloth
 - Liquids
 - Gases
 - etc.



Hot Gases
(Foster & Metaxas '97)



Cloth
(Baraff & Witkin '98)

Demo



Dynamics

- Advantages:
 - Free animator from having to specify details of physically realistic motion with spline curves
 - Easy to vary motions due to new parameters and/or new constraints
- Challenges:
 - Specifying constraints and objective functions
 - Avoiding local minima during optimization