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# Efficient NORMAL-FORM Parsing

for Combinatory Categorical Grammar

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# CCG and the Spurious Ambiguity Problem

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[John likes Mary]	S (sentence)
John [likes Mary]	S\NP (sentence missing NP to its left – "\")
[John likes] Mary	S/NP (sentence missing NP to its right – "/")



**... can conjoin this with other predicates**

*[John likes], and [Sue hates], that woman in the hat*

**... can ask who satisfies it**

*Who does [John like]?*

**... can state who satisfies it**

*It is MARY that [John likes]. / [John likes] MARY.*

**CCG allows linguistically useful extra constituents ...**

# CCG and the Spurious Ambiguity Problem

Two parses for an unambiguous sentence:

[[John likes] Mary] (non-standard parse)

[John [likes Mary]] (standard parse)

**the [aide in the] Senate [that D'Amato says Clinton tried to] bribe**

**... but CCG forces hundreds of extra parses on us.**

# Today's Talk

- **Sketch of CCG formalism**
  - + the B combinators
- **A solution to spurious ambiguity**
- **Why the solution works (formal intuitions)**
- **Important extensions of the solution**
  - + the S combinator (straightforward)
  - + the T combinator (work in progress)
  - + restrictions on the rules

**forward rules**

$\text{>B0: } A/B \ B \ \longrightarrow \ A$   
 $\text{>B1: } A/B \ B/C \ \longrightarrow \ A/C$   
 $\quad \quad A/B \ B\backslash C \ \longrightarrow \ A\backslash C$   
 $\text{>B2: } A/B \ B/C/D \ \longrightarrow \ A/C/D$   
 $\quad \quad A/B \ B/C\backslash D \ \longrightarrow \ A/C\backslash D$   
 $\quad \quad A/B \ B\backslash C/D \ \longrightarrow \ A\backslash C/D$   
 $\quad \quad A/B \ B\backslash C\backslash D \ \longrightarrow \ A\backslash C\backslash D$

*etc.***backward rules**

$\text{<B0: } \quad \quad B \ A\backslash B \ \longrightarrow \ A$   
 $\text{<B1: } \quad \quad B\backslash C \ A\backslash B \ \longrightarrow \ A\backslash C$   
 $\quad \quad B/C \ A\backslash B \ \longrightarrow \ A/C$   
 $\text{<B2: } \quad \quad B\backslash C\backslash D \ A\backslash B \ \longrightarrow \ A\backslash C\backslash D$   
 $\quad \quad B\backslash C/D \ A\backslash B \ \longrightarrow \ A\backslash C/D$   
 $\quad \quad B/C\backslash D \ A\backslash B \ \longrightarrow \ A/C\backslash D$   
 $\quad \quad B/C/D \ A\backslash B \ \longrightarrow \ A/C/D$

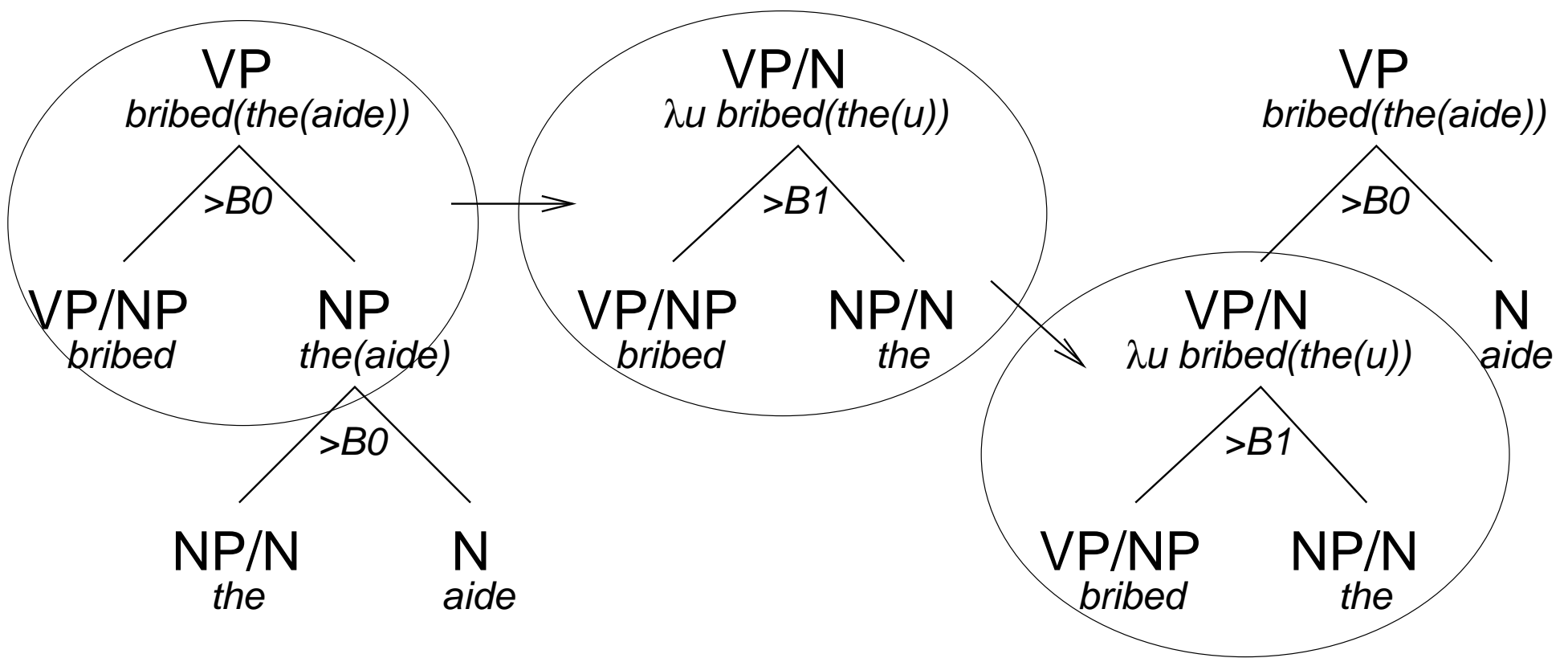
*etc.*

# Sketch of CCG Formalism:

# Example

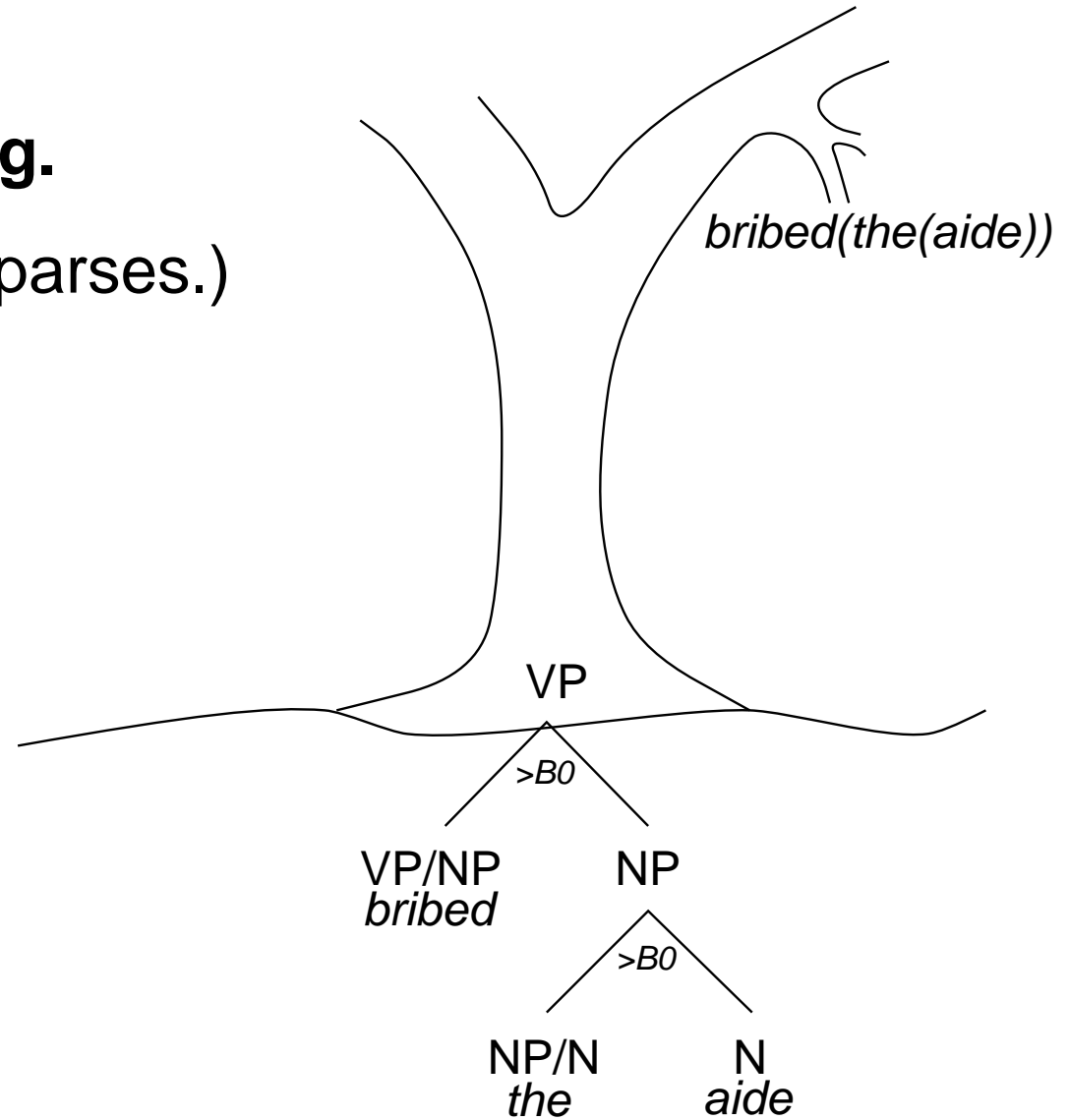
$\text{>B0: } \begin{matrix} A/B & B \\ f & x \end{matrix} \Rightarrow \begin{matrix} A \\ f(x) \end{matrix}$

$\text{>B1: } \begin{matrix} A/B & B/C \\ f & g \end{matrix} \Rightarrow \begin{matrix} A/C \\ \lambda u f(g(u)) \end{matrix}$



**Exactly one parse per reading.**

(Efficiently suppress all other parses.)



How can we rule out extra parses?

Yes, allow all of CCG's non-standard constituents,

both when useful

*[D'Amato said Clinton tried],*

*and [maybe he said she failed], to bribe that aide.*

and when useless.

*[D'Amato said Clinton tried] to bribe that aide.*

**BUT:**

1 parse not 5

1 parse not 5

**[ [D'Amato said Clinton tried] [to bribe that aide] ]**

assemble 1 parse not 25

and in this case, disallow even that 1 parse!

(but do allow: [ [D'Amato] [said Clinton tried to bribe that aide] ] )



**Standard kind of spurious ambiguity:**

**Forward (or backward) "chains"**

**VP/NP NP/N N**

*2 parses*

**A/A A/B B\C/D/E E/F F\G**

*14 parses*

**The OUTPUT of forward composition**

**(>B1, >B2, >B3, ...)**

**may not be the primary (left) INPUT to any forward rule.**

**(>B0, >B1, >B2, >B3 ...)**

**The OUTPUT of backward composition**

**(>B1, >B2, >B3, ...)**

**may not be the primary (right) INPUT to any backward rule.**

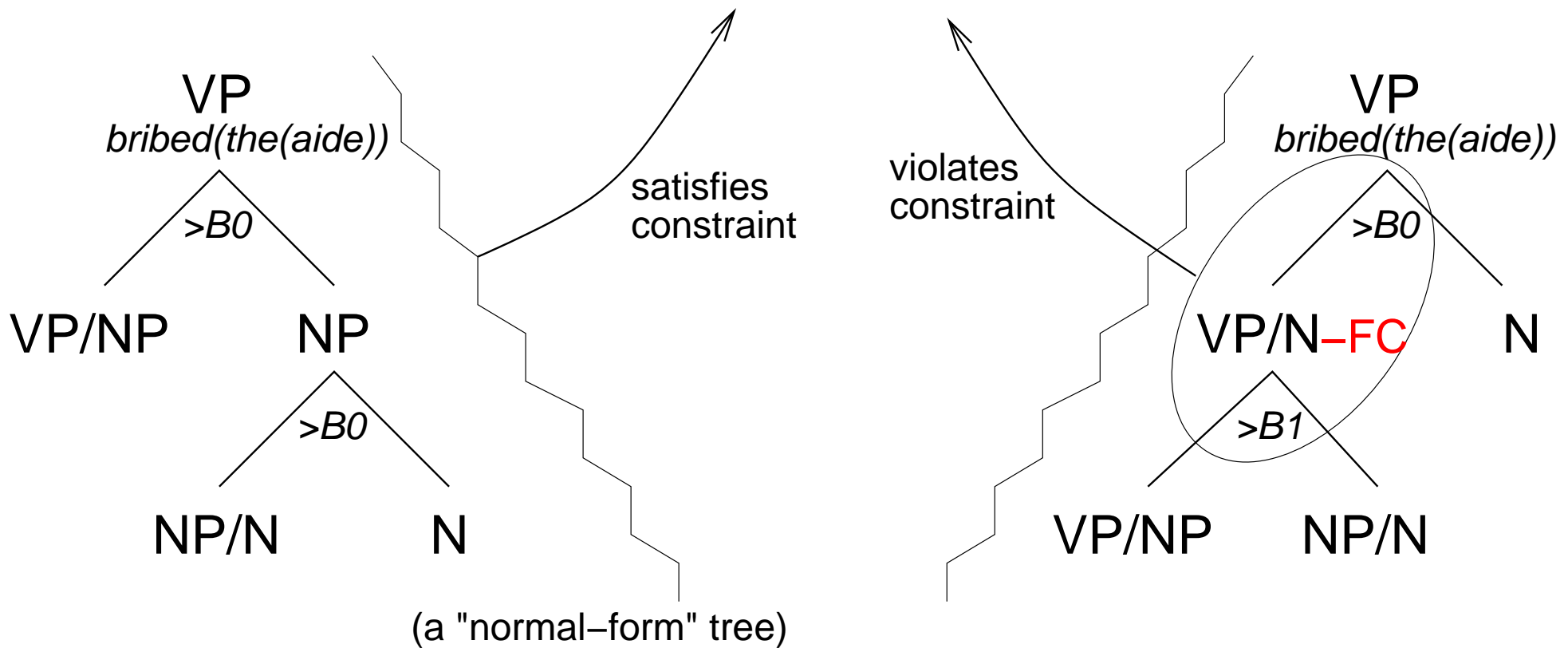
**(>B0, >B1, >B2, >B3 ...)**

The **OUTPUT** of forward composition

(>B1, >B2, >B3, ...)

may not be the primary (left) **INPUT** to any forward rule.

(>B0, >B1, >B2, >B3 ...)



For CCG with the generalized composition rules (including mixed),  
these tactics

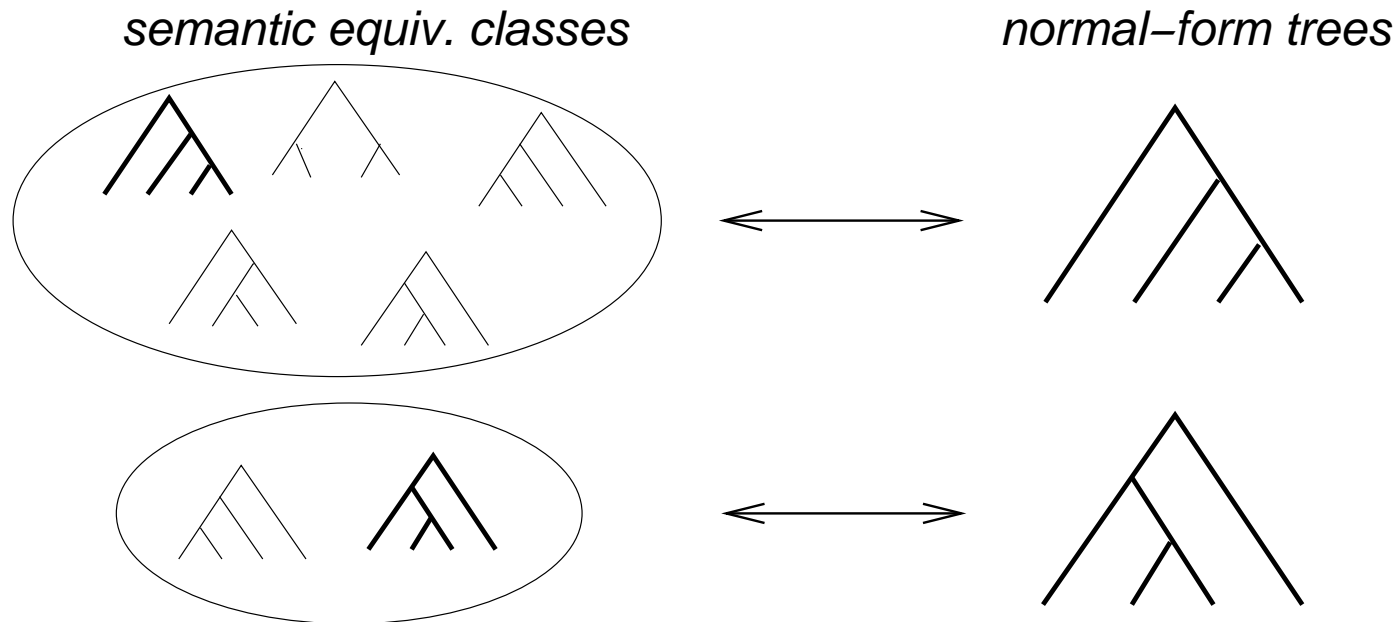
(1) eliminate **ONLY** spurious ambiguity

(safety)

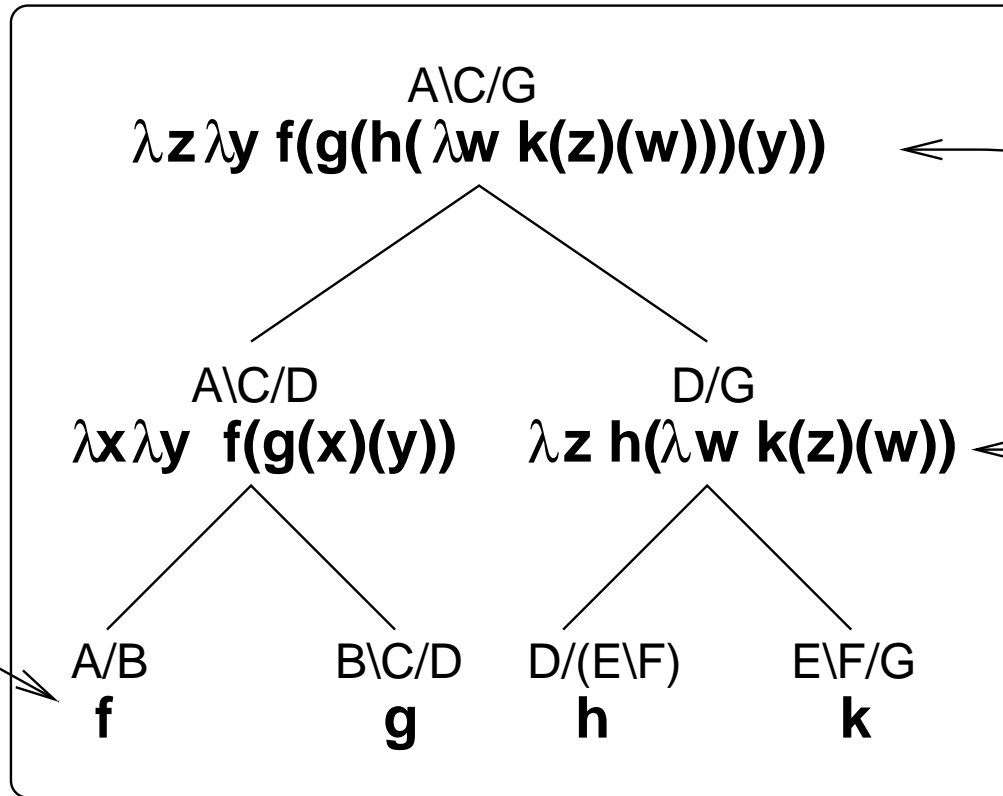
(2) eliminate **ALL** spurious ambiguity

(completeness)

1-1 correspondence:



# Formal Intuitions: What is Spurious Ambiguity?



A syntax tree takes interps of the words,

and combines them semantically into an interp. of the phrase.

**So a syntax tree on n words**

**computes an n-ary function:**  $\lambda f \lambda g \lambda h \lambda k (\lambda z \lambda y f(g(h(\lambda w k(z)(w)))(y)))$

**Two trees on the same n words are semantically equivalent**

**iff they compute the same n-ary semantic function.**

# Formal Intuitions: What is Spurious Ambiguity?

Two trees on the same  $n$  words are semantically equivalent iff they compute the same  $n$ -ary semantic function.

What this definition is NOT:

(1) Does this mean "iff they compute the same lambda-term"?

(2) Do we eliminate one parse from each of these pairs?

[quietly [knock twice]]

[[quietly knock] twice]

denote  
same action

[ $\pi$  equals [[2 plus 3] over 4]]

[ $\pi$  equals [2 plus [3 over 4]]]

denote same  
truth value ("false")

## Formal Intuitions: Existence Theorem

*Theorem.* For every tree  $T$  we cut down with our constraints, we leave standing a semantically equivalent tree,  $NF(T)$ .

*Proof.* To construct  $NF(T)$  from  $T$ , essentially



Construction used is inductive.

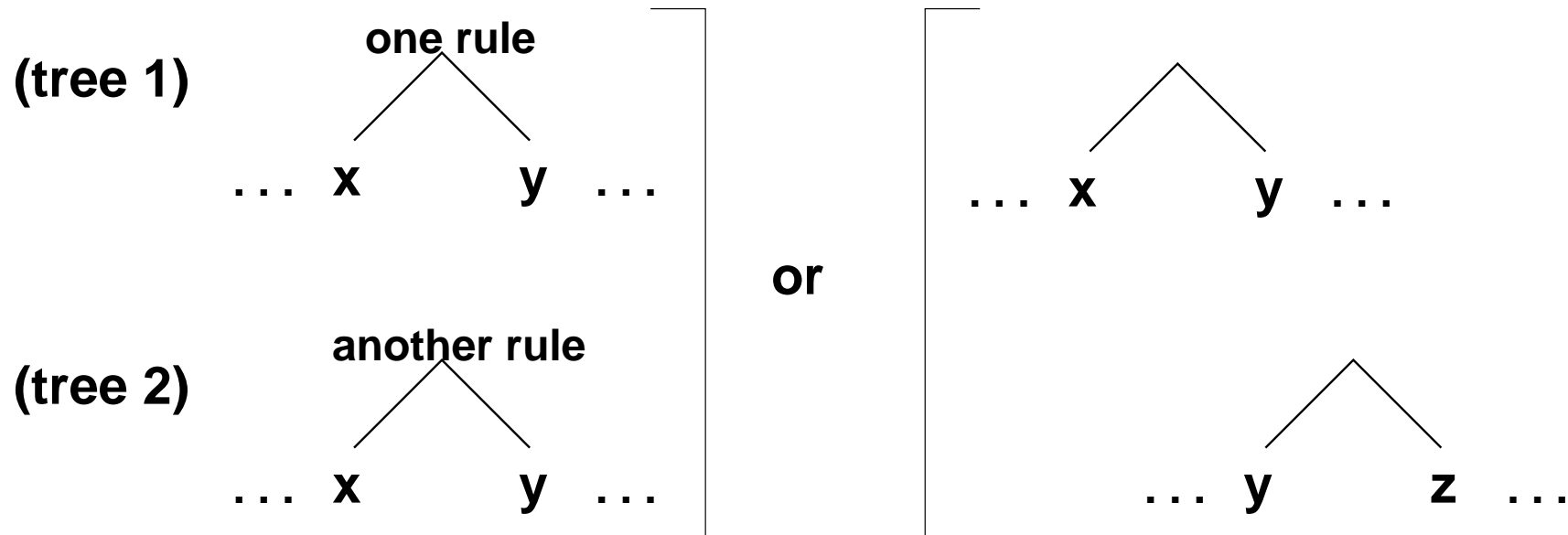
Takes  $O(1)$  time, if  $NF(T')$  is known for  $T'$  smaller than  $T$ .

# Formal Intuitions: Uniqueness Theorem

*Theorem.* We never leave two equivalent trees standing.

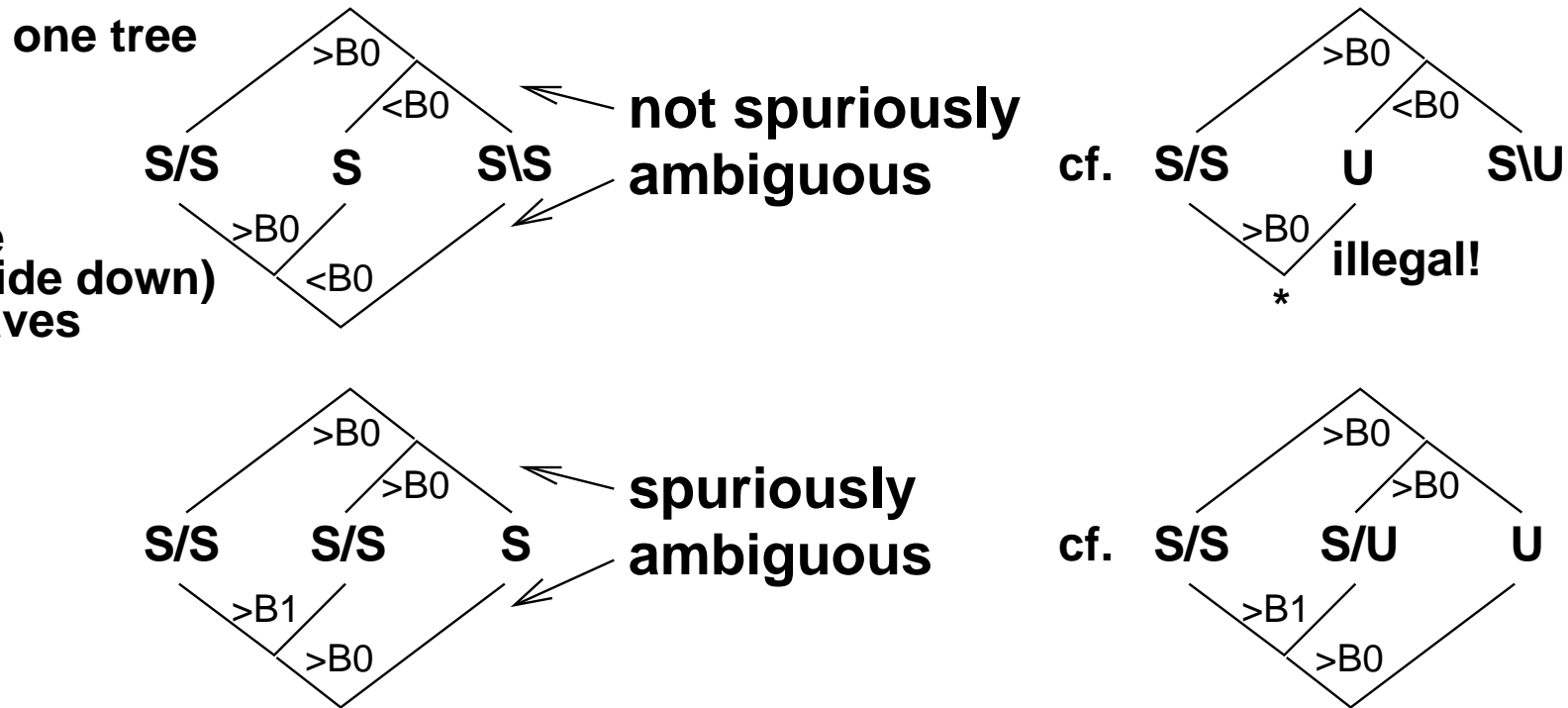
*Proof.* Given two distinct trees that we keep.  
They must differ somewhere syntactically:

so contain either



Show that they differ semantically as a result.

# Formal Intuitions: The Spurious Ambiguity Lemma



2 parses on the same sequence of words are spuriously ambiguous ...

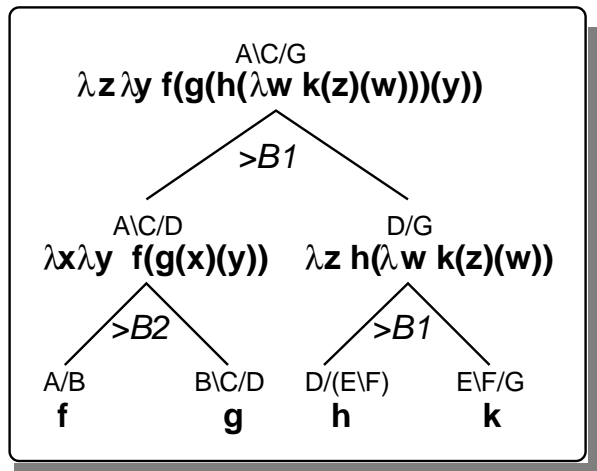
*Def.* ... iff **spuriousity is robust under changes to words' semantics.**

*Equiv def.* ... iff **ambiguity is robust under changes to words' syntax.**

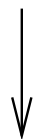
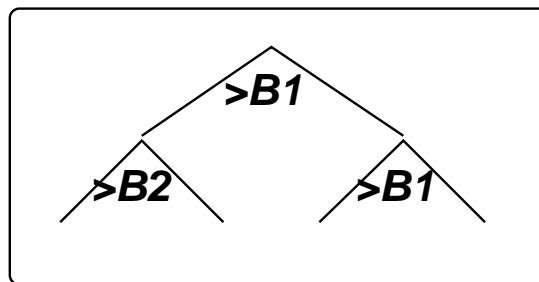
**Easy syntactic characterization of a semantic property!**



# Formal Intuitions: Proof of Spurious Ambig. Lemma



no-category syntax tree



restricted combinator

$\lambda f \lambda g \lambda h \lambda k ( \lambda z \lambda y f(g(h( \lambda w k(z)(w)))(y)))$

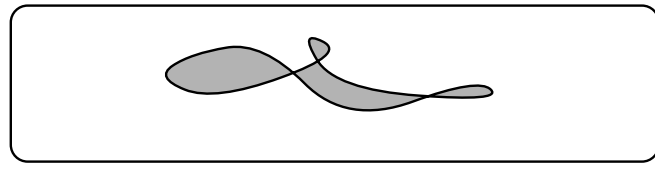
*injective*

*injective*

most general polymorphic type

n-ary function in model

$(B \rightarrow A) \rightarrow (D \rightarrow C \rightarrow B) \rightarrow (X \rightarrow D) \rightarrow (G \rightarrow X) \rightarrow (G \rightarrow C \rightarrow A)$   
 can write as  $(A|C|G) | (X|G) | (D|X) | (B|C|D) | (A|B)$



## Extensions: The S and T combinators

If we add the S (substitution) combinator, we need a new restriction:

Just as

The OUTPUT of ( $>B_1, >B_2, >B_3, \dots$ )  
may not be the primary (left) INPUT to ( $>B_0, >B_1, >B_2, >B_3, \dots$ )

now

The OUTPUT of ( $>B_2, >B_3, \dots$ )  
may not be the primary (left) INPUT to  $>S$

If we add the T (type-raising) combinator,

the ambiguities get much trickier! Work in progress.

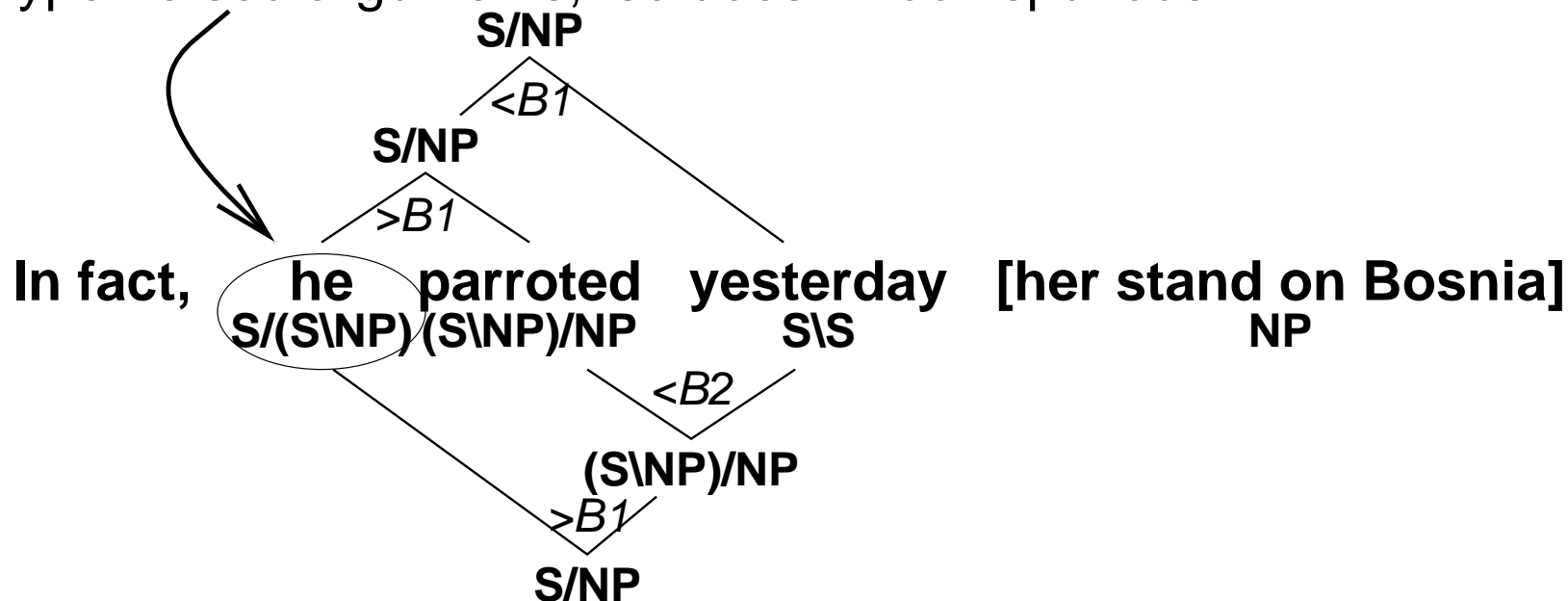
## Extensions: Making TR visible to the grammar

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If type-raising is only lexical,  
our definition can't see this ambiguity:

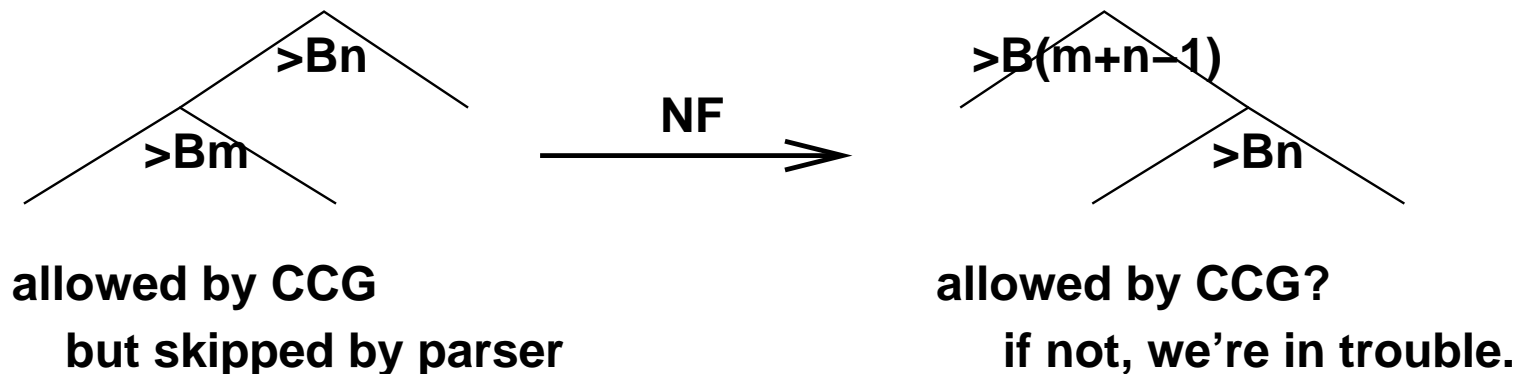
**John**   **likes**   **Mary**                      **John**   **likes**   **Mary**  
NP   (S\NP)/NP   NP                              S/(S\NP) (S\NP)/NP   NP  
*parses of different sentences!*

and the ambiguity below depends on funny "lexical" properties  
of type-raised arguments, so doesn't look spurious:



## Extensions: Restrictions on CCG rules

In practice, a CCG grammar may state WHICH rules can apply, & WHEN.



### Solution:

**Don't change the theorems, change the parser!**

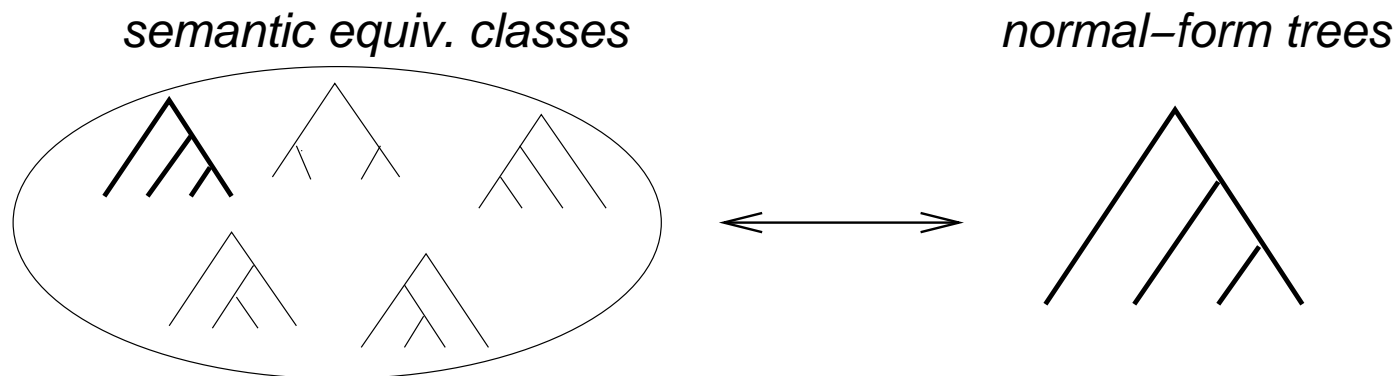
*Karttunen 1986:* **No constraints on parses. Whenever we find a new parse of a constituent, check that it's not redundant.**

**But checking new parse against old parses takes exponential time.**

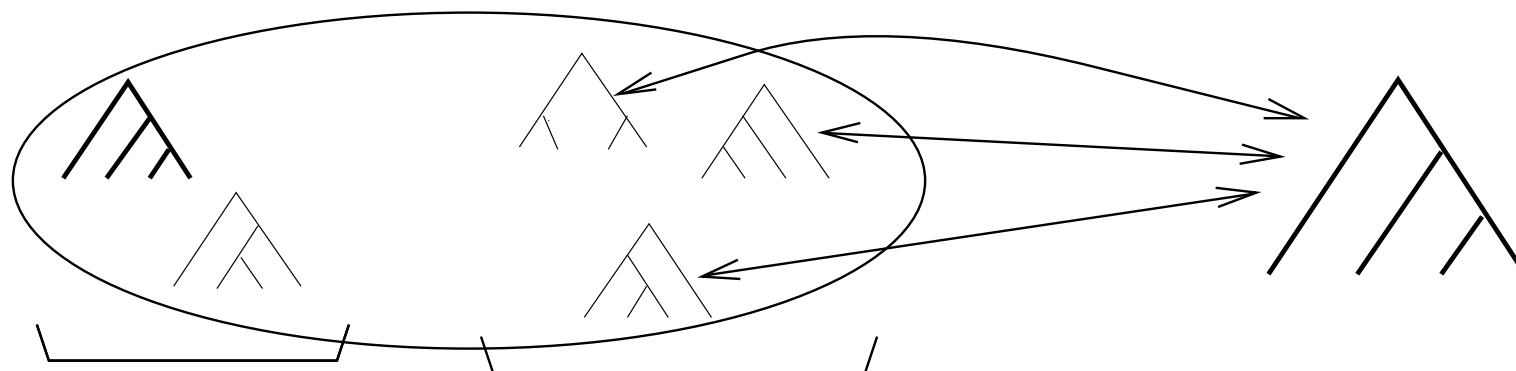
*New idea:* **See if its NF matches an old parse's. Can do in  $O(1)$  time.**

# Extensions: Finding Equiv Classes instead of NFs

Have proved 1-1 correspondence:



So use each NF tree as a magnet for its equivalence class:



*not found by parser  
(disallowed by grammar,  
or conflict with prior  
"incremental" commitments)*

*keep just one of these legal parses – e.g. the first,  
or the best according to prosody or discourse module*

# Summary of Results

- + A useful model–theoretic definition of spurious ambiguity . . . and a lemma giving a syntactic test for it.**
- + Easy, fast parser for CCG with the B and S rules.  
Simple constraints provably eliminate all spurious ambiguity.**
- + Fast parser still possible if grammar rules have nasty restrictions:  
Rapidly group legal (sub)trees by semantic equivalence class –  
just have each NF tree point to the legal trees in its class.**