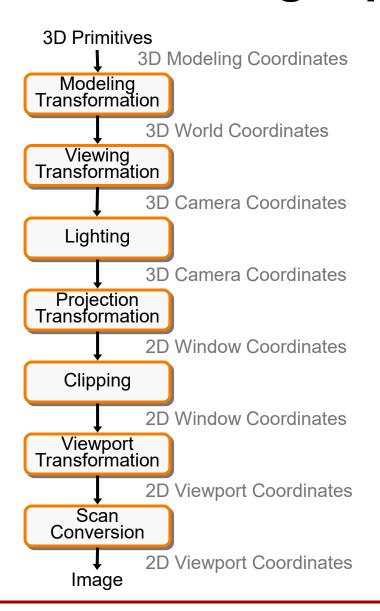


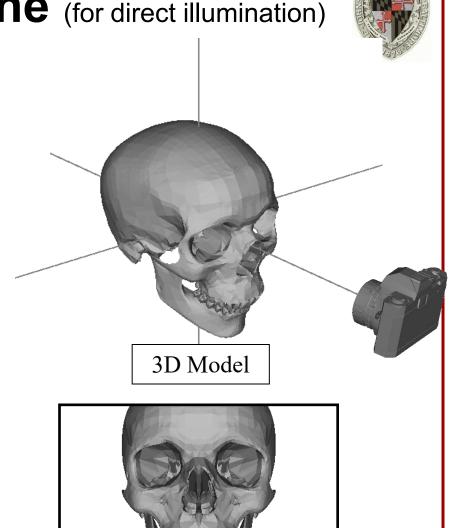
#### **Scan Conversion**

Michael Kazhdan

(601.457/657)

#### 3D Rendering Pipeline (for direct illumination)

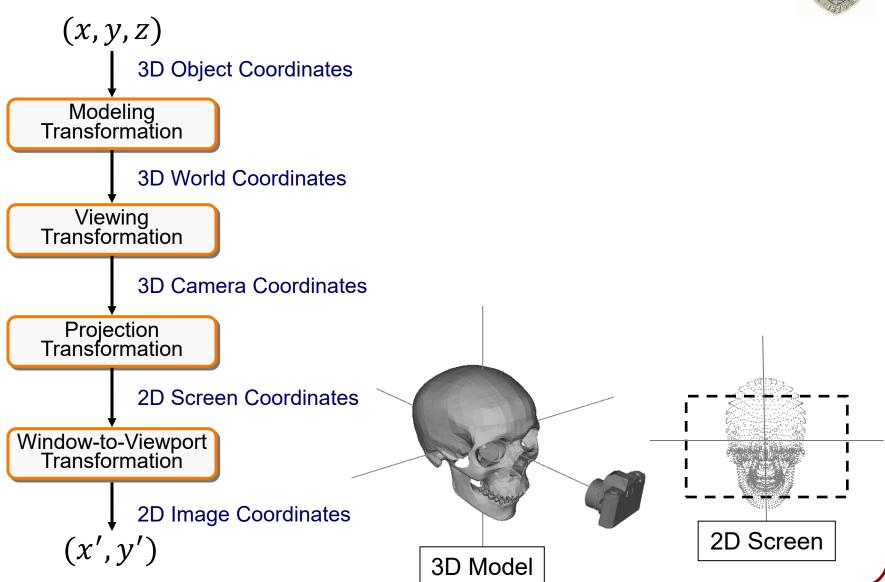


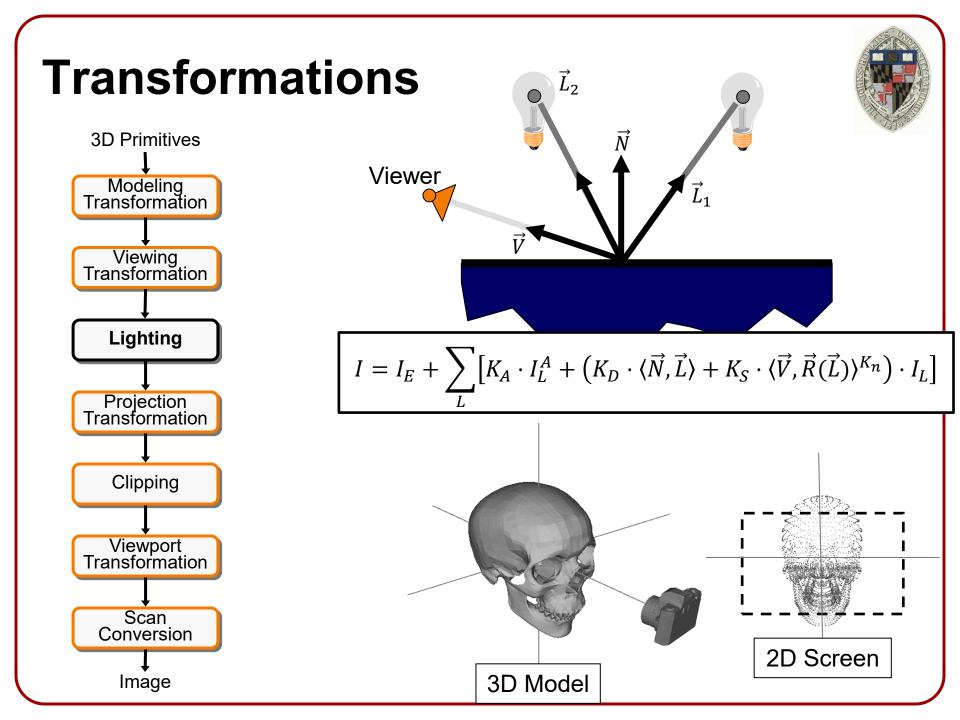


2D Viewport

#### 3D Rendering Pipeline (for direct illumination)

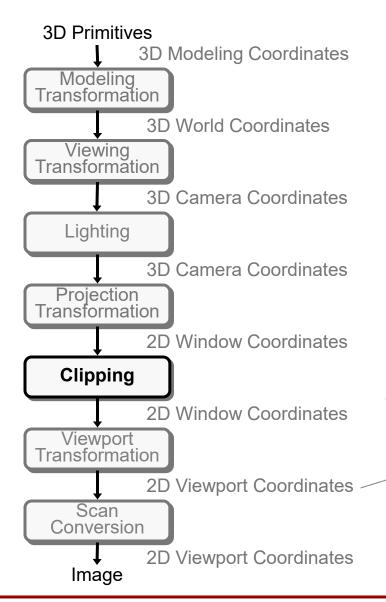






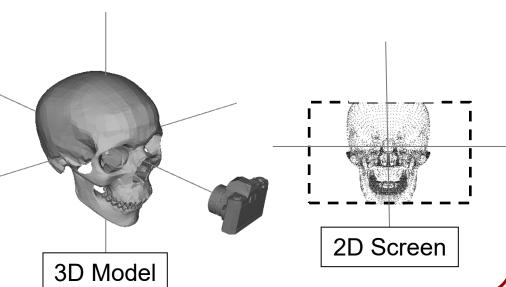
#### 3D Rendering Pipeline (for direct illumination)





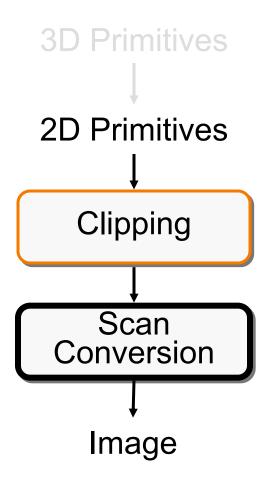
At this point we have the:

- Positions of the mesh vertices (including new vertices obtained through clipping)
- Color at each vertex.
- A list of (possibly clipped) polygons describing the intersection of the projected 3D polygons with the window.



### **2D Rendering Pipeline**





Clip portions of geometric primitives residing outside the window

Fill pixels representing primitives in viewport coordinates

#### **Overview**



#### Scan conversion

Figure out which pixels to fill

#### Shading

Determine a color for each filled pixel

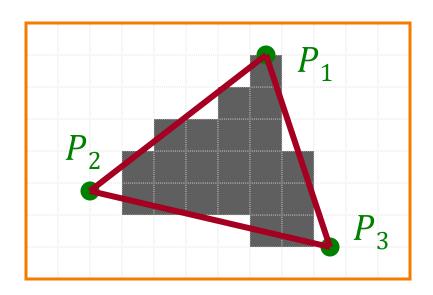
#### Depth test

Determine when pixel color should be overwritten

#### **Scan Conversion**



Render an image of a geometric primitive (specifically, a triangle) by setting interior pixel colors.

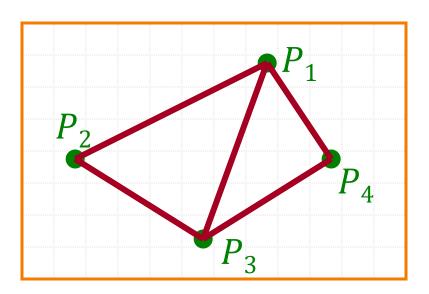


### **Triangle Scan Conversion**



Properties of a good algorithm

Must be fast

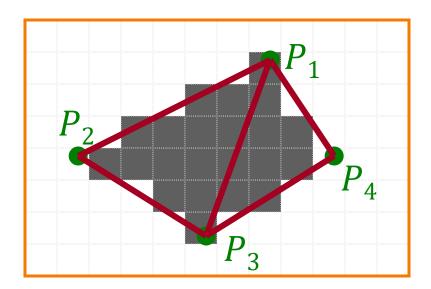


# **Triangle Scan Conversion**



#### Properties of a good algorithm

- Must be fast
- No cracks between adjacent primitives

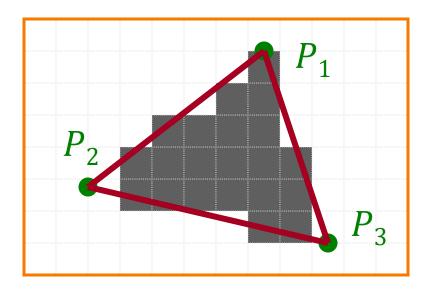


### Simple Algorithm



#### Color all pixels inside triangle

```
void ScanTriangle( Triangle T , Color rgba )
{
    for each pixel center in image (x,y)
    if( PointInsideTriangle( (x,y) , T ) )
        SetPixel( x , y , rgba );
}
```



### Line defines two halfspaces

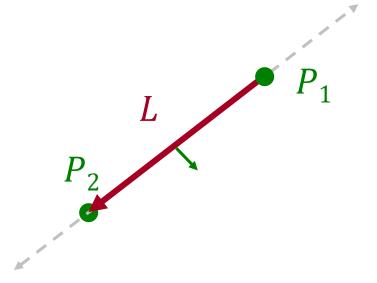


Test: use implicit equation for a line

$$\circ$$
 On line:  $ax + by + c = 0$ 

$$\circ$$
 To the right:  $ax + by + c < 0$ 

$$\circ$$
 To the left:  $ax + by + c > 0$ 

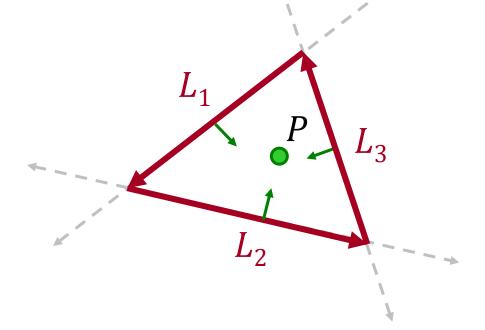


# **Inside Triangle Test**



Triangle vertices are ordered counter-clockwise (resp. clockwise):

⇒ Since triangles are convex, an interior point must be to the left (resp. right) of every bounding line.



### **Inside Triangle Test**



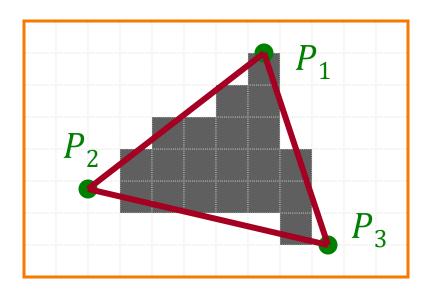
```
Boolean PointInsideTriangle(Point P, Triangle T)
  for each boundary line L of T
      Scalar d = L.a*P.x + L.b*P.y + L.c; if( d<0.0 ) return FALSE;
   return TRUE;
     Assumes triangle
    orientation is CCW.
```

### Simple Algorithm



What is bad about this algorithm?

```
void ScanTriangle( Triangle T , Color rgba )
{
    for each pixel center in image (x,y)
    if( PointInsideTriangle( (x,y) , T ) )
        SetPixel( x , y , rgba );
}
```



# **Triangle Sweep-Line Algorithm**

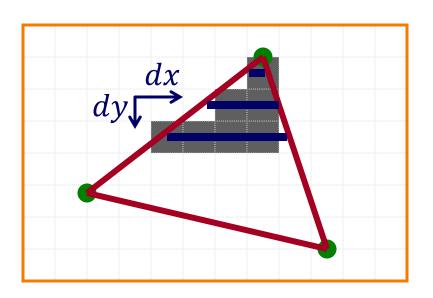


#### Take advantage of spatial coherence

Per row, interior pixels are bounded by left/right edges.

#### Take advantage of edge linearity

 Moving from row to row, left/right boundary change is determined by the slope.



# **Triangle Sweep-Line Algorithm**



```
void ScanTriangle(Triangle T, Color rgba)
   for both edge pairs
       initialize x_L, x_R, y; compute dx_L/dy_L and dx_R/dy_R;
        until y reaches the first end-point
            for(int x=x_L; x <= x_R; x++) SetPixel(x, y, rgba);
            x_L += dx_L/dy_L;

x_R += dx_R/dy_R;
                                                  dx_I
```

# **Triangle Sweep-Line Algorithm**



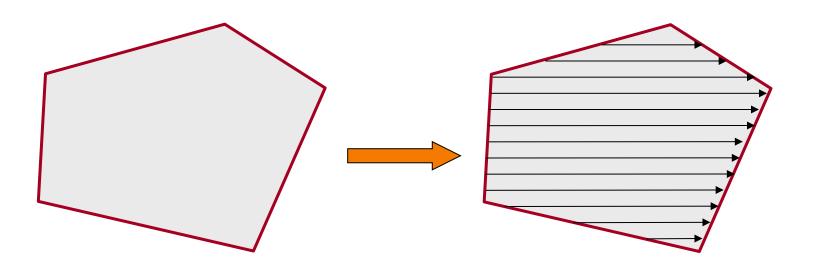
```
void ScanTriangle (Triangle T, Color rgba)
   for both edge pairs
        initialize x_L, x_R, y; compute dx_L/dy_L and dx_R/dy_R;
        until y reaches the first end-point
             for(int x=x_L; x <= x_R; x++) SetPixel(x, y, rgba);
             x_L += dx_L/dy_L;

x_R += dx_R/dy_R;
                                                                         dx_R
                                                                                \mathcal{X}_{R}
```



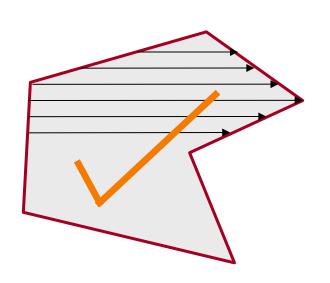
Will the method work for convex polygons?

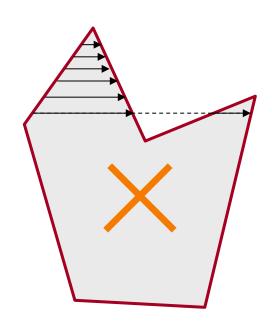
 Yes, since each scan line will only intersect the polygon at two points.





How about these polygons?

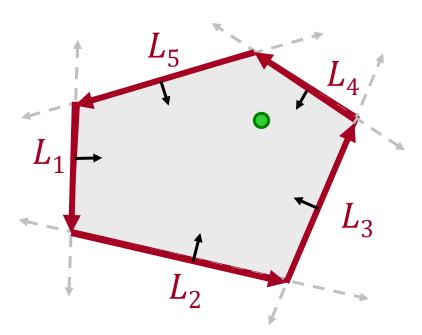




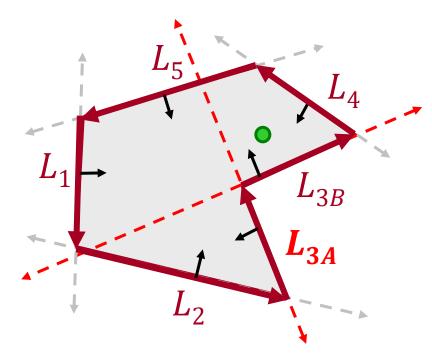


#### Need better test for points inside polygon

 Triangle sweep-line algorithm only generalizes to convex polygons



Convex Polygon

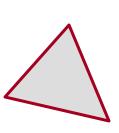


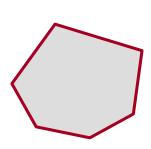
**Concave Polygon** 



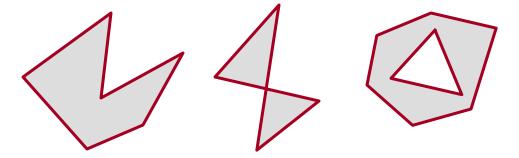
#### Fill pixels inside a polygon

- Triangle
- Convex
- Star-shaped
- Concave
- Self-intersecting
- Holes





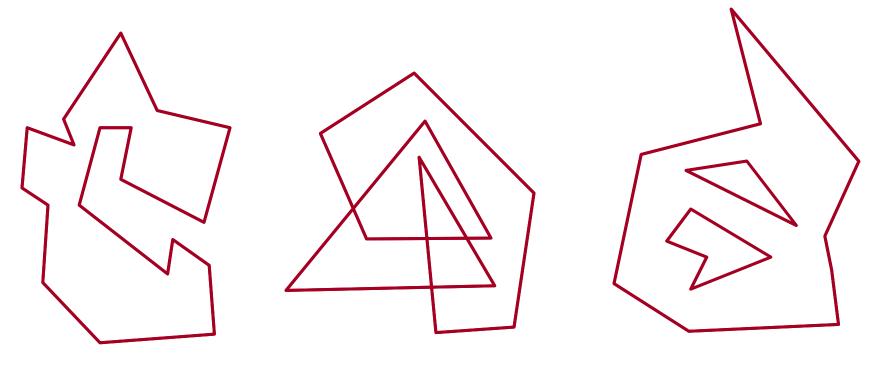




# Inside Polygon Rule



What is a good rule for which pixels are inside?



Concave

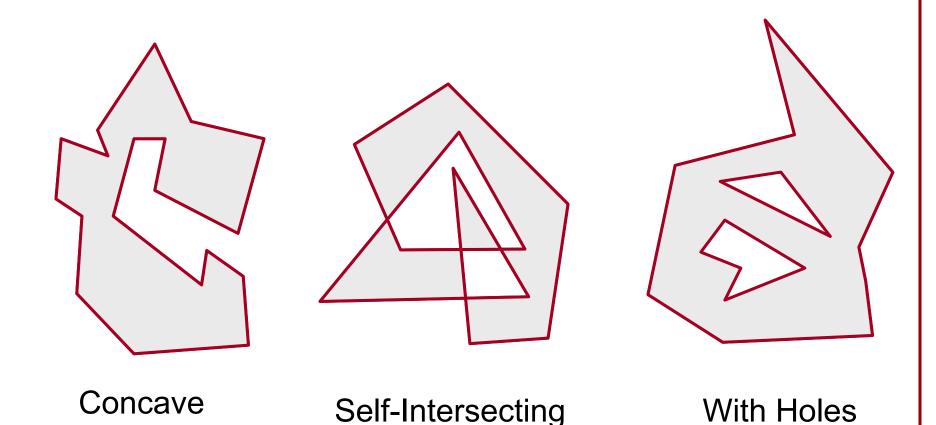
Self-Intersecting

With Holes

### Inside Polygon Rule



What is a good rule for which pixels are inside?

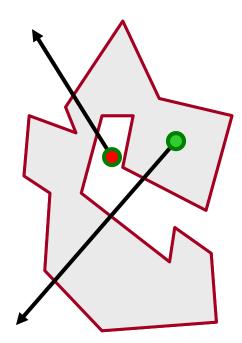


### Inside Polygon Rule

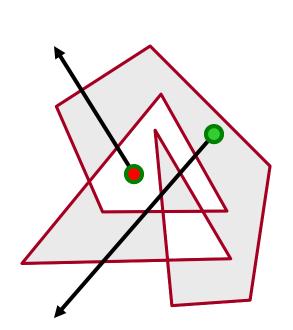


#### Odd-parity rule

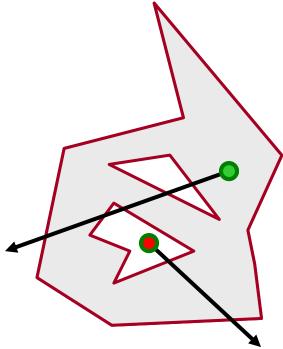
 Any ray from inside the shape, out to infinity, must cross an odd number of edges







Self-Intersecting



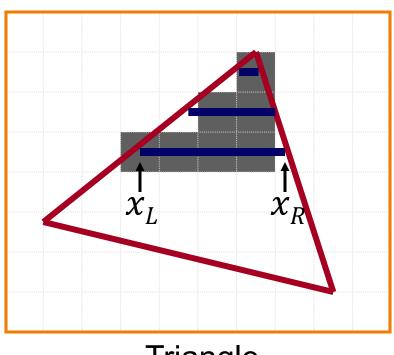
With Holes

# Polygon Sweep-Line Algorithm

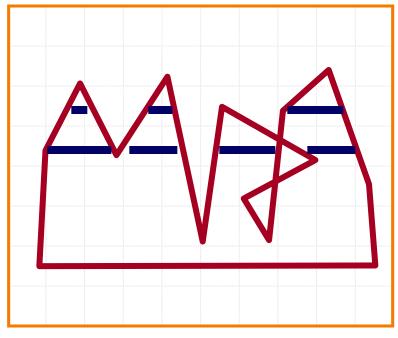


- Use incremental algorithm to find spans
- Determine "insideness" with odd (horizontal) parity rule

Takes advantage of scan line coherence

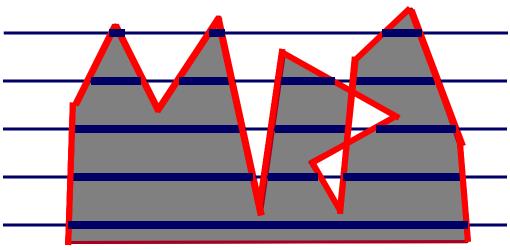


Triangle



Polygon

# Polygon Sweep-Line Algorithm

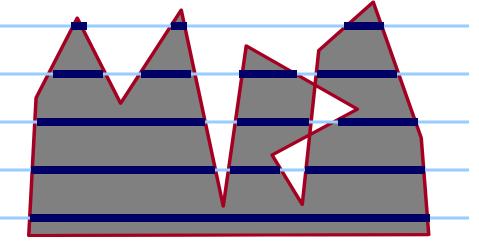


# Polygon Sweep-Line Algorithm



#### **Observation**:

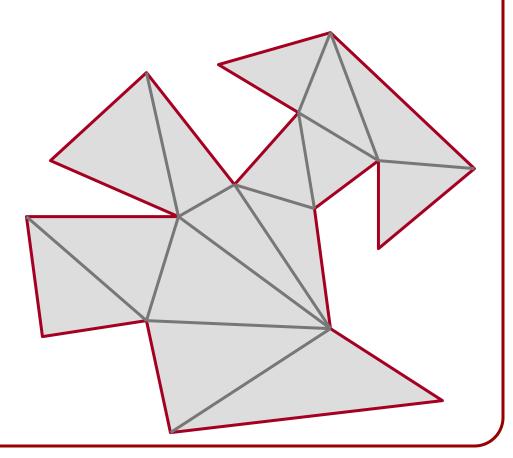
Don't have to do a full sort since ordering only changes when adjacent edges intersect.





Triangulate the polygon

Scan convert the triangles





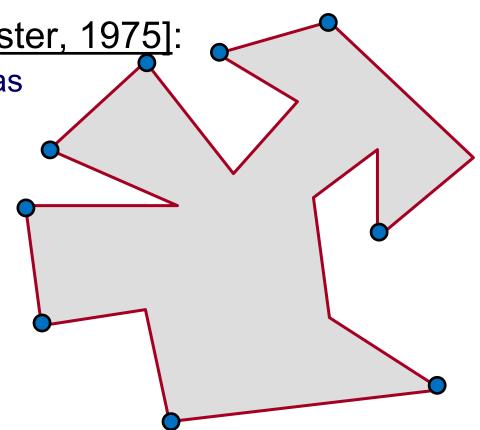
#### **Definition**:

A vertex of a simple polygon is an *ear* if the edge connecting its neighbors is inside the polygon.

Two Ear Theorem [Meister, 1975]:

Every simple polygon has at least two ears.

- 1. Clip off an ear
- 2. Repeat





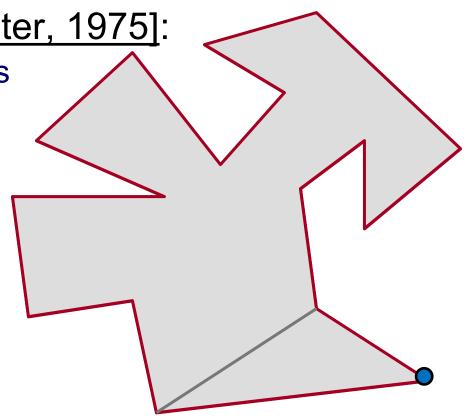
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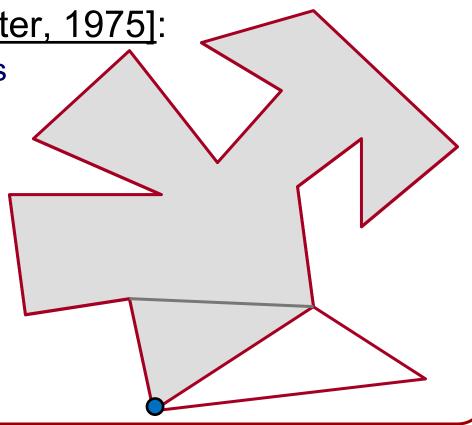
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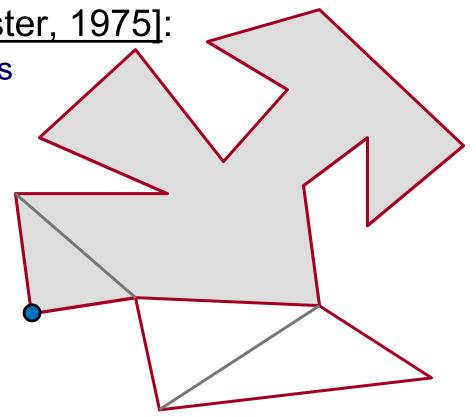
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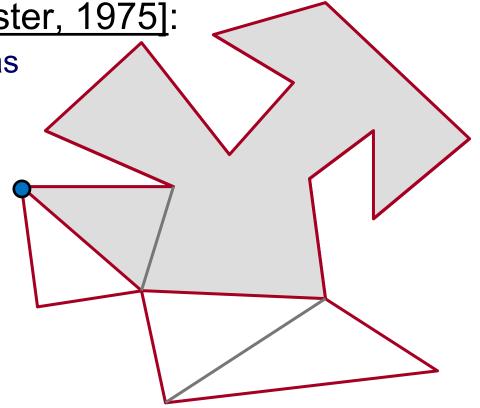
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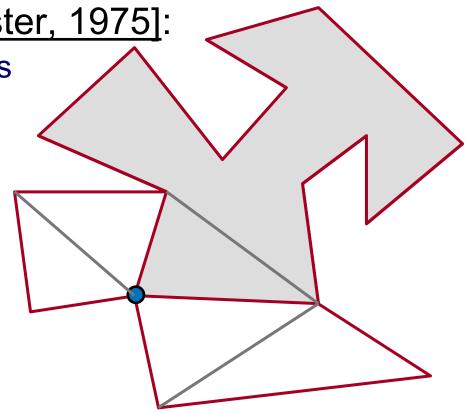
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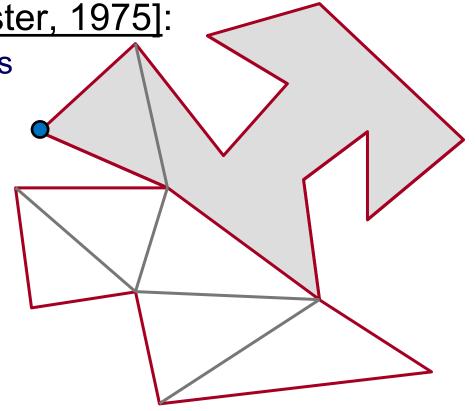
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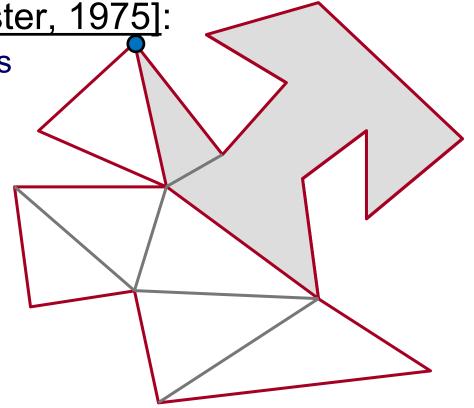
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- 2. Repeat





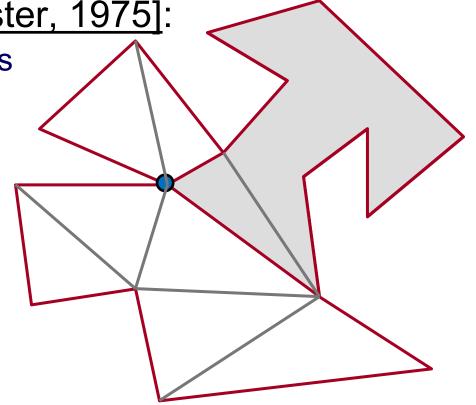
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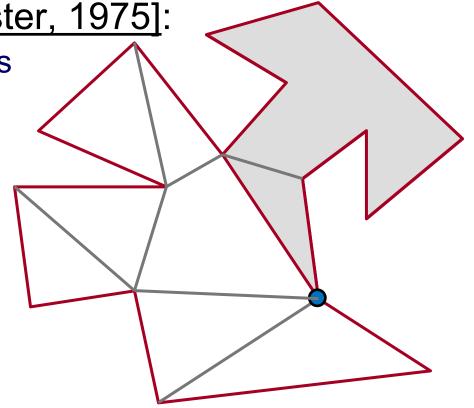
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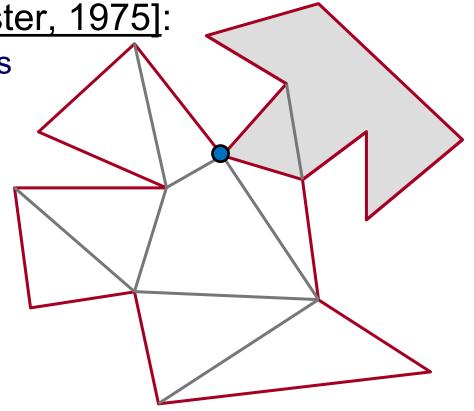
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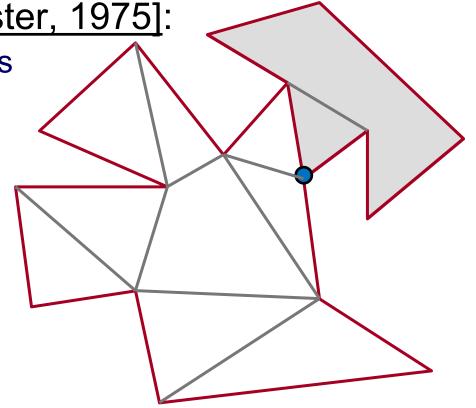
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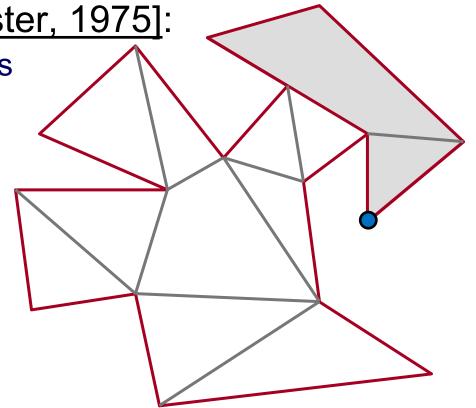
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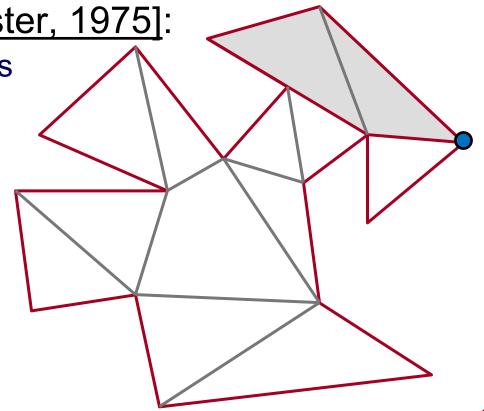
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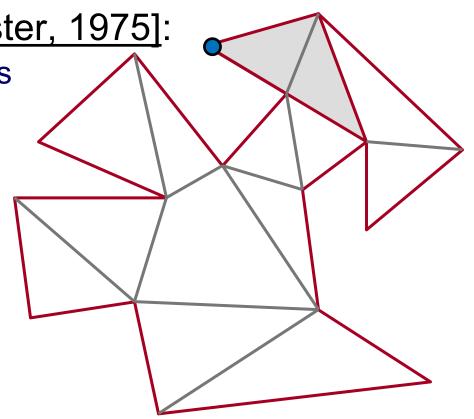
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- 2. Repeat





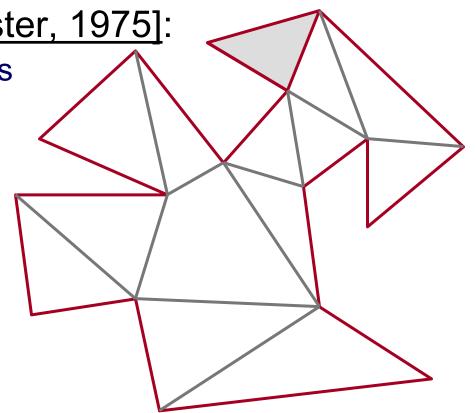
#### **Definition**:

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- 2. Repeat





#### **Definition**:

A vertex of a simple polygon is an *ear* if the edge connecting its neighbors is inside the polygon.

### Two Ear Theorem [Meister, 1975]:

Every simple polygon has at least two ears.

#### Alg Note:

OpenGL renders polygons, but it will assume that the polygon is *planar* and *convex*.

#### Recall:

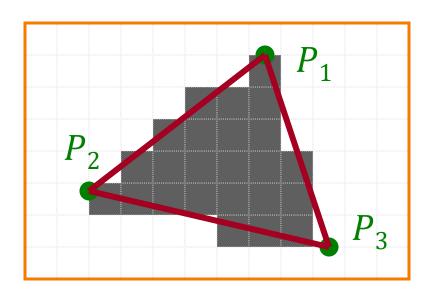
Even if you only pass in triangles for rendering, OpenGL may still have to render polygons after the triangle is clipped. But these are guaranteed to be *planar* and *convex*.

### **Scan Conversion**



### What about pixels on edges?

 If we set them either "on" or "off" we get aliasing or "jaggies" (similar to using nearest interpolation)



## **Scan Conversion**

### Example:



No Anti-Aliasing

# **Antialiasing Techniques**



### Display at higher resolution

- Corresponds to increasing sampling rate
- Not always possible (fixed size monitors, etc.)

### Modify pixel intensities

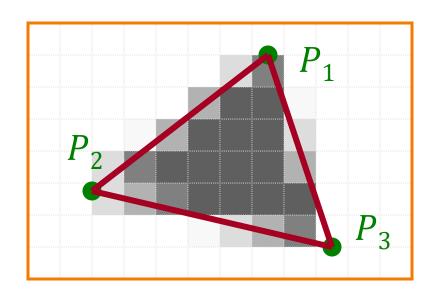
Vary pixel intensities along boundaries for antialiasing

### **Scan Conversion**



### What about pixels on edges?

- Setting them either "on" or "off" we get aliasing/"jaggies"
- Antialias by varying pixel intensities along boundaries

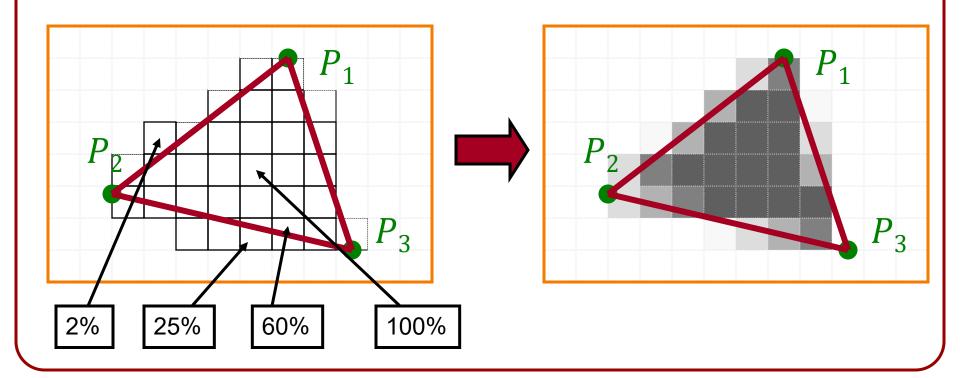


# **Antialiasing**



### Ideally – area sampling

- Calculate percent of pixel covered by primitive
- Multiply this percentage by desired intensity/color

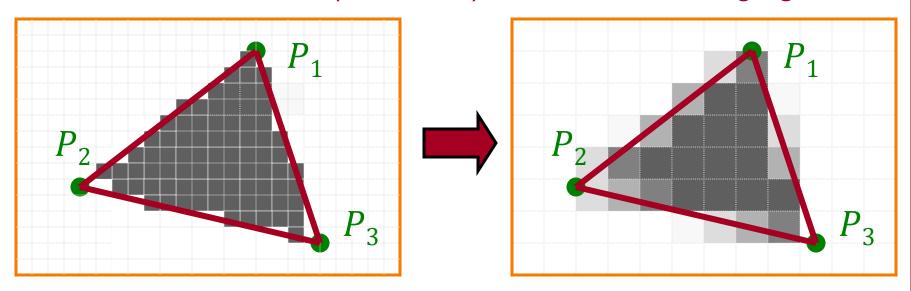


# **Antialiasing**



In practice – supersampling (aka postfiltering)

- Sample as if screen were higher resolution
- Average multiple samples to get final intensity
  - » This is done by rendering the scene multiple times with different (fractional) offsets and averaging



» The fractional value will be at a granularity determined by the number of rendering passes.

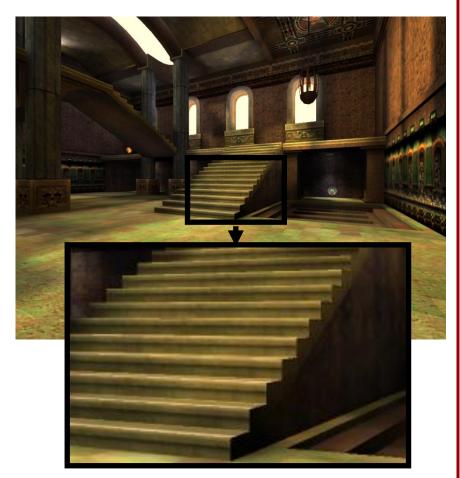
## **Scan Conversion**



### • Example:



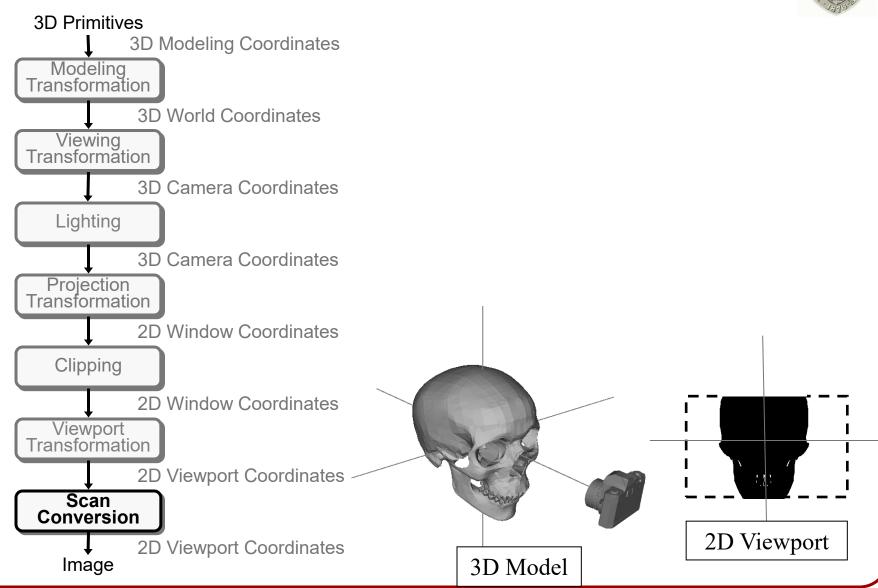
No Anti-Aliasing



4 x Anti-Aliasing
Images courtesy of NVIDIA

# 3D Rendering Pipeline (for direct illumination)





### **Overview**



#### Scan conversion

Figure out which pixels to fill

### Shading

Determine a color for each filled pixel

### Depth test

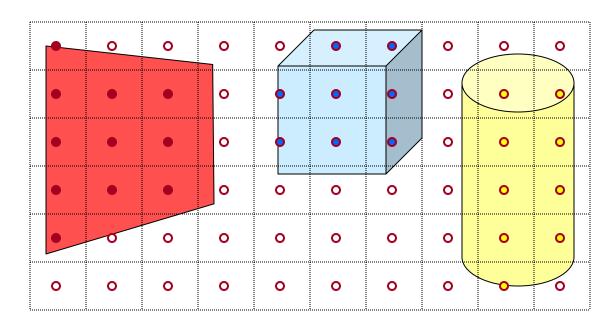
 Determine when the color of a pixel comes from the front-most primitive

# **Polygon Shading**



### Take advantage of spatial coherence

 Illumination calculations for pixels covered by same primitive are related to each other



$$I = I_E + \sum_{\vec{l}} \left[ K_A \cdot I_L^A + \left( K_D \cdot \langle \vec{N}, \vec{L} \rangle + K_S \cdot \langle \vec{V}, \vec{R}(\vec{L}) \rangle^{K_n} \right) \cdot I_L \right]$$

# **Polygon Shading Algorithms**



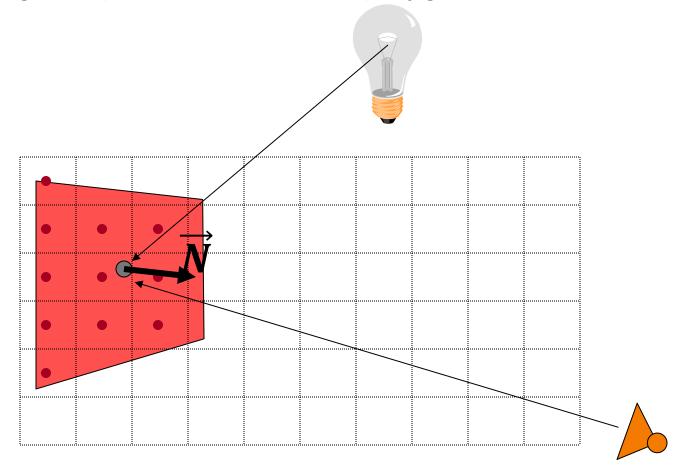
### Shading models:

- Flat
- Gouraud
- Phong



### One lighting calculation per polygon

Assign all pixels inside each polygon the same color



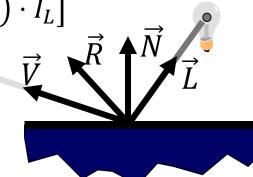


### Take advantage of spatial coherence

 Make the lighting equation constant over the surface of each primitive

	Surface Normal	Light Direction	View Direction
Emissive	-	-	-
Ambient	-	-	-
Diffuse	+	+	-
Specular	+	+	+

$$I = I_E + \sum_{L} \left[ K_A \cdot I_L^A + \left( K_D \cdot \langle \vec{N}, \vec{L} \rangle + K_S \cdot \langle \vec{V}, \vec{R}(\vec{L}) \rangle^{K_n} \right) \cdot I_L \right]$$





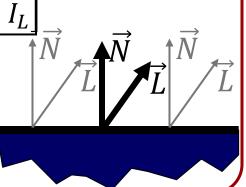
#### Take advantage of enatial cohorance

- If the normal is constant over the primitive, and
- If the light is directional,
- ⇒ The diffuse component is the same for all points on the primitive

	Surface Normal	Light Direction	View Direction
Emissive	-	-	-
Ambient	-	-	-
Diffuse	+	+	-
Specular	+	+	+

$$I = I_E + \sum_{L} \left[ K_A \cdot I_L^A + \left( K_D \left[ \langle \vec{N}, \vec{L} \rangle \right] + K_S \cdot \langle \vec{V}, \vec{R}(\vec{L}) \rangle^{K_R} \right) \cdot I_L \right]_{\uparrow \vec{N}}$$







#### Take advantage of chatial cohorance

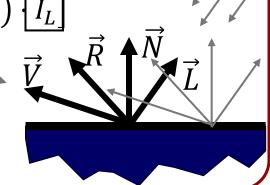
- If the normal is constant over the primitive, and
- If the light is directional,
- ⇒ The diffuse component is the same for all points on the primitive

Surface Normal	Light Direction	View Direction
----------------	-----------------	----------------

- Emissi
  - If the normal is constant over the primitive,
- Ambie If the light is directional, and
  - If the direction to the viewer is constant over the primitive
- Diffuse ⇒ The specular component is the same for all points on the primitive

Specular	+	+	+
----------	---	---	---

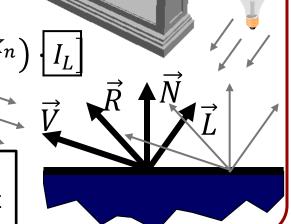
$$I = I_E + \sum_{L} \left[ K_A \cdot I_L^A + \left( K_D \cdot \langle \vec{N}, \vec{L} \rangle + K_S \cdot \left[ \langle \vec{V}, \vec{R}(\vec{L}) \rangle \right]^{K_n} \right) \cdot I_L \right]$$





- ⇒ Illuminates as though the lights are directional, the polygon is flat, and the camera uses parallel projection
  - $\circ \langle \vec{N}, \vec{L} \rangle$  constant over surface
  - $\circ \langle \vec{V}, \vec{R}(\vec{L}) \rangle$  constant over surface
  - $\circ$   $I_L$  constant over surface

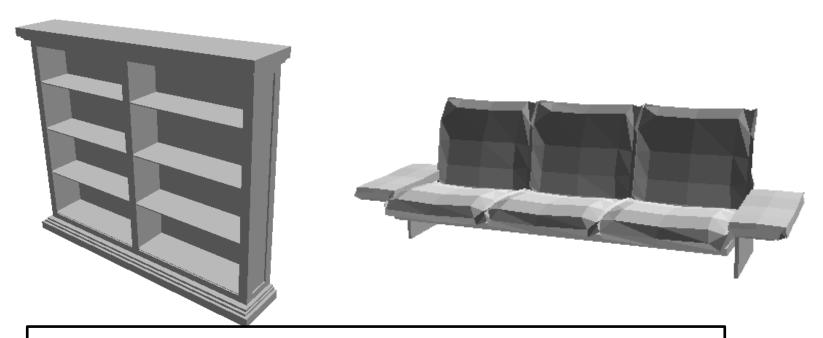
$$I = I_E + \sum_{l} \left[ K_A \cdot I_L^A + \left( K_D \left[ \langle \vec{N}, \vec{L} \rangle \right] + K_S \cdot \left[ \langle \vec{V}, \vec{R}(\vec{L}) \rangle \right]^{K_n} \right)$$





Objects look like they are composed of polygons

- OK for faceted objects
- Not so good for smooth surfaces



Although this is the "simplest" lighting model, it is tricky to implement this on the graphics card.

# **Polygon Shading Algorithms**

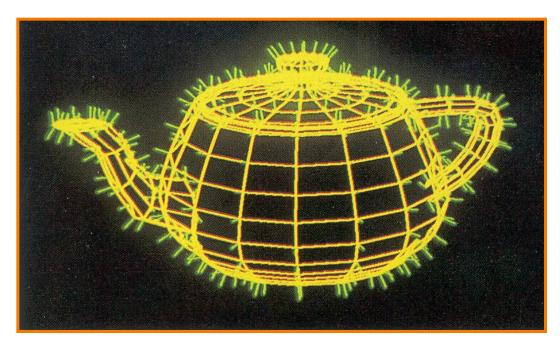


### Shading models:

- Flat
- Gouraud
- Phong



Represent a polygonal mesh with a normal at each vertex



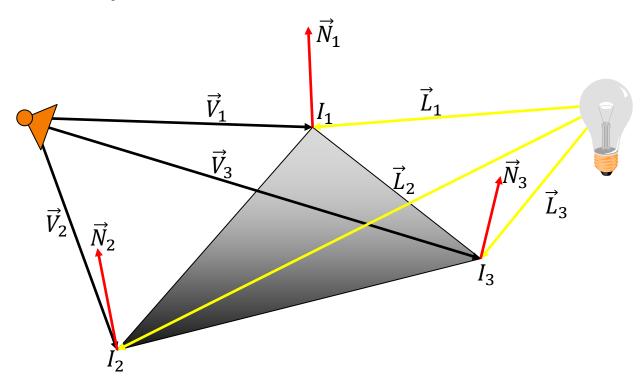
Watt Plate 7

$$I = I_E + \sum_{I} \left[ K_A \cdot I_L^A + \left( K_D \cdot \langle \vec{N}, \vec{L} \rangle + K_S \cdot \langle \vec{V}, \vec{R}(\vec{L}) \rangle^{K_n} \right) \cdot I_L \right]$$



### One lighting calculation per vertex

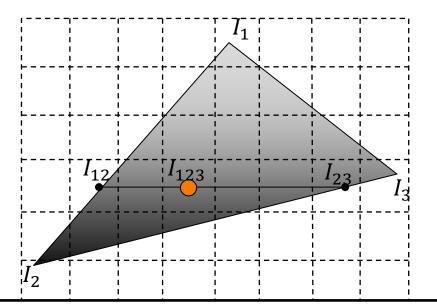
 Assign pixel colors inside polygon by interpolating colors computed at vertices





When rasterizing, linearly interpolate colors (first) across and (then) between edges:

$$(I_1, I_2, I_3) \rightarrow (I_{12}, I_{23}) \rightarrow I_{123}$$

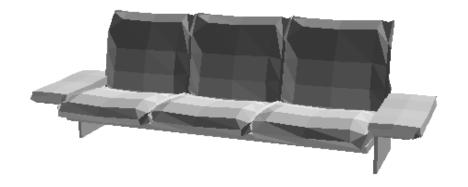


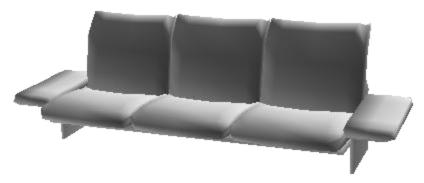
- $I_1$ ,  $I_2$ , and  $I_3$  are constant per triangle.
- $I_{12}$  and  $I_{23}$  (and  $I_{13}$ ) are constant per scan-line.
- $I_{123}$  varies across the scan-line



### Produces smoothly shaded polygonal mesh

Continuous shading over adjacent polygons





Flat Shading

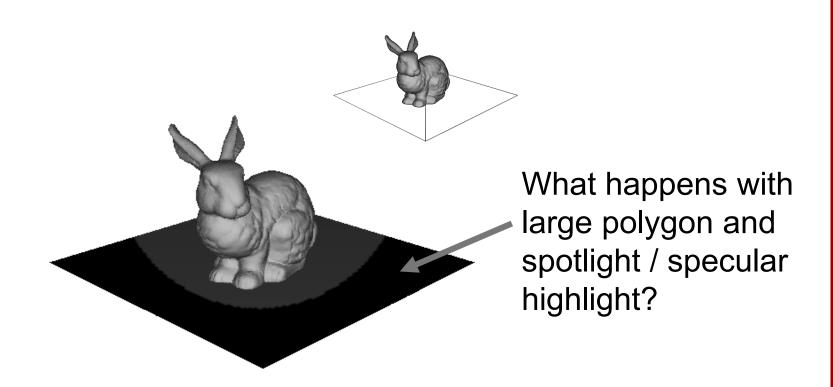
Gouraud Shading

This is the lighting model that was implemented on the graphics card as part of the fixed pipeline.



### Produces smoothly shaded polygonal mesh

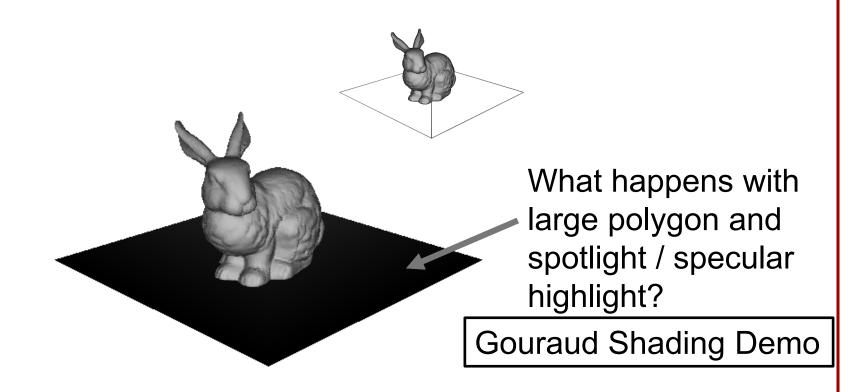
Continuous shading over adjacent polygons





### Produces smoothly shaded polygonal mesh

Continuous shading over adjacent polygons



# **Polygon Shading Algorithms**



### Shading models:

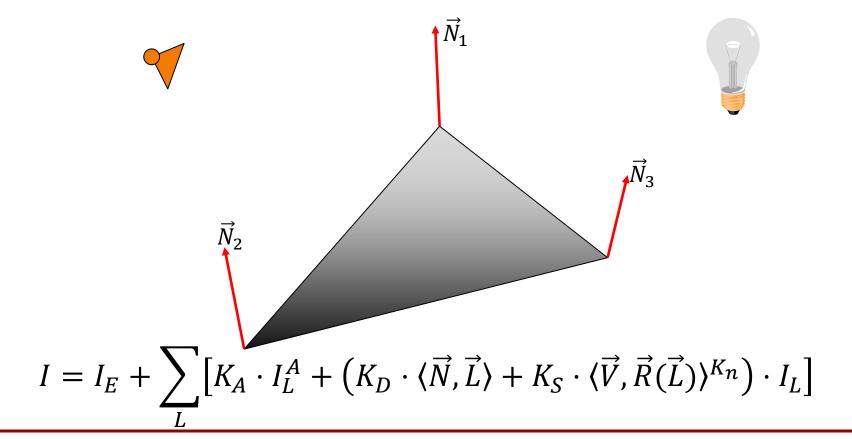
- Flat
- Gouraud
- Phong

# **Phong Shading**



### One lighting calculation per pixel/fragment

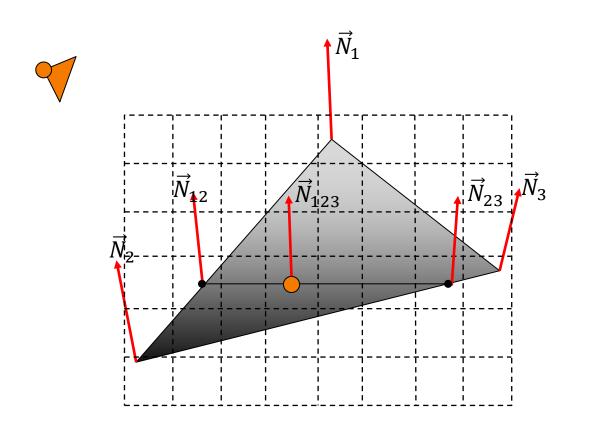
 Approximate surface normals for points inside polygons by linear interpolation of normals from vertices



### **Phong Shading**



When rasterizing, interpolate normals down and across scan lines

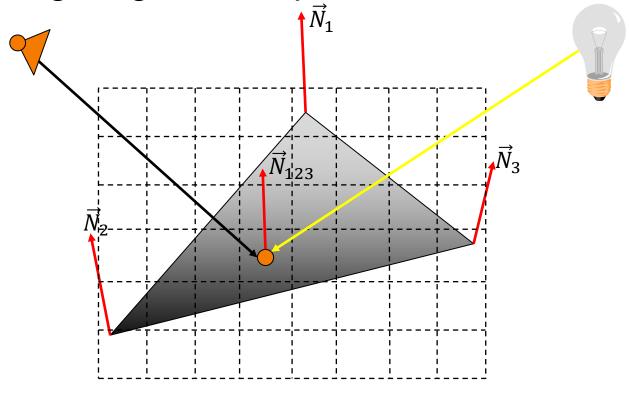


### **Phong Shading**



When rasterizing, interpolate normals down and across scan lines

Compute lighting at each pixel

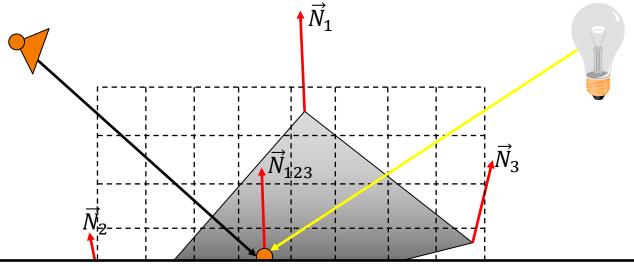


### **Phong Shading**



When rasterizing, interpolate normals down and across scan lines

Compute lighting at each pixel



Wasn't supported in early generation graphic cards. Can now be implemented in the GPU's <u>fragment shader</u>.

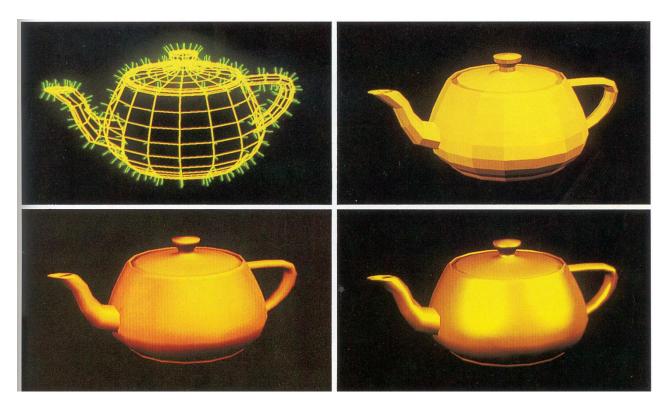
Phong Shading Demo

# **Polygon Shading Algorithms**



Wireframe

Flat

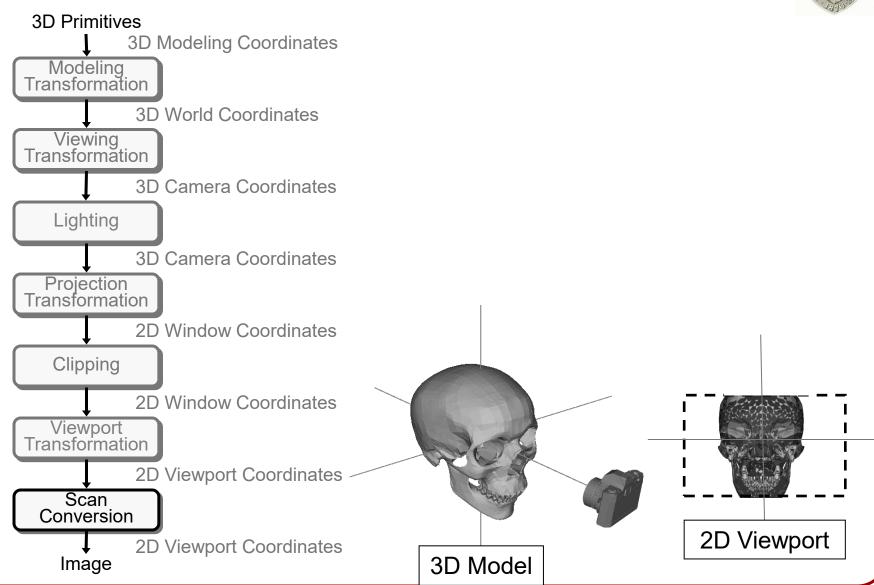


Gouraud

Phong

### 3D Rendering Pipeline (for direct illumination)





#### **Overview**



#### Scan conversion

Figure out which pixels to fill

#### Shading

Determine a color for each filled pixel

### Depth test

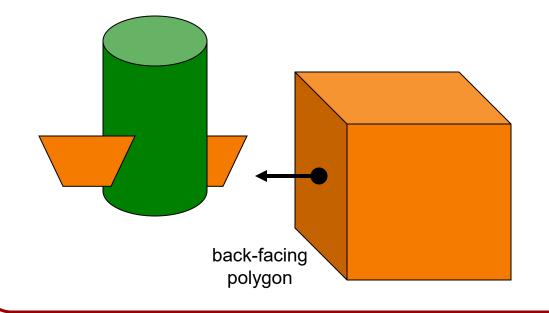
 Determine when the color of a pixel comes from the front-most primitive

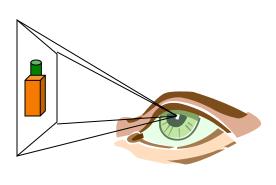
#### **Motivation**



In general, don't want to draw surfaces that are not visible:

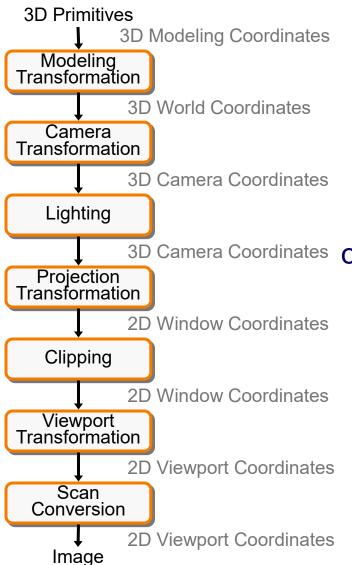
- Surfaces may be back-facing
- Surfaces may be covered in 3D
- Surfaces may be covered in the image plane





# 3D Rendering Pipeline





Somewhere, need to decide which objects are visible, and which are hidden (the sooner the better).

# Visibility algorithms



I. E. Sutherland, R. F. Sproull, and R. A. Schumacker

A Characterization of Ten Hidden-Surface Algorithms

ALGORITHMS										
		COMPARIS	SON ALGORITHMS	OBJECT SPACE	(partly each)	IMAGE SPACE	DEPTH PRIORIT	Y ALGORITHMS		
		edges edges		edges volumes	LIST PRIDRITY		area samplin	18	point sampling	
					ALGORITHMS /	•	1			
		/   \			priority	dynamicall, computed priority	\		/   \	
		Į.	•	•	•	priority	7		L	
	APPEL 1967	GALIMBERTI, et al 1969	LOUTREL 1967	ROBERTS 1963	SCHUMACKER, et al	NEWELL, et al	WARNOCK 1968	WATKINS	ROMNEY, et al	BOUKNIGHT
RESTRICTIONS	TP,NP	TP,NP	TP,NP	TP, CC, CF, NP	CF, NP, LS (TP)	None	(TR) None	1970 None	1967 TR,CF,NP	1969
COHERENCE	of a vertex to all	Promote visibility of a vertex to all edges at vertex	Promote visibility of a vertex to all edges at vertex		Frame coherence in depth No X coherence used	None used	Area coherence	Scanline X coherence	Scanline Depth Coherence	Scanline X Coherence
(1) What, what property (2) Method	Back Edge Cull  1) Edges separating back-facing planes 2) Dot product with normals & topology 3) Cull 4) List of edges, E 5) 1, E t	back-facing planes  2) Dot product with normals & topology	Back Edge Cull  1) Edges separating back-facing planes 2) bot product with normals & topology 3) Cull 4) List of edges, E, 5) 1, E,		Intra-Cluster Priority 1) Faces visibility 2) Dot product with normals 3) Exhaustive search 4) Ordered table 5) 0, (off-line)	Z Sort T) Faces, max Z 2) Comparison of max points 3) n logm 4) Ordered table 5) 1, F <sub>T</sub>	2) Comparison of max points 3) n log m	5) 1, E	Y Sort 1) Folygons, Y endpoints 2) Comparison 3) 2 bucket 4) Table of lists 5) 1, Fr	Y Sort 1) Edges, Min Y 2) Comparison 3) Bucket 4) Table of lists 5) 1, E <sub>r</sub>
(3) Type (4) Result structure (5) Kumber per frame, num- ber of ob- jects (merge) Number of new entries per frame, length of	Contour Edge Cull 1) Edges separating front \$\(^4\) back faces 2) Bot product with normals \$\(^4\) topology 3) Cull 4) List, E <sub>C</sub> 5) 1, E <sub>C</sub>	(Omatted)	(Omitted)	Clipping Cull 1) Intersect edge with visible volume 2) 3) Cull 4) E 5) 1, E 5	Inter-Cluster Priority 1) Clusters 2) Not product with separating planes 3) Prefix scens binary tree 4) ordered table 5) 1, Ct	Newell Special 1) Faces, pairwise visibility 2) Depth, bounding boxes, separation 3) Bubble, splittin 4) Ordered table 5) 1.F <sub>T</sub> *split faces	Warnock Special  1) Faces with Windox  2) Depth, mini-max  in X and Y, sum of langles  3) Radix 4 subdivi- sion With overlap  4) Stacks of unordered tables  5) L, F, factor 1	2) Comparison 3) Merge (ordred 4) 2-way linked	5) n. S <sub>2</sub>	X Merge 1) Edges, X value 2) Comparison 3) Merge (ordered) 4) Linked list 5) E <sub>r</sub> , 2S <sub>g</sub> (edges)
	against all faces 2) Depth, Surroundedness 3) Exhaustive search 4) Quantitative visibility of vertex	Initial Visibility. 1) Ray to vertex against all faces 2) Depth, surroundedness 3) Exhaustive search 4) Quantitative visibility of vertex 5) #objects, Fr	against all faces 2) Betweenness, surroundedness 3) Exhaustive search 4) Quantitative	1) Edges, visibilit relative to volumes 2) Linear Programming 3) Mini-max sort	Back-Face Cull yl) Faces 2) Dot product with face normal 3) Cull 4) Smaller ordered table 5) 1, Ft	Y Sort 1) Face segment by Y range 2) Y intercept 3) Bucket 4) None 5) Fr + split faces Hf	Depth Search 1) Surrounder faces 2) 4-corner compare 3) Exhaustive 4) Answer/failure 5) L <sub>v</sub> , F <sub>r</sub> /factor 2	2) Comparison 3) Bubble 4) 2-way linked	X Priority Search 1) Edges, X value 2) Comparison 3) Priority search 4) Active segment list 5) n, m	1) Edges, X value 2) Comparison 3) Bubble 4) 1-way linked list 5) N, 25 <sub>g</sub> (edges)
Number of searches, length of last	with all be	Edge Intersection 1) Intersect one Eswith all Egy Intersect in picture plane, depth 3) Cull (unordered) 4) Intersection list 5) Eg, Eg - 1	Edge Intersection 1) Intersect one Es with all E 2) Intersect in picture plane, depth 5) Cull (unordered) 4) Intersection list 5) E <sub>S</sub> , E <sub>S</sub> - 1		Y Cull 1) Faces by Y extent 2) Mini-max on X intercepts 3) Cull (unordered) 4) X intercepts of relevant segments 5) n, E <sub>5</sub>	X Merge 1) Segments, X intercept 2) Comparison 3) Ordered merge 4) Ordered 11st 5) Sr, Sy/2	needed	<ol> <li>Double comparison</li> <li>Cull ordered list</li> </ol>	2) Linear equations and comparison 3) Search (unordered 4) Visible segment 5) n*2S <sub>1</sub> ,0 <sub>C</sub>	Z Search 1) Segments, depth 2) Linear equations and comparison 3) Search of un- ordered active list 4) Visible segment 5) n*2S <sub>g</sub> , D <sub>c</sub>
4	Sort Along Edge 1) Intersections on edge, ordering 2) Comparison 3) Bubble 4) Answer 5) E, , X/E, Gmat if well hidden)	Sort Along Edge 1) Intersections on edge, ordering 2) 3) 4) Answer 5) E <sub>5</sub> , X <sub>V</sub> /E <sub>5</sub> (must be done)	Sort Along Edge 1) Intersections on edge, ordering 2) 3) 4) Answer 5) E <sub>5</sub> , X <sub>V</sub> /E <sub>5</sub> (Omit if well hidden		X Sort 1) Segments 2) Counters 3) Hardware 4) Segments at this X 5) nm, Sg			Z Search 1) Segments, Z 2) Depth by logarithmic search 3) Search (unordered 4) Visible segment 5) n*S <sub>v</sub> *f(>1), D <sub>c</sub>	(Omitted if X priorities same as last time)	in the second
					Priority Search 1) Segments, priorit 2) Logic network 3) Logic network 4) Wisible segment 5) nm, S,					

Figure 29. Characterization of ten opaque-object algorithms b. Comparison of the algorithms.

[Sutherland '74]

### Hidden Surface Removal (HSR)



#### Algorithms for HSR

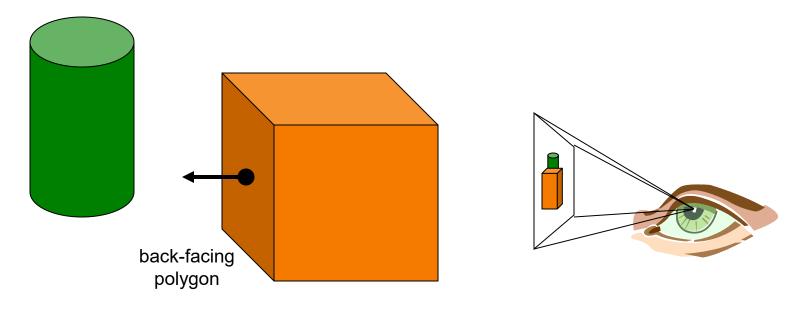
- Back-face detection
- View-frustrum culling
- ∘ *z*-buffer

### **Back-face detection**



Q: How do we test for back-facing polygons?

A: Dot product of the normal and view directions.



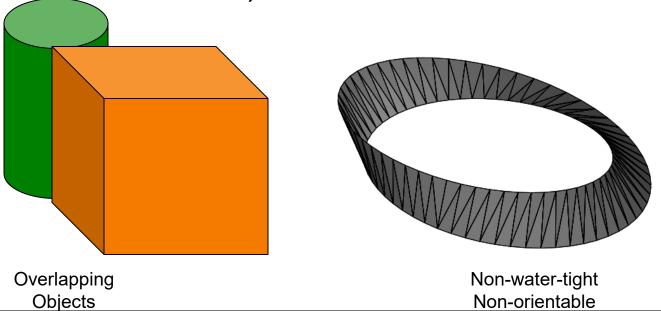
If  $\langle \vec{V}, \vec{N} \rangle > 0$ , then polygon is back-facing

### **Back-face detection**



#### This method:

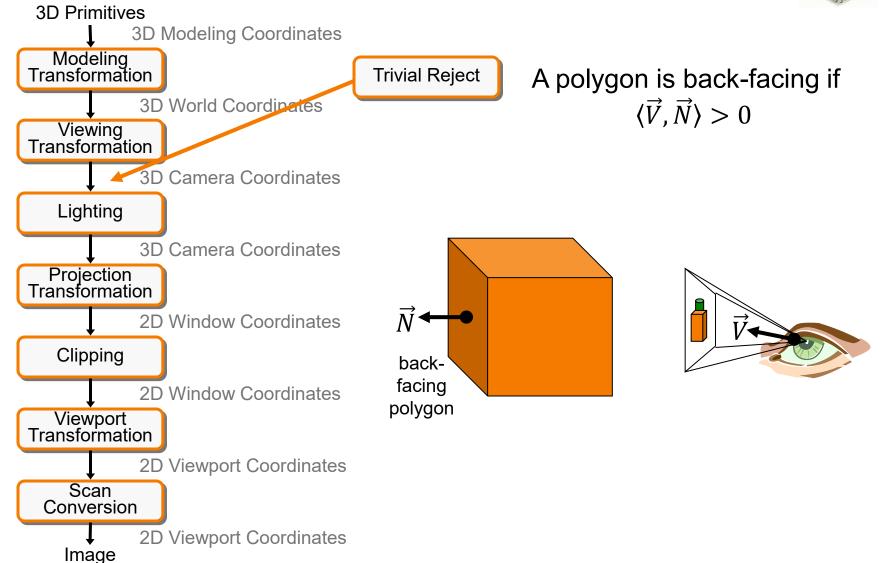
- Does not eliminate shapes overlapping in 3D or 2D
- Requires surface to be water-tight and orientable (not all surfaces are)



In general, back-face expected to remove ≈ half of polygon surfaces from removal further visibility tests

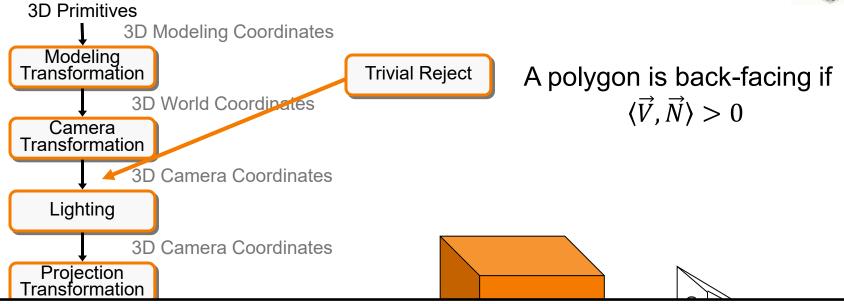
### 3D Rendering Pipeline





# 3D Rendering Pipeline





Note: When your graphics card does this, it does <u>not</u> use the rendering normals (used for lighting).

It uses the geometric normal – the cross-product of the triangle edges.

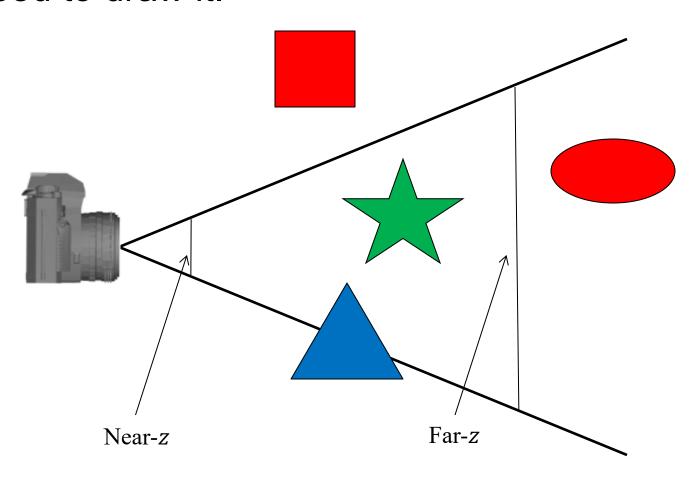
⇒ Make sure that the ordering of the vertices is consistent.

By default, triangles/polygons are back-facing if the vertices are in clockwise order when viewed from the camera.

### View-frustrum culling

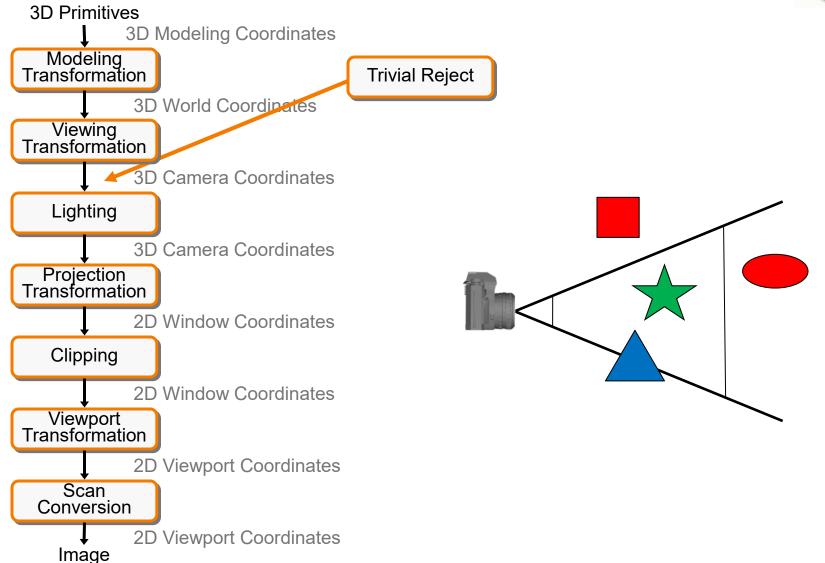


If the shape is outside the viewing volume, we don't need to draw it.



# View-frustrum culling

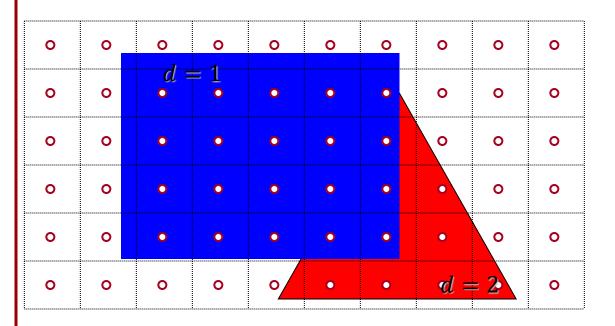






#### Store color & depth of closest object at each pixel

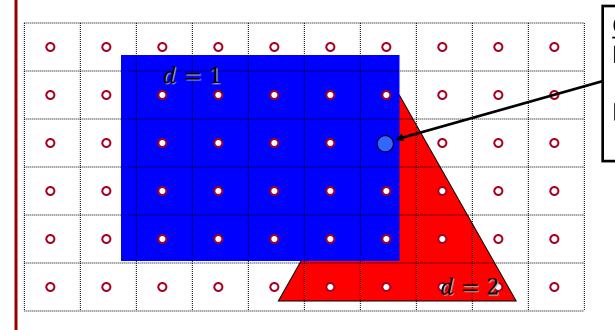
- $\circ$  Initialize depth of each pixel in the z-buffer to  $\infty$
- Only update pixels from a primitive when the depth is closer what's stored in the z-buffer





#### Store color & depth of closest object at each pixel

- $\circ$  Initialize depth of each pixel in the z-buffer to  $\infty$
- Only update pixels from a primitive when the depth is closer what's stored in the z-buffer



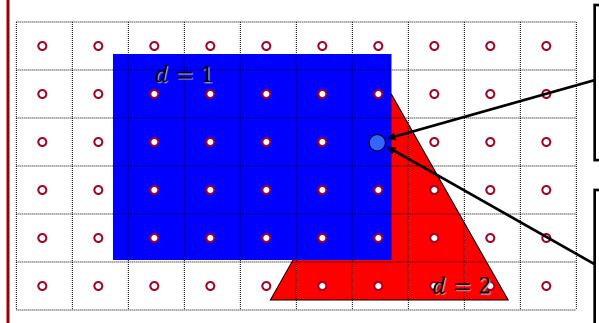
Case 1 (Blue before Red): Blue  $\rightarrow$  (d = 1) < ( $d = \infty$ ): Set RGB = (0,0,1), d = 1Red  $\rightarrow$  (d = 2) > (d = 1):

Don't change pixel



#### Store color & depth of closest object at each pixel

- Initialize depth of each pixel in the z-buffer to  $\infty$
- Only update pixels from a primitive when the depth is closer what's stored in the z-buffer



#### Case 1 (Blue before Red):

Blue 
$$\rightarrow$$
  $(d = 1) < (d = \infty)$ :  
Set  $RGB = (0,0,1), d = 1$   
Red  $\rightarrow$   $(d = 2) > (d = 1)$ :  
Don't change pixel

#### Case 2 (Red before Blue):

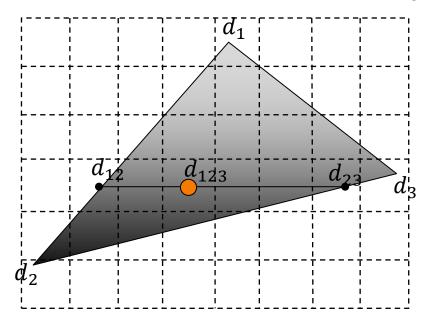
Red 
$$\rightarrow$$
  $(d = 2) < (d = \infty)$ :  
Set  $RGB = (1,0,0), d = 2$   
Blue  $\rightarrow$   $(d = 1) < (d = 2)$ :

Blue 
$$\rightarrow$$
  $(d = 1) < (d = 2)$ :  
Set  $RGB = (0,0,1), d = 1$ 



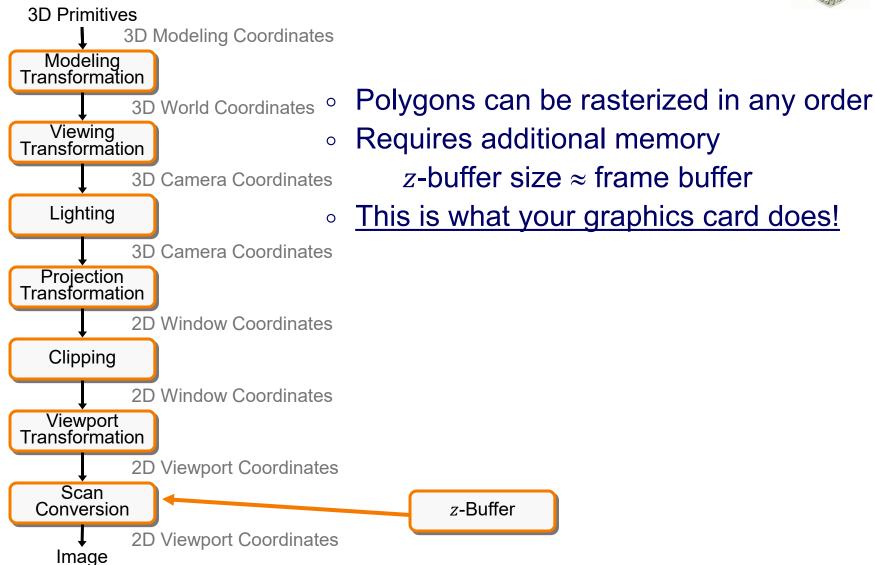
#### Store color & depth of closest object at each pixel

- $\circ$  Initialize depth of each pixel in the z-buffer to  $\infty$
- Only update pixels from a primitive when the depth is closer what's stored in the z-buffer
- Depths are interpolated from vertices, just like colors



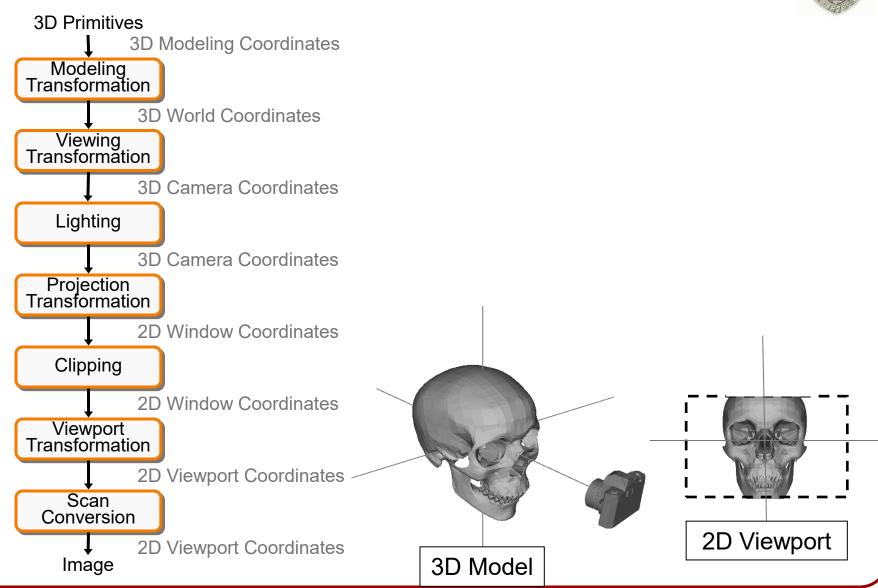
### 3D Rendering Pipeline





### 3D Rendering Pipeline (for direct illumination)





### **Scan Conversion**

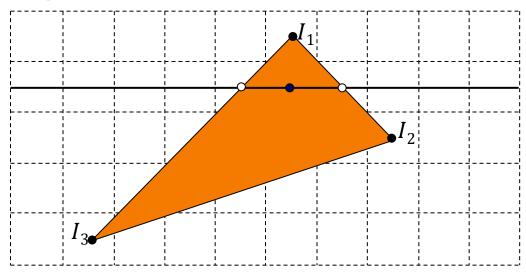


How do we average information (e.g. color, normal, depth) from the three vertices of a triangle?

- Interpolate using screen space (2D) weights
- Interpolate using world space (3D) weights

It's easier to do the interpolation in 2D.

Is there a difference?



### **Scan Conversion**



Projective transformations (recall)

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ m & n & o & p \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

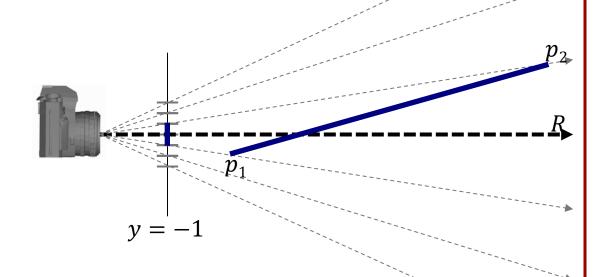
#### Properties of projective transformations:

- Origin does not necessarily map to origin
- Lines map to lines
- (Weighted) average is not necessarily preserved
- Parallel lines do not necessarily remain parallel
- Closed under composition



A line segment in 2D projected onto a 1D window.

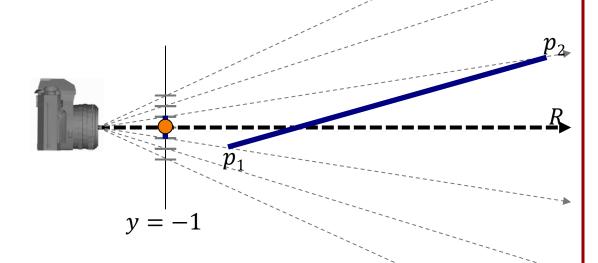
How to interpolate the information from vertices  $p_1$  and  $p_2$  at the pixel corresponding to ray R?





A line segment in 2D projected onto a 1D window.

- 1. [Projected] The ray intersects the window directly between the projections of  $p_1$  and  $p_2$ :
  - $\Rightarrow$  Use equal contributions from  $p_1$  and  $p_2$ .





A line segment in 2D projected onto a 1D window.

- 1. [Projected] The ray intersects the window directly between the projections of  $p_1$  and  $p_2$ :
  - $\Rightarrow$  Use equal contributions from  $p_1$  and  $p_2$ .
- 2. [Unprojected] The ray intersects the 2D line segment closer to  $p_1$ :
  - $\Rightarrow$  Use more information from  $p_1$  than from  $p_2$ .

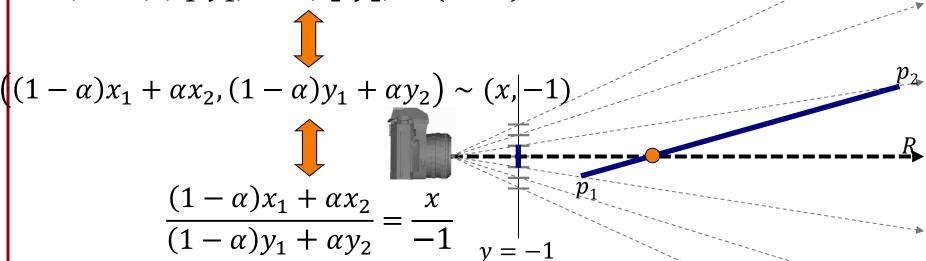




Q: How do we interpolate correctly at (x, -1)?

If  $p_1 = (x_1, y_1)$  and  $p_2 = (x_2, y_2)$ , to find the blending value  $\alpha$  for a pixel falling at position x in the screen we need to solve:

$$(1 - \alpha)(x_1, y_1) + \alpha(x_2, y_2) \sim (x, -1)$$





Q: How do we interpolate correctly at (x, -1)?

If  $p_1 = (x_1, y_1)$  and  $p_2 = (x_2, y_2)$ , to find the blending value  $\alpha$ for a pixel falling at position x in the screen we need to solve:\*

$$(1-\alpha)$$

$$(1-\alpha)x_1$$

 $(1-\alpha]$  To compute the interpolation weights, perform a perspective divide:

$$\frac{(1-\alpha)x_1 + \alpha x_2}{(1-\alpha)y_1 + \alpha y_2} = \frac{x}{-1}$$

This is different than solving for the blending value in the image plane:

$$(1 - \alpha)\frac{x_1}{y_1} + \alpha \frac{x_2}{y_2} = \frac{x}{-1}$$