

Properties of Coordinate System
transformations• Used to convert the coordinates of a point
specified in one coordinate system to another. $P_A = T_{A_B} \cdot P_B$ • Can be *inverted*Inverse of $T_{A_B} = T_{B_A}$



Properties of Coordinate System Transformations

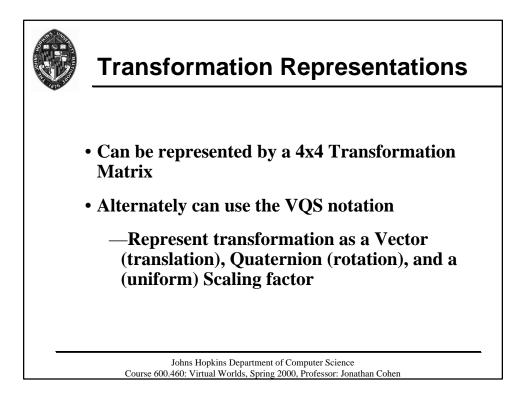
• Can be *composed* to compute the relationship between several coordinate systems

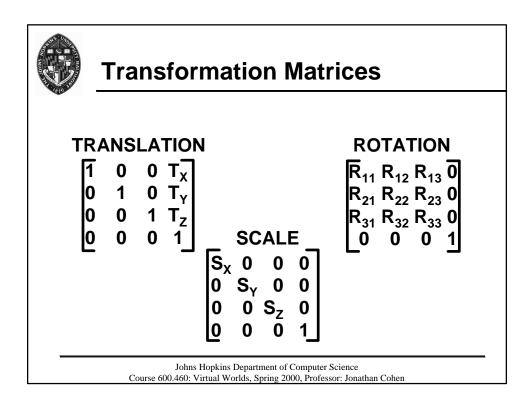
$$\mathbf{T}_{\mathbf{A}_{\mathbf{C}}} = \mathbf{T}_{\mathbf{A}_{\mathbf{B}}} \bullet \mathbf{T}_{\mathbf{B}_{\mathbf{C}}}$$

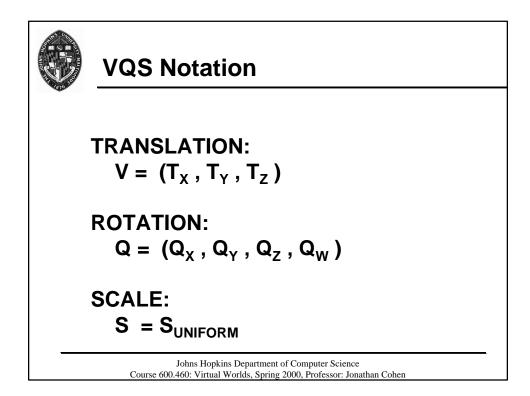
---Note: Nice property of subscript cancellation

Example:

 $T_{Shoulder_Hand} = T_{Shoulder_Elbow} \bullet T_{Elbow_Hand}$



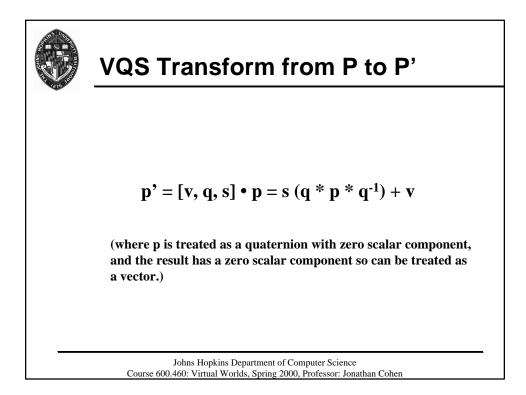


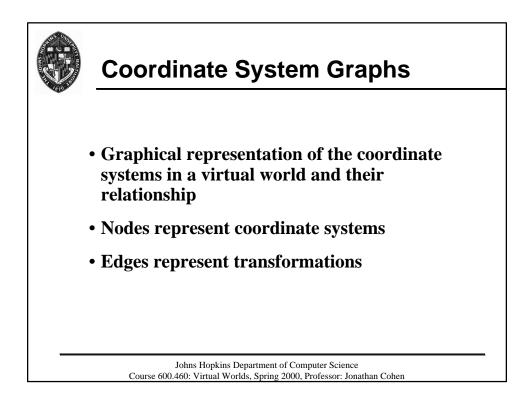


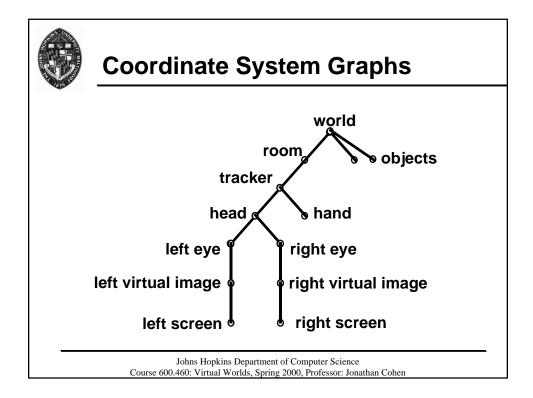


Transformations: Why Quaternions?

- Allow simple interpolation
- More compact
- Angle and axis of rotation easy to extract
- More efficient (composing and inverting)
- More tractable mathematically than matrices or Euler angles









Coordinate System Graphs: How do I use them?

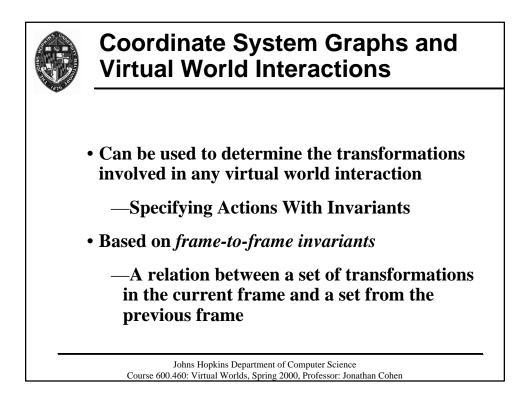
Can be used to determine the transformations involved in converting between coordinate systems.

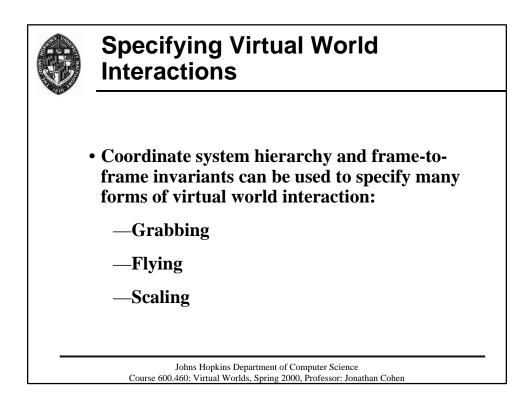
Example: Finding world coord of head space point

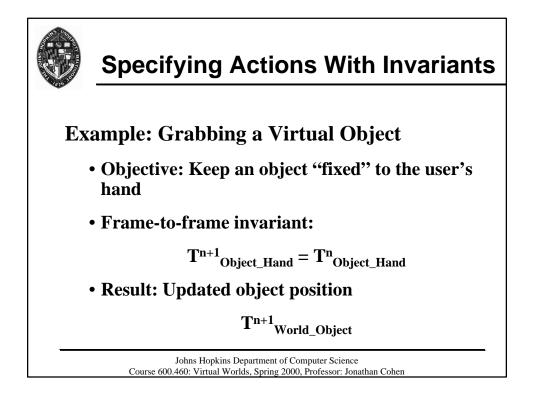
$$\mathbf{P}_{\mathbf{World}} = \mathbf{T}_{\mathbf{World_Head}} \bullet \mathbf{P}_{\mathbf{Head}}$$

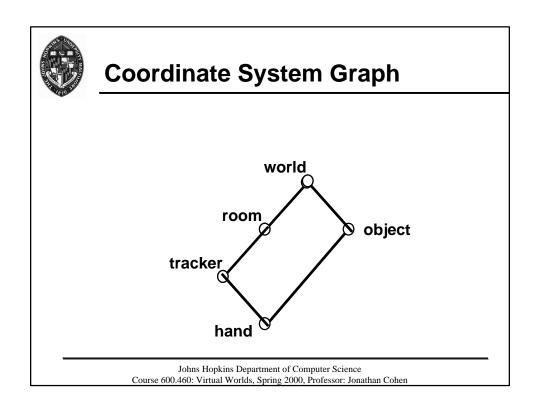
 $\mathbf{T}_{\text{World_Head}} = \mathbf{T}_{\text{World_Room}} \bullet \mathbf{T}_{\text{Room_Tracker}} \bullet \mathbf{T}_{\text{Tracker_Head}}$

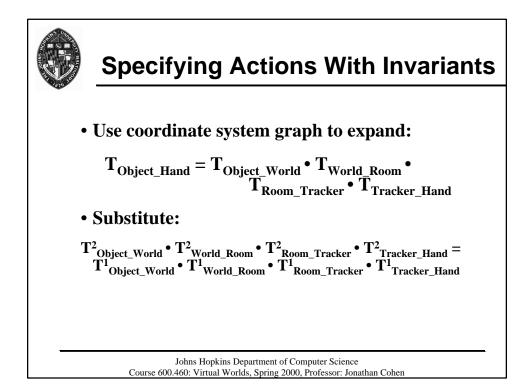
 $\mathbf{P}_{\text{World}} = \mathbf{T}_{\text{World}_\text{Room}} \bullet \mathbf{T}_{\text{Room}_\text{Tracker}} \bullet \mathbf{T}_{\text{Tracker}_\text{Head}} \bullet \mathbf{P}_{\text{Head}}$

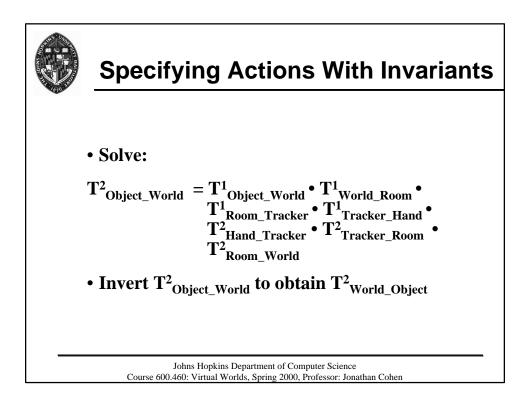


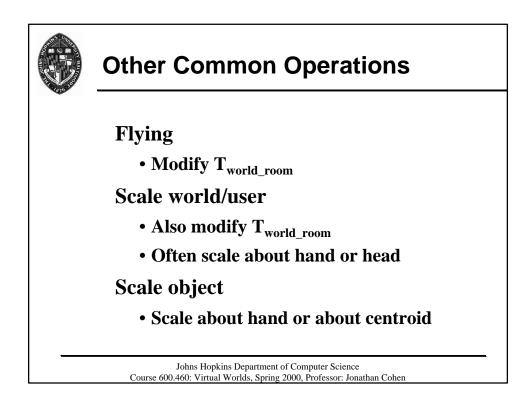














Where do I learn more?

• Computer graphics texts (e.g. Foley, vanDam, Feiner, and Hughes)

---probably on reserve at MSE for Kumar's Computer Graphics class

• 1994 Paper by Robinett and Holloway

-READ IT!

- Paper on quaternions by Shoemake and Chou
- Quaternion/transformation support provided by quatlib

