600.469 / 600.669 Approximation Algorithms

Topic: Topic **Date:** 1/27/15

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1.1 The Topic

Citing a reference [CW87].

A description list.

Part a: The first part.

Part b: The second part.

Part c: The last part.

An itemized list.

- Item #1.
- Item #2.

A numbered list.

- 1. First
- 2. Second

1.1.1 Statements of Results

Definition 1.1.1 Define your problem here.

Theorem 1.1.2 A theorem.

Lemma 1.1.3 A helpful lemma.

Proof: Proof of the lemma goes here.

Now we can prove Theorem 1.1.2.

Proof of Theorem 1.1.2: Follows from Lemma 1.1.3

1.2 Some Formulas and Algorithms

1.2.1 A Linear Program

Consider linear program (TSP-LP) below.

minimize:
$$\sum_{e} c(e) \cdot x_e$$
 (TSP-LP)

subject to:
$$x(\delta(S)) \ge 2$$
 for each cut $\emptyset \subsetneq S \subsetneq V$ (1.2.1)

$$x(\delta(v)) = 2$$
 for each vertex $v \in V$ (1.2.2)
 $x \ge 0$

Constraints (1.2.1) are the *cut constraints* and Constraints (1.2.2) are the *degree constraints*.

1.2.2 Tips

Use $\log n$, not $\log n$.

$$V = \{v_1, v_2, \dots, v_n\}.$$

Check out
$$\sum_{i=1}^{n} i$$
 vs. $\sum_{i=1}^{n} i$.

A displayed equation:

$$H_n = \sum_{k=1}^n \frac{1}{k} = \int_1^n \frac{dx}{x} + O(1) = \ln n + O(1)$$

A matrix:

$$\left(\begin{array}{cccc}
x_1 & y_1 & z_1 \\
x_2 & y_2 & z_2 \\
0 & 0 & 1
\end{array}\right)$$

Problem names should look like this: Set Cover.

1.2.3 An Algorithm

Algorithm 1 Kruskal's Minimum Spanning Tree Algorithm

Input: Undirected graph G = (V, E) with edge costs $c(e) \ge 0, e \in E$.

Output: A minimum spanning tree of G.

$$T \leftarrow \emptyset$$
 for each edge $e \in \mathcal{F}$

for each edge $e \in E$ in increasing order of cost c(e) do

if $T \cup \{e\}$ does not contain a cycle then

$$T \leftarrow T \cup \{e\}$$

end if

end for

return T

References

- CW87 D. COPPERSMITH and S. WINOGRAD, Matrix multiplication via arithmetic progressions, *Proceedings of the 19th ACM Symposium on Theory of Computing*, 1987, pp. 1–6.
 - S69 V. Strassen, Gaussian Elimination Is Not Optimal, *Numerische Mathematik* 13, 1969, pp. 354–356.
 - P84 V. Pan, *How To Multiply Matrices Faster*, Springer-Verlag, Lecture Notes in Computer Science Vol. 179, 1984.