

Deep Networks

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Supervised Learning $y=f(\mathbf{x})$

- Binary Classification:
 - Given $\mathbf{x}$ find $y \in \{-1, 1\}$
- Multiclass Classification
 - Given $\mathbf{x}$ find $y \in \{1, \dots, k\}$
- Regression
 - Given $\mathbf{x}$ find $y \in \mathbb{R}$ (or, $\mathbb{R}^d$)

Traditional Recognition Approach



Image

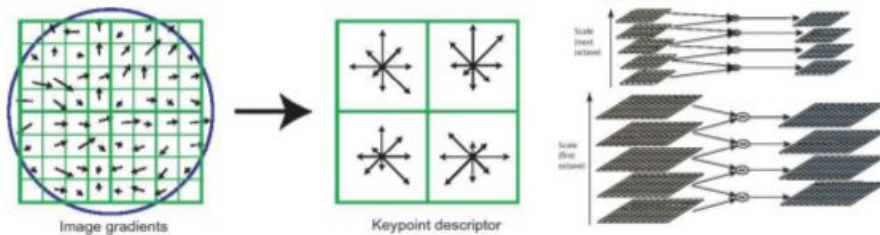


Low-level vision features (edges, SIFT, HOG, etc.)

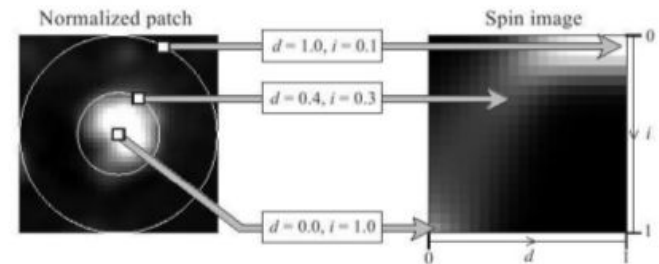


Object detection / classification

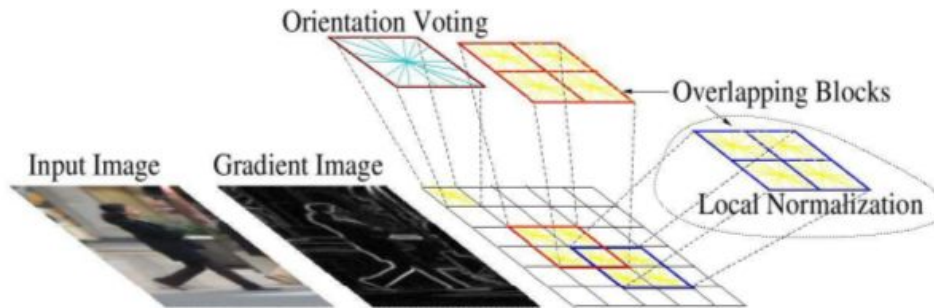
Computer vision features



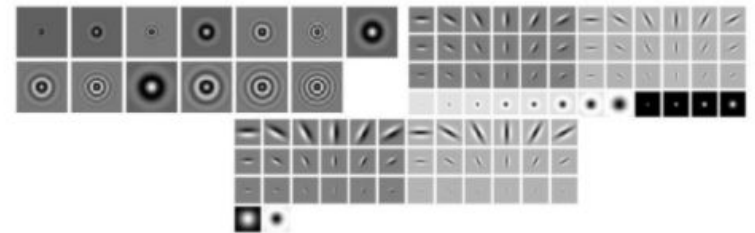
SIFT



Spin image



HoG



Textons

and many others:

SURF, MSER, LBP, Color-SIFT, Color histogram, GLOH,

Computer vision features

SIFT

Computer vision features

SIFT

HOG

Computer vision features

SIFT

LBP

HOG

Computer vision features

SIFT

LBP

HOG

SURF

Computer vision features

SIFT

LBP

HOG

SURF

MSER

Computer vision features

SIFT

LBP

Textons

HOG

SURF

MSER

Computer vision features

SIFT

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Computer vision features

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Computer vision features

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Computer vision features

SIFT

SPIN

LBP

GLOH

Texton

HOG

PHOG

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MSER

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SIFT

Computer vision features

SIFT

SPIN

LBP

GLOH

Texton

HOG

PHOG

s

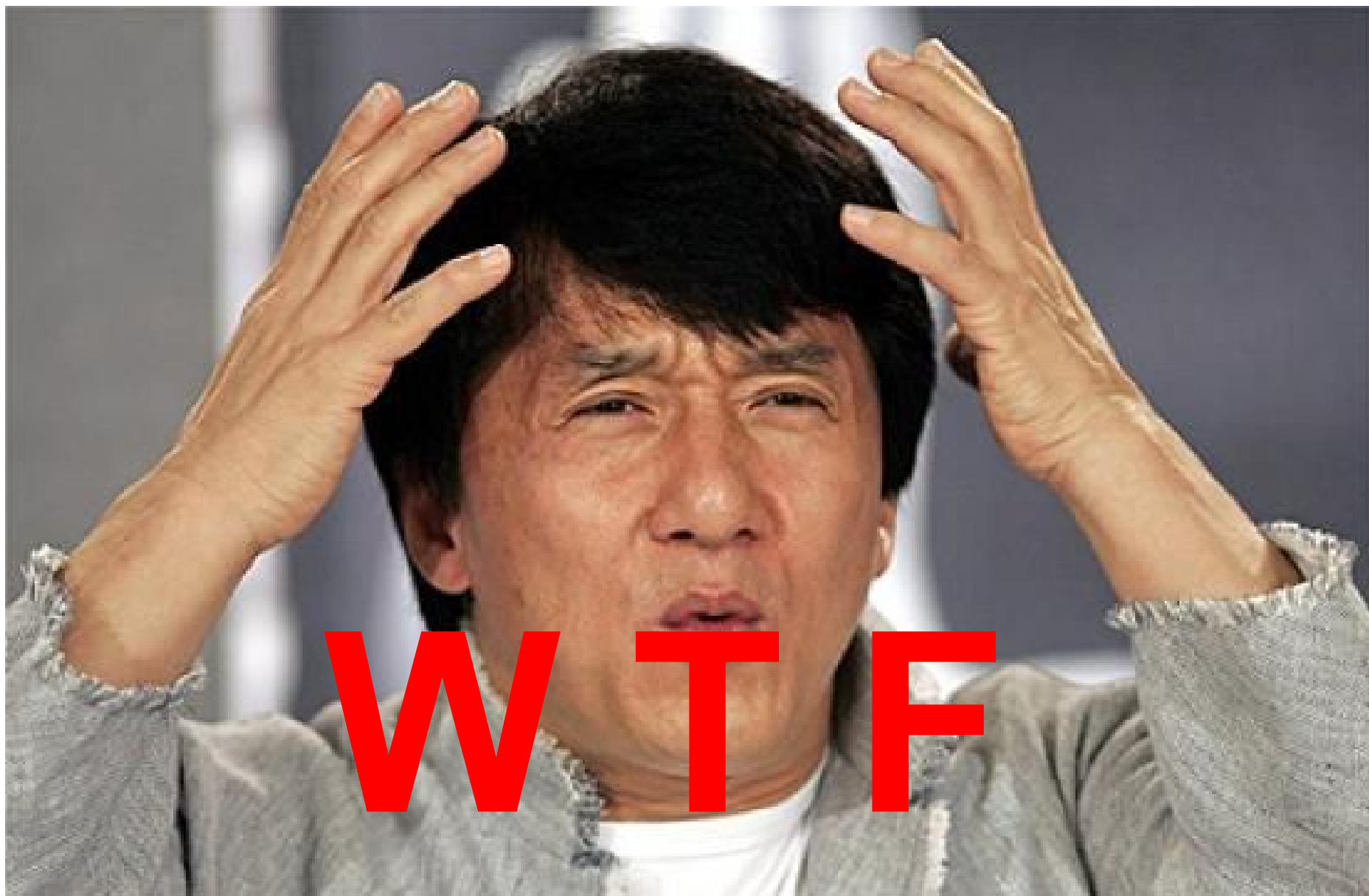
Color-

MSER

SURF

SIFT

...



A close-up photograph of Jackie Chan. He has a frustrated or overwhelmed expression, with his eyebrows furrowed and his mouth slightly open. He is holding both hands to his temples, with his fingers spread. He is wearing a grey, textured jacket over a white shirt. The background is blurred, showing what appears to be an indoor setting with some vertical lines.

Which

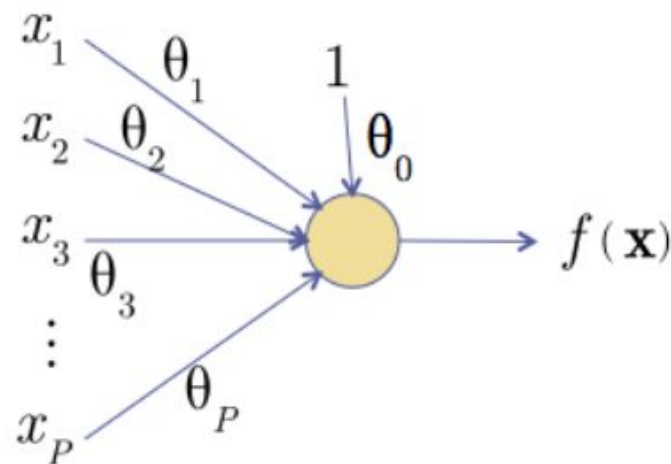
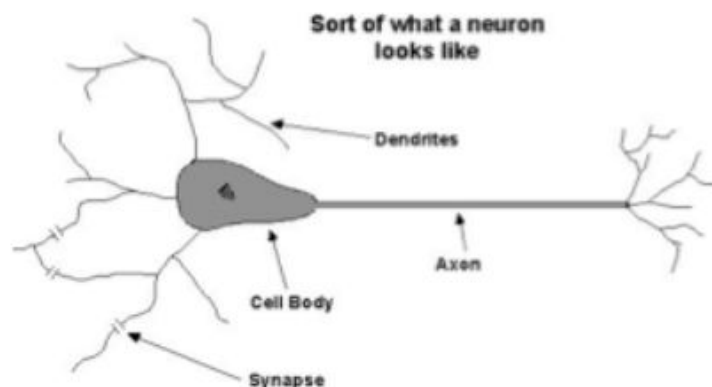
Training

Features to use?

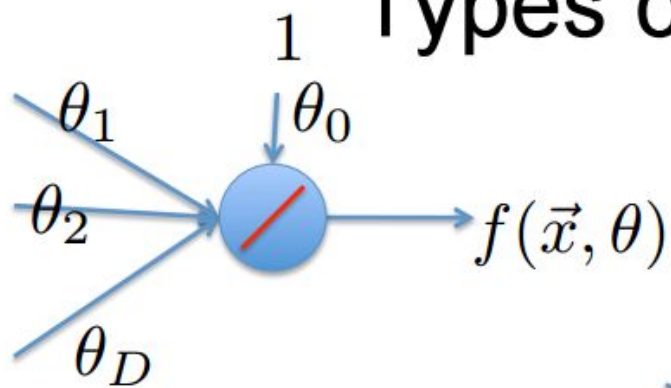
Can we learn the
features (internal
representations)?

Recall: The Neuron Metaphor

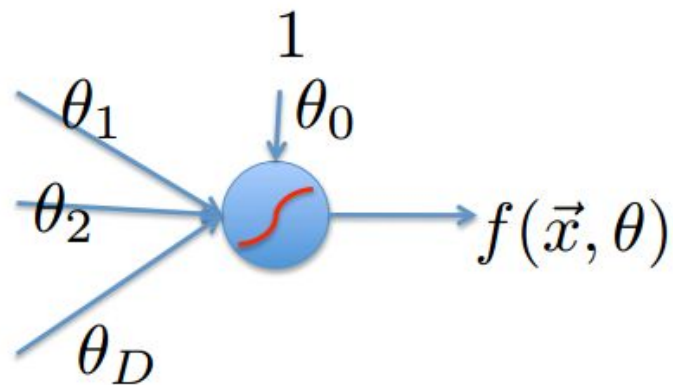
- Neurons
 - accept information from multiple inputs,
 - transmit information to other neurons.
- Multiply inputs by weights along edges
- Apply some function to the set of inputs at each node



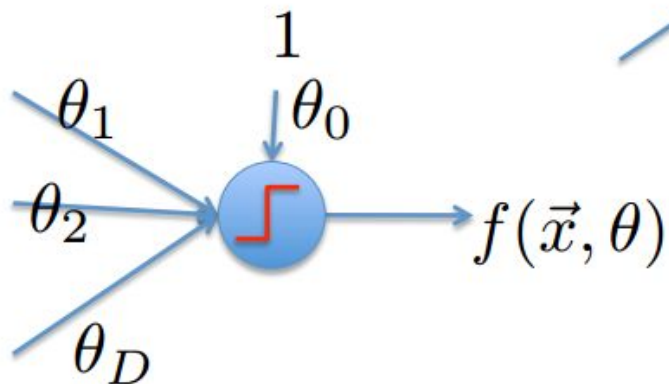
Types of Neurons



Linear Neuron



Logistic Neuron



Perceptron

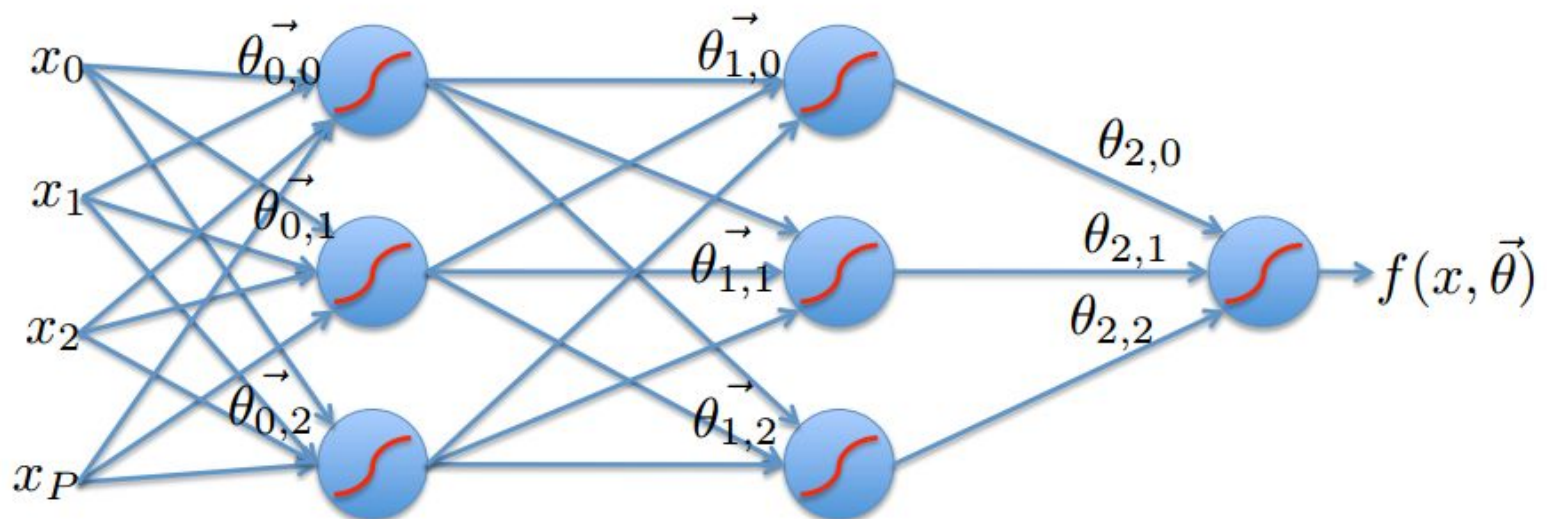
Potentially more. Require a convex loss function for gradient descent training.

Limitation

- A single “neuron” is still a linear decision boundary
- What to do?
- Idea: Stack a bunch of them together!

Multilayer Networks

- Cascade Neurons together
- The output from one layer is the input to the next
- Each Layer has its own sets of weights



A quick note

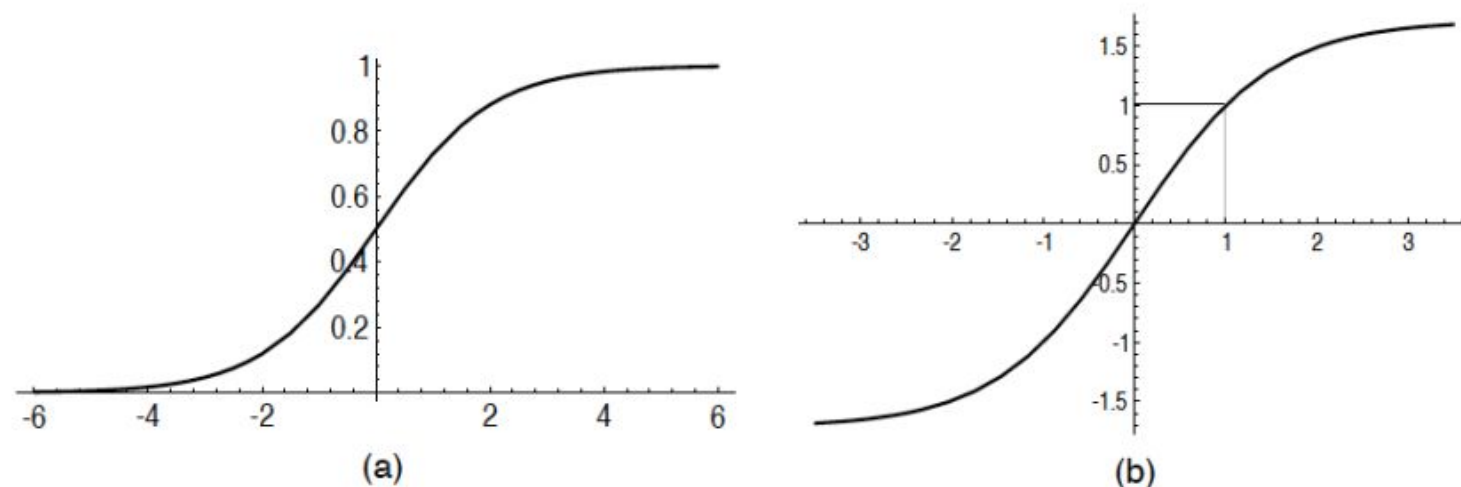
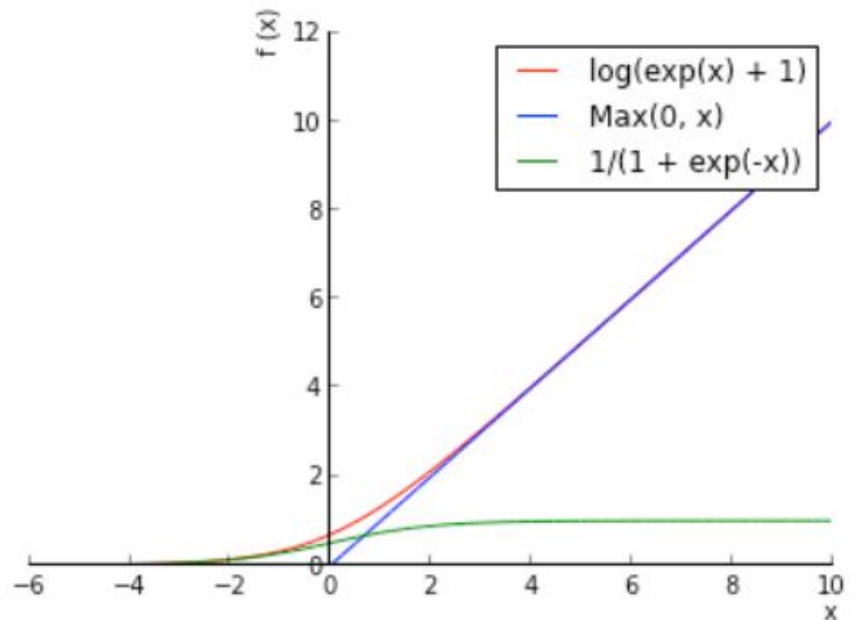
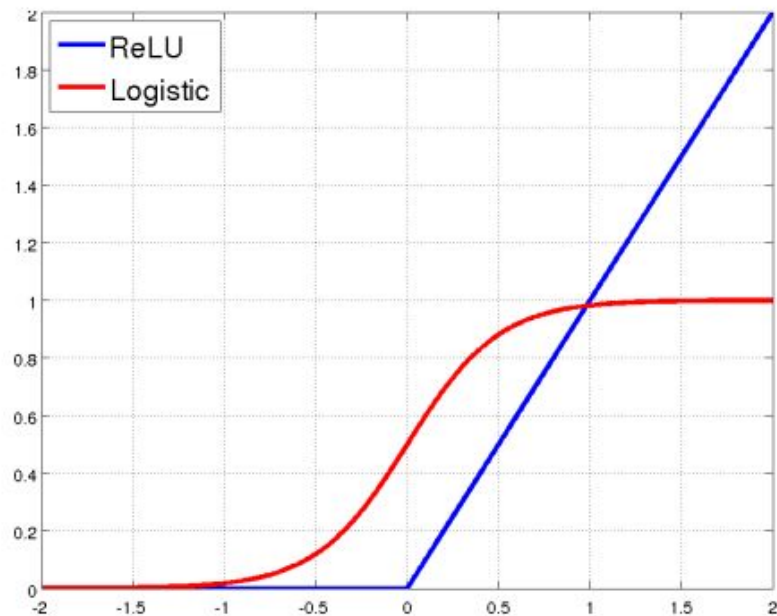


Fig. 4. (a) Not recommended: the standard logistic function, $f(x) = 1/(1 + e^{-x})$. (b) Hyperbolic tangent, $f(x) = 1.7159 \tanh(\frac{2}{3}x)$.

Rectified Linear Units (ReLU)



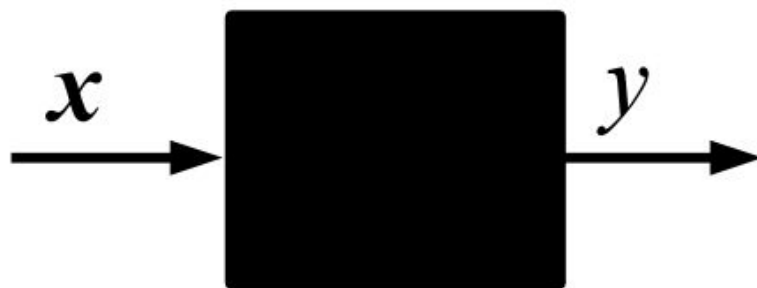
Supervised Learning

$\{(\mathbf{x}^i, y^i), i=1 \dots P\}$ training dataset

$\mathbf{x}^i$ i-th input training example

y^i i-th target label

P number of training examples



Goal: predict the target label of unseen inputs.

Supervised Learning: Examples

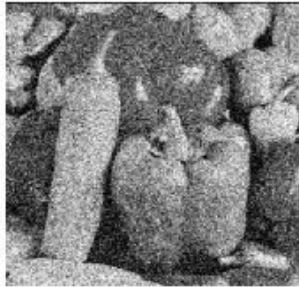
Classification



“dog”

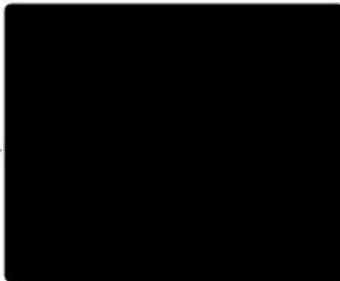
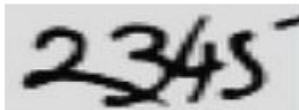
classification

Denoising



regression

OCR

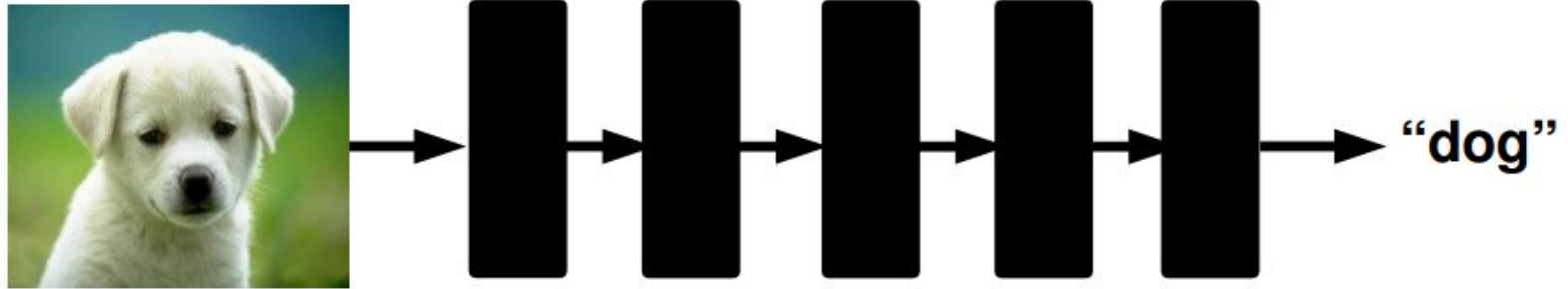


“2 3 4 5”

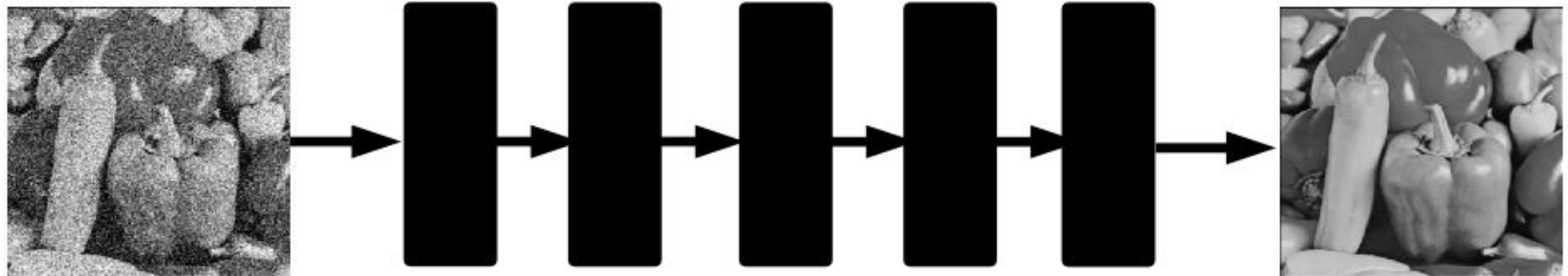
structured prediction

Supervised Deep Learning

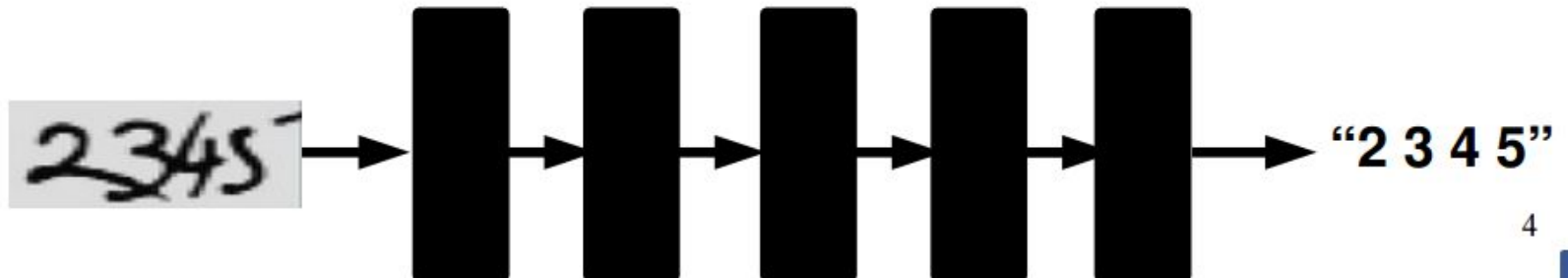
Classification



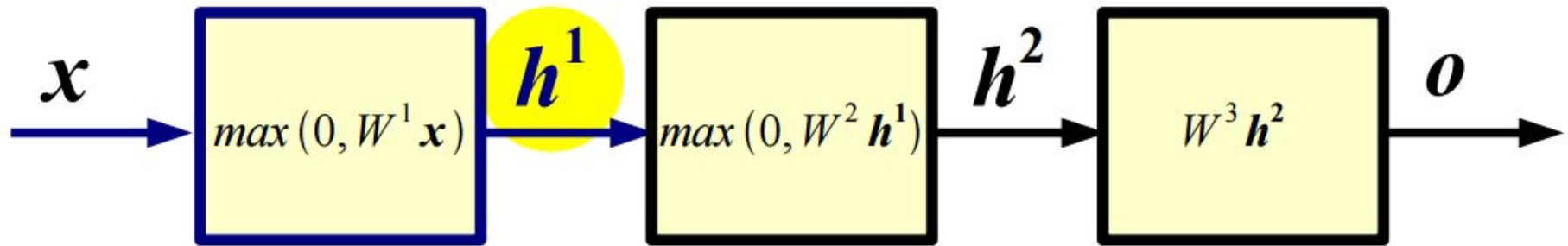
Denoising



OCR



Forward Propagation



$$x \in R^D \quad W^1 \in R^{N_1 \times D} \quad b^1 \in R^{N_1} \quad h^1 \in R^{N_1}$$

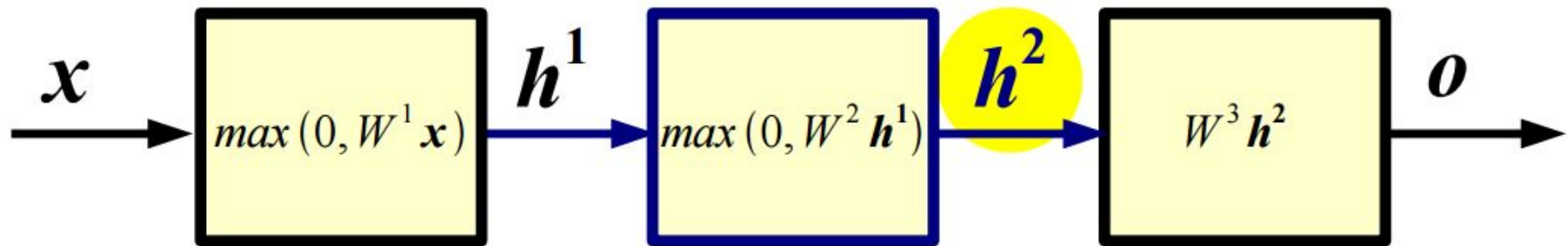
$$h^1 = \max(0, W^1 x + b^1)$$

W^1 1-st layer weight matrix or weights

b^1 1-st layer biases

The non-linearity $u = \max(0, v)$ is called **ReLU** in the DL literature. Each output hidden unit takes as input all the units at the previous layer: each such layer is called “**fully connected**”.

Forward Propagation



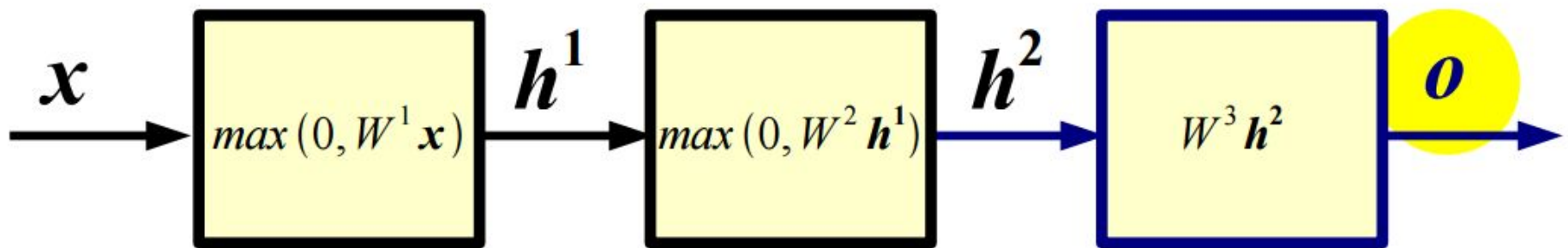
$$h^1 \in R^{N_1} \quad W^2 \in R^{N_2 \times N_1} \quad b^2 \in R^{N_2} \quad h^2 \in R^{N_2}$$

$$h^2 = \max(0, W^2 h^1 + b^2)$$

W^2 2-nd layer weight matrix or weights

b^2 2-nd layer biases

Forward Propagation



$$h^2 \in R^{N_2} \quad W^3 \in R^{N_3 \times N_2} \quad b^3 \in R^{N_3} \quad o \in R^{N_3}$$

$$o = \max(0, W^3 h^2 + b^3)$$

W^3 3-rd layer weight matrix or weights
 b^3 3-rd layer biases

Training

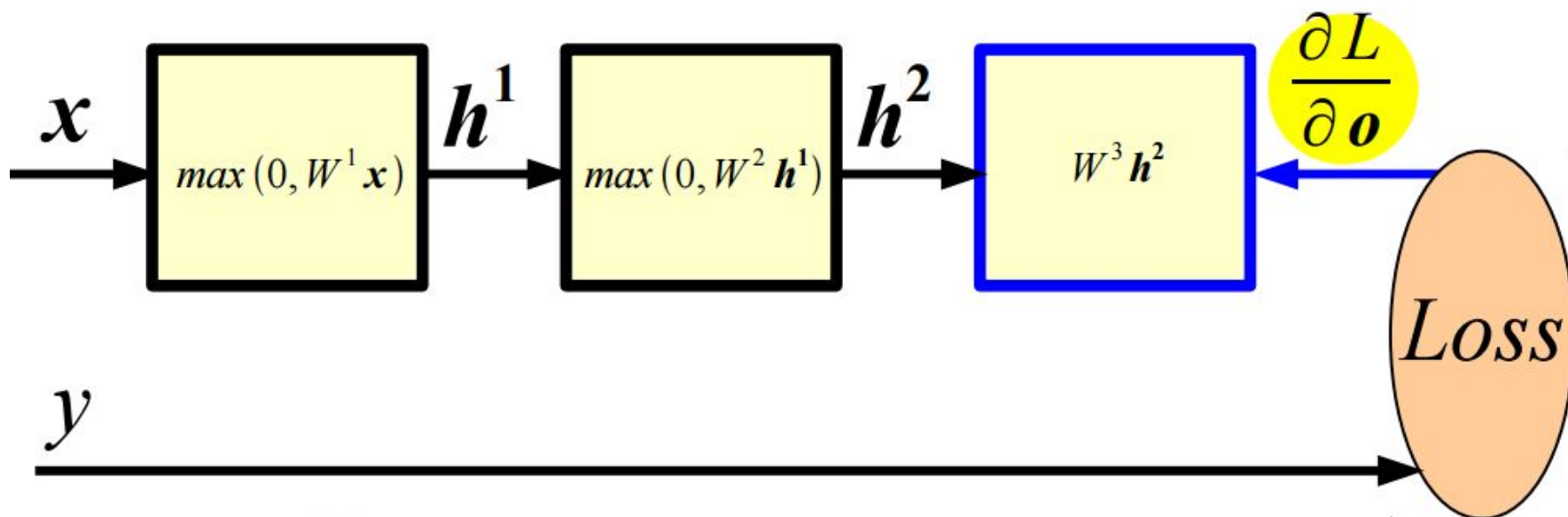
Learning consists of minimizing the loss (plus some regularization term) w.r.t. parameters over the whole training set.

$$\theta^* = \arg \min_{\theta} \sum_{n=1}^P L(\mathbf{x}^n, y^n; \theta)$$

Question: How to minimize a complicated function of the parameters?

Answer: Chain rule, a.k.a. **Backpropagation!** That is the procedure to compute gradients of the loss w.r.t. parameters in a multi-layer neural network.

Backward Propagation

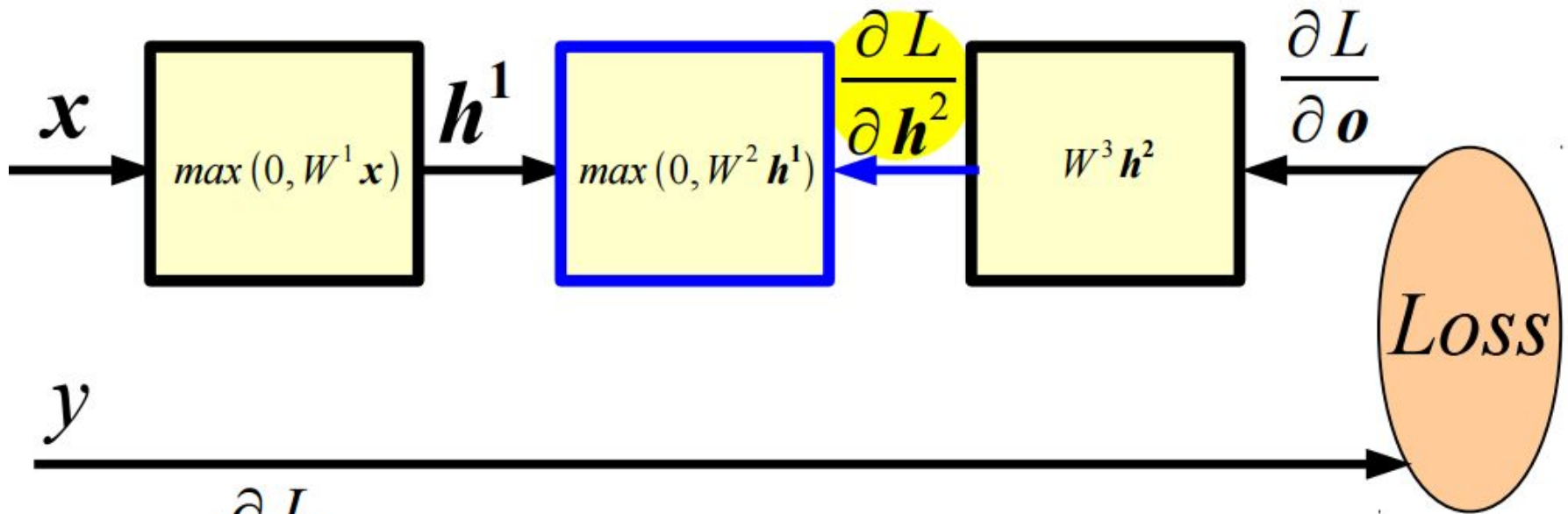


Given $\partial L / \partial \mathbf{o}$ and assuming we can easily compute the Jacobian of each module, we have:

$$\frac{\partial L}{\partial W^3} = \frac{\partial L}{\partial \mathbf{o}} \frac{\partial \mathbf{o}}{\partial W^3}$$

$$\frac{\partial L}{\partial \mathbf{h}^2} = \frac{\partial L}{\partial \mathbf{o}} \frac{\partial \mathbf{o}}{\partial \mathbf{h}^2}$$

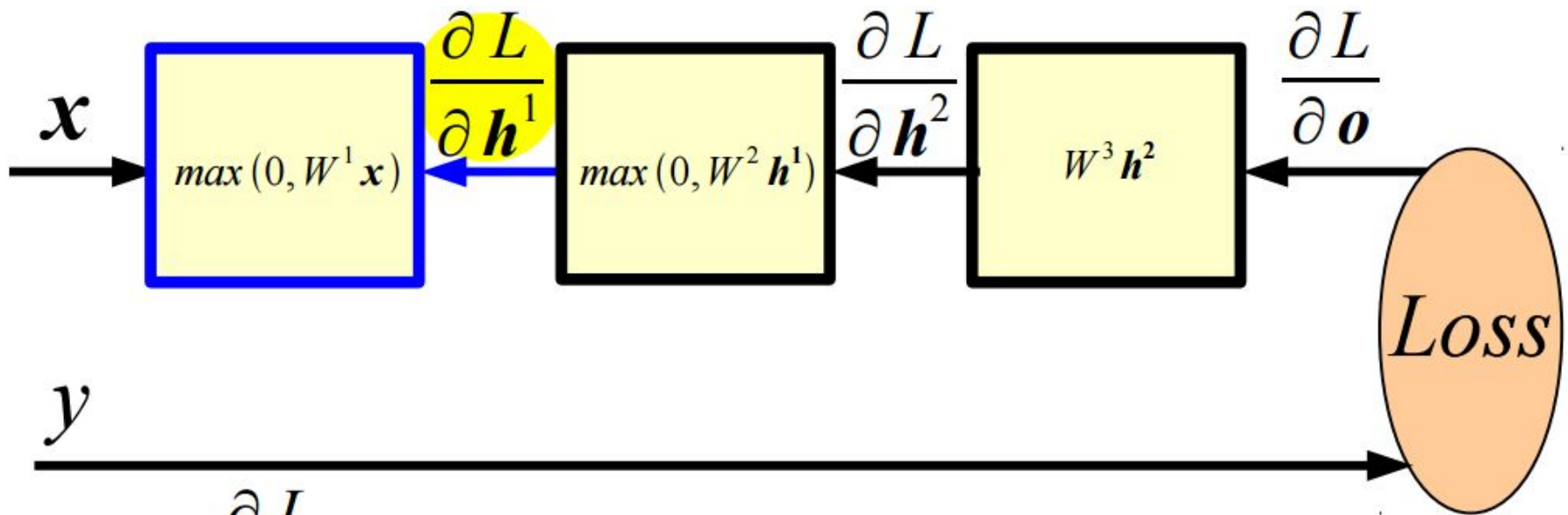
Backward Propagation



Given $\frac{\partial L}{\partial h^2}$ we can compute now:

$$\frac{\partial L}{\partial W^2} = \frac{\partial L}{\partial h^2} \frac{\partial h^2}{\partial W^2} \quad \frac{\partial L}{\partial h^1} = \frac{\partial L}{\partial h^2} \frac{\partial h^2}{\partial h^1}$$

Backward Propagation



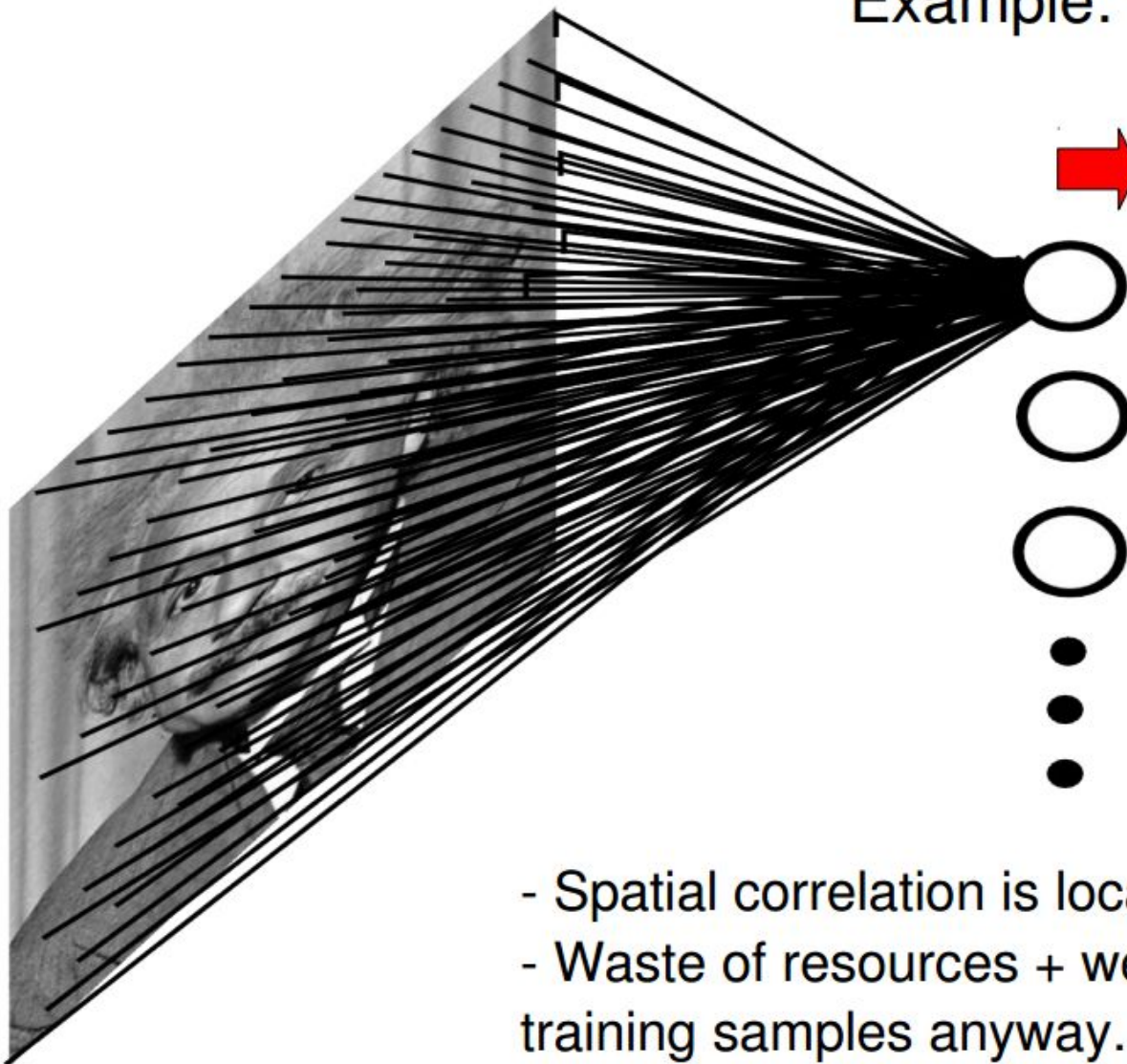
Given $\frac{\partial L}{\partial h^1}$ we can compute now:

$$\frac{\partial L}{\partial W^1} = \frac{\partial L}{\partial h^1} \frac{\partial h^1}{\partial W^1}$$

Convolutional Neural Networks

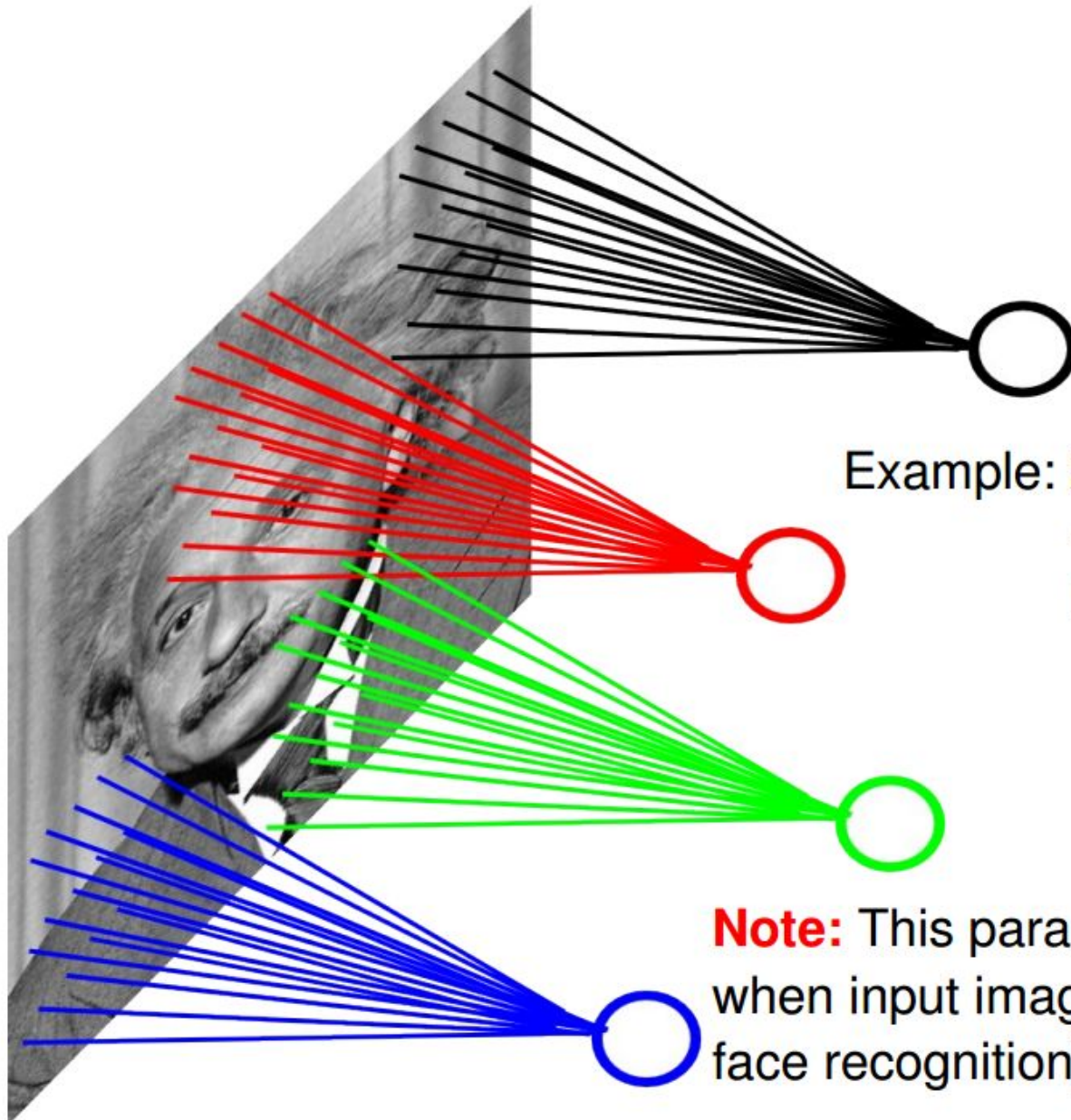
Fully Connected Layer

Example: 200x200 image
40K hidden units
→ **~2B parameters!!!**



- Spatial correlation is local
- Waste of resources + we have not enough training samples anyway..

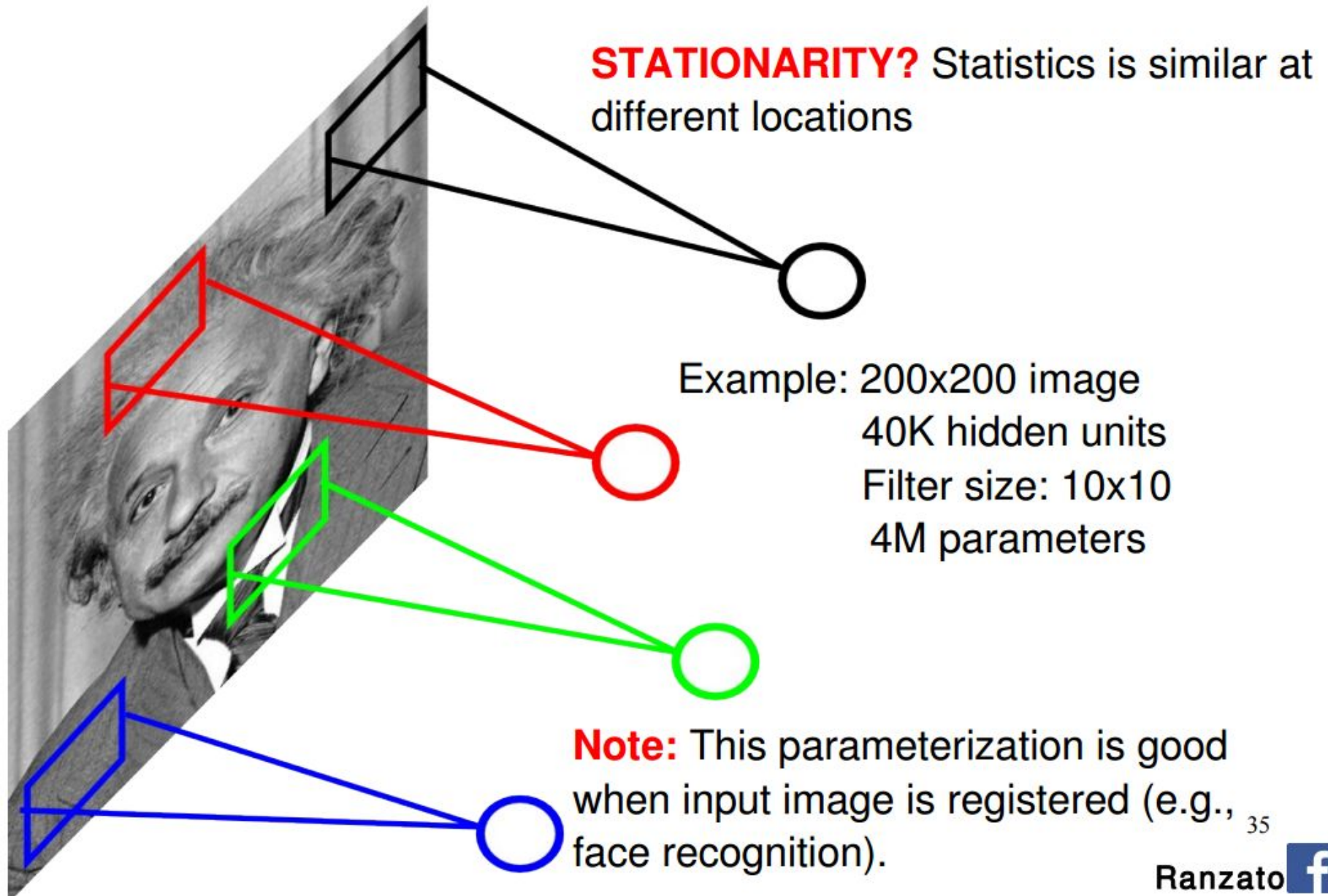
Locally Connected Layer



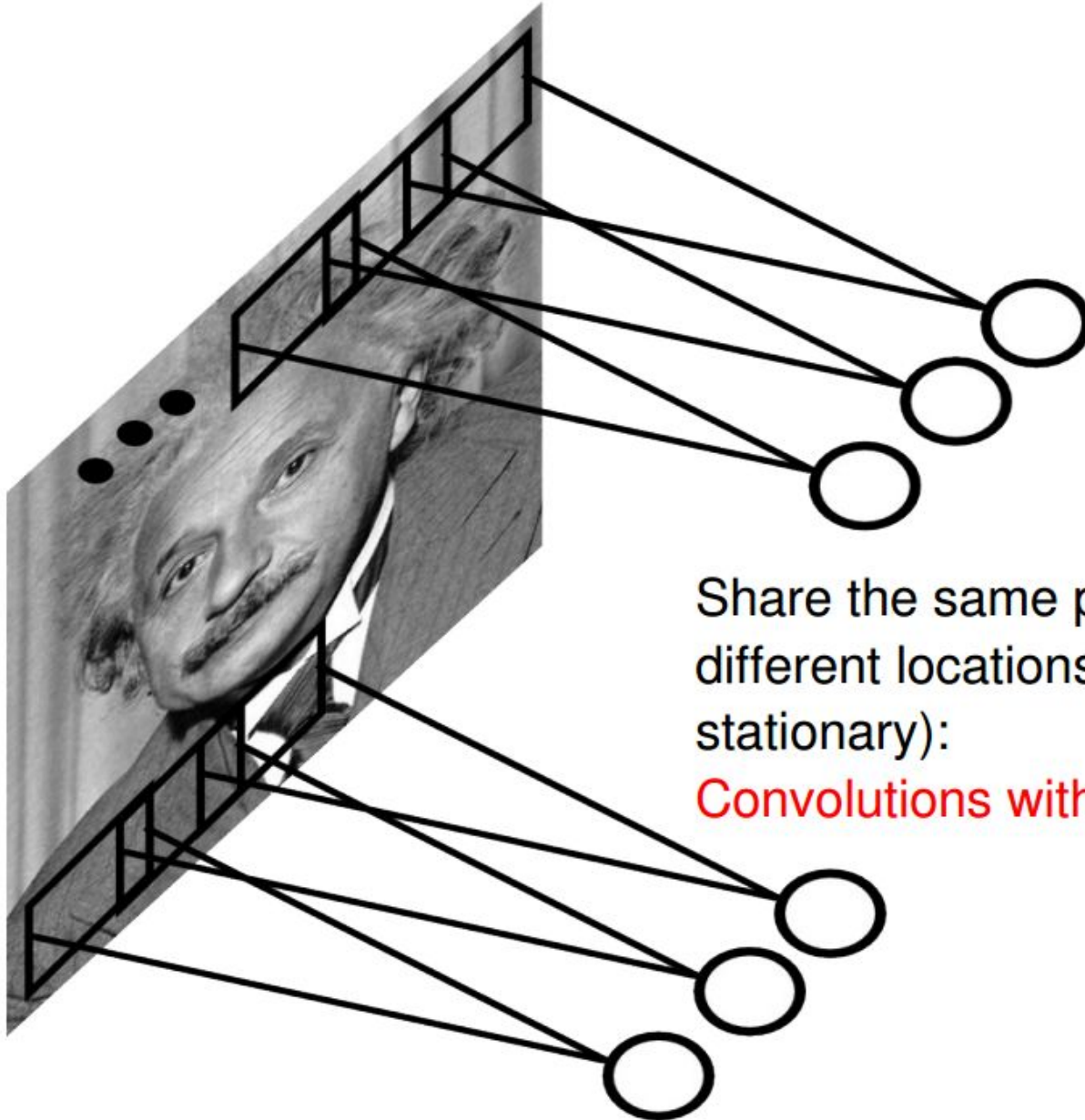
Example: 200x200 image
40K hidden units
Filter size: 10x10
4M parameters

Note: This parameterization is good when input image is registered (e.g., face recognition).

Locally Connected Layer



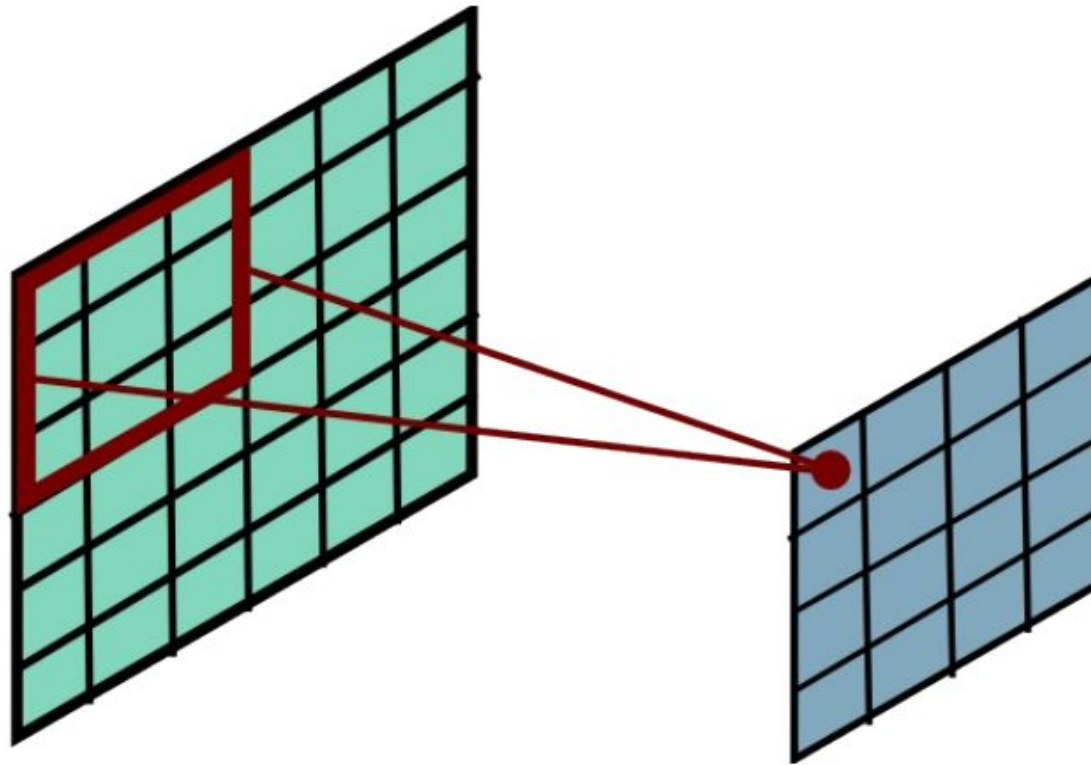
Convolutional Layer



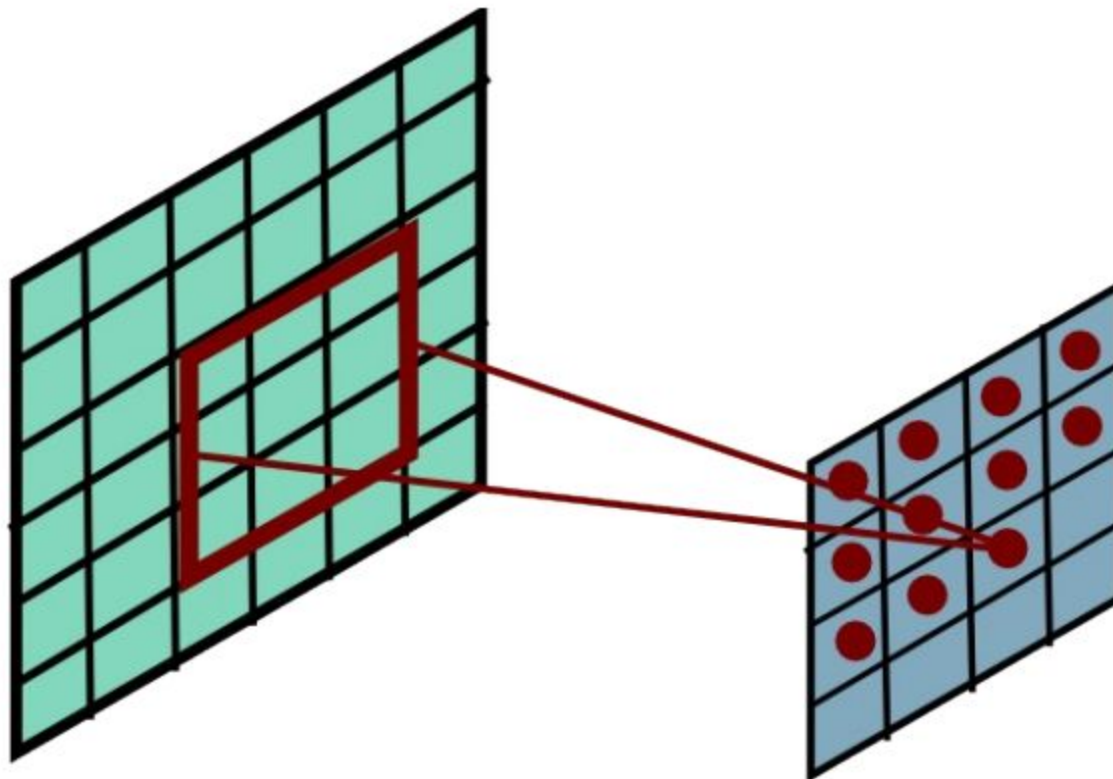
Share the same parameters across different locations (assuming input is stationary):

Convolutions with learned kernels

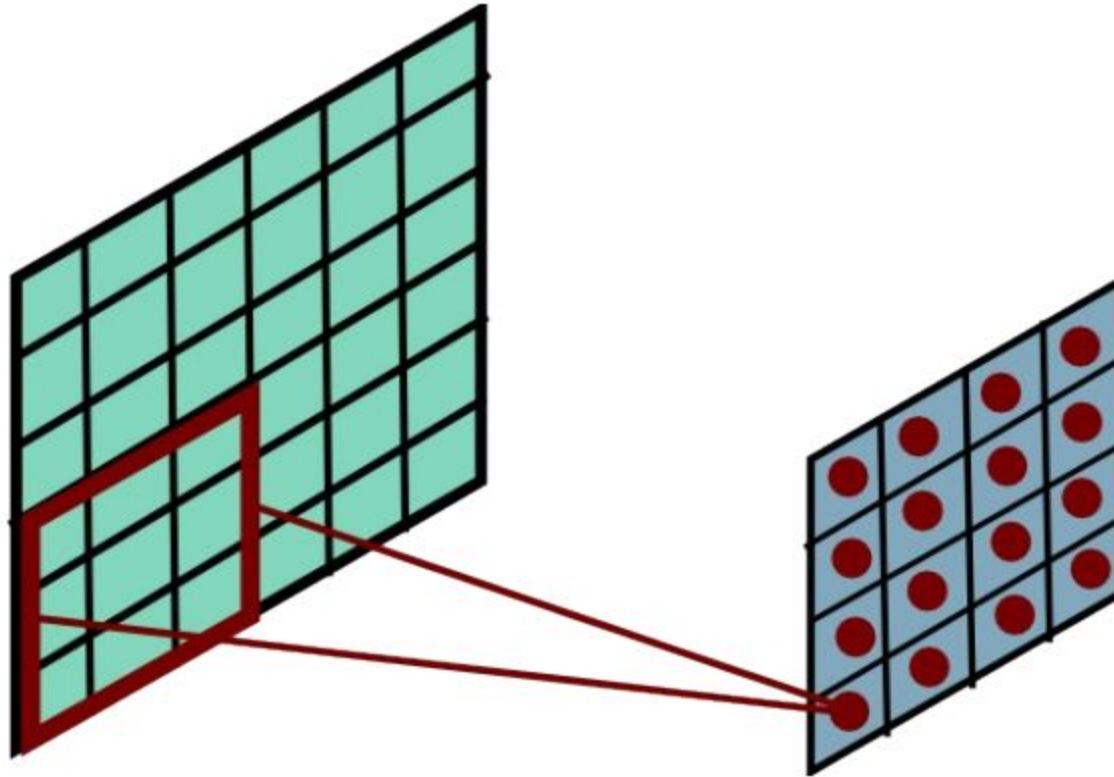
Convolutional Layer



Convolutional Layer



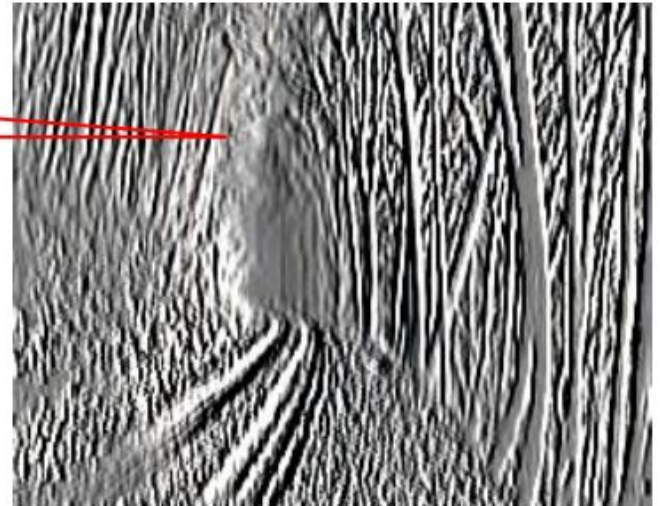
Convolutional Layer



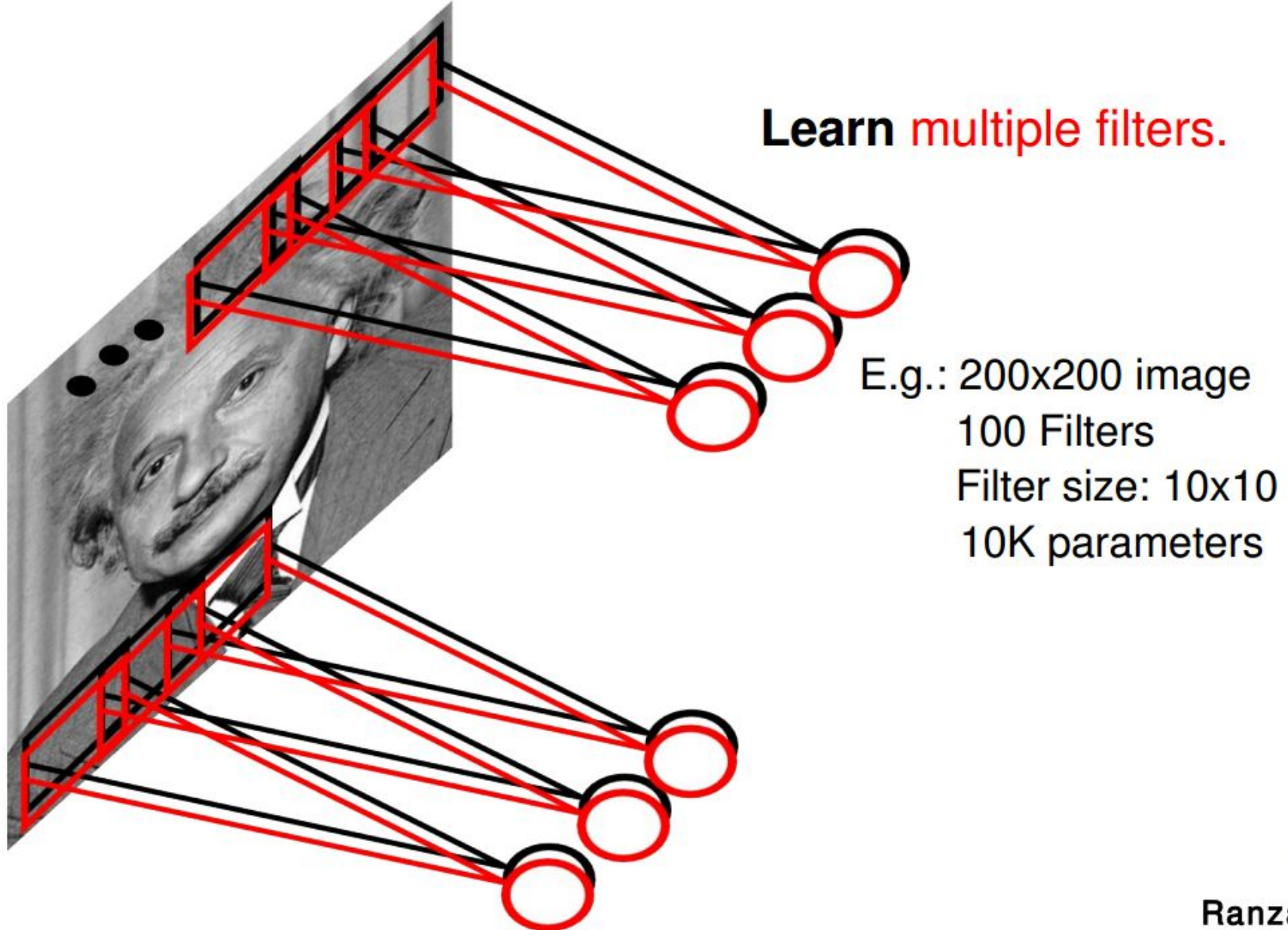
Convolutional Layer



$$\begin{matrix} * & \begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix} & = \end{matrix}$$



Convolutional Layer



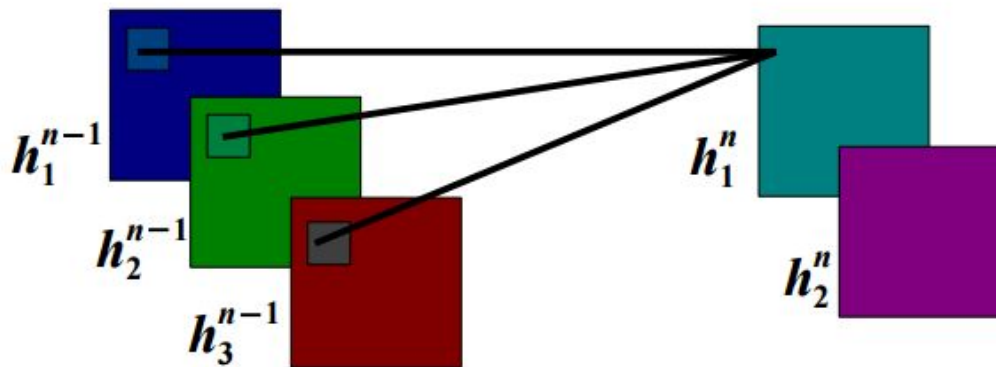
Convolutional Layer

$$h_j^n = \max(0, \sum_{k=1}^K h_k^{n-1} * w_{kj}^n)$$

output
feature map

input feature
map

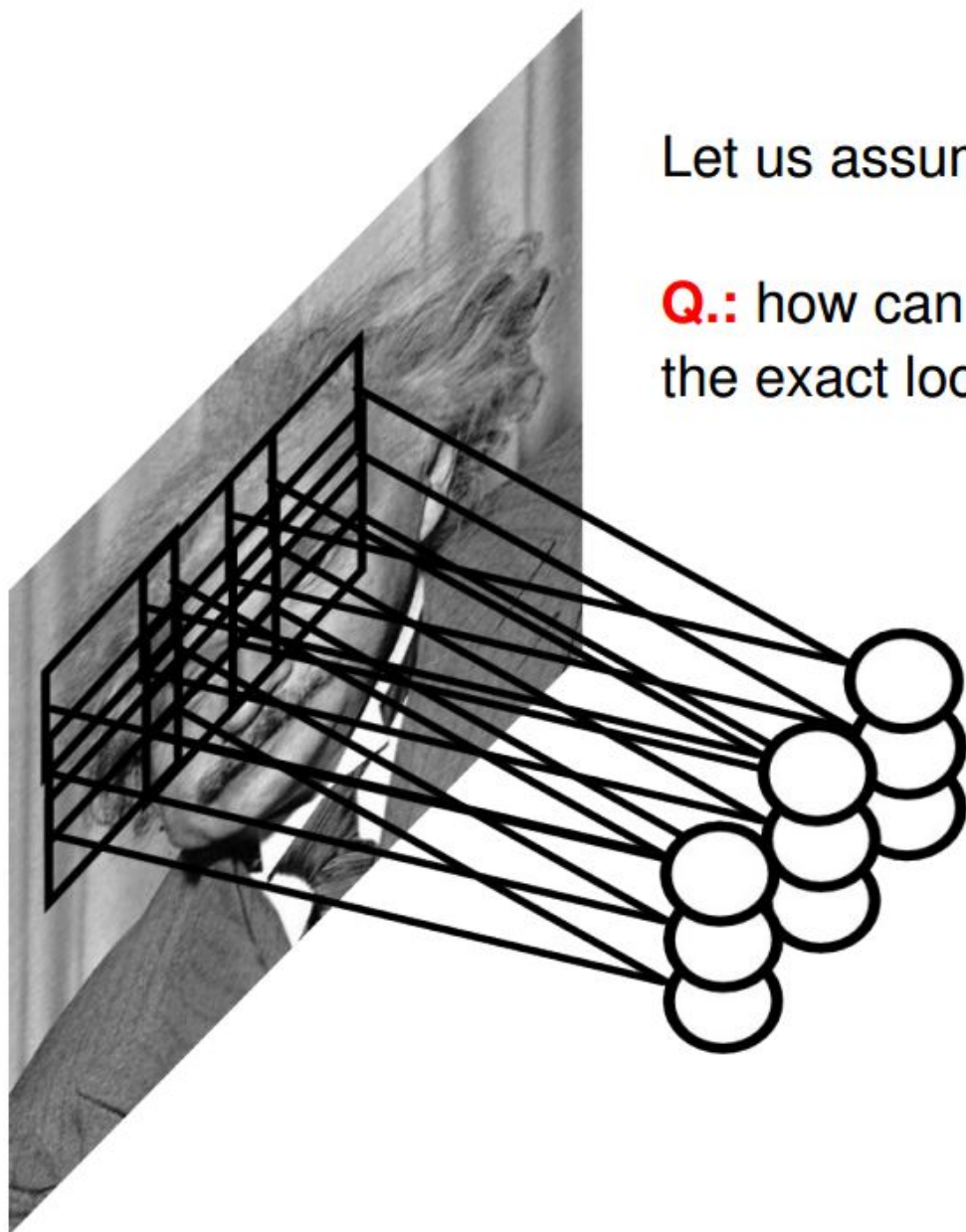
kernel



Pooling Layer

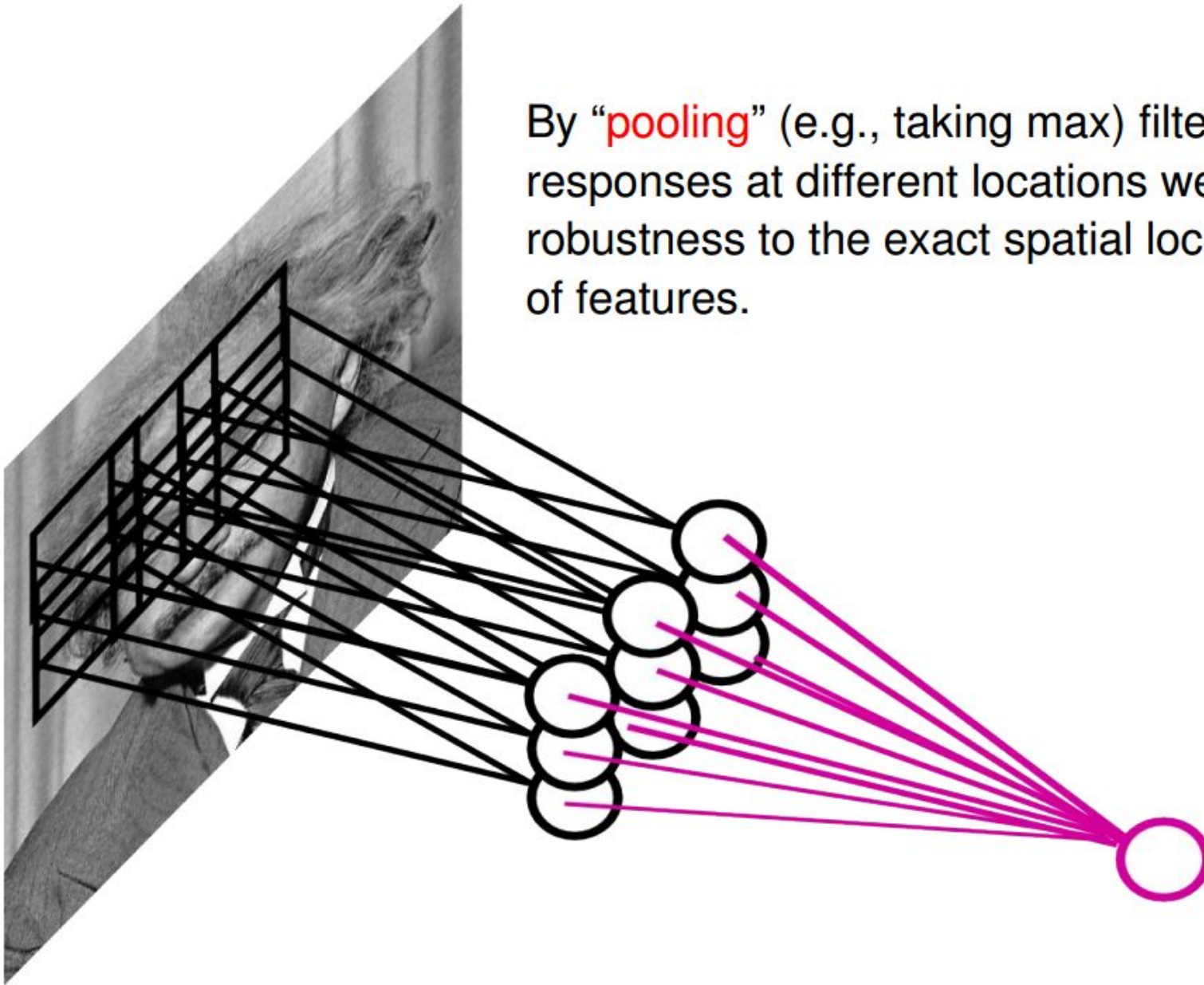
Let us assume filter is an “eye” detector.

Q.: how can we make the detection robust to the exact location of the eye?



Pooling Layer

By “pooling” (e.g., taking max) filter responses at different locations we gain robustness to the exact spatial location of features.



Pooling Layer: Examples

Max-pooling:

$$h_j^n(x, y) = \max_{\bar{x} \in N(x), \bar{y} \in N(y)} h_j^{n-1}(\bar{x}, \bar{y})$$

Average-pooling:

$$h_j^n(x, y) = 1/K \sum_{\bar{x} \in N(x), \bar{y} \in N(y)} h_j^{n-1}(\bar{x}, \bar{y})$$

L2-pooling:

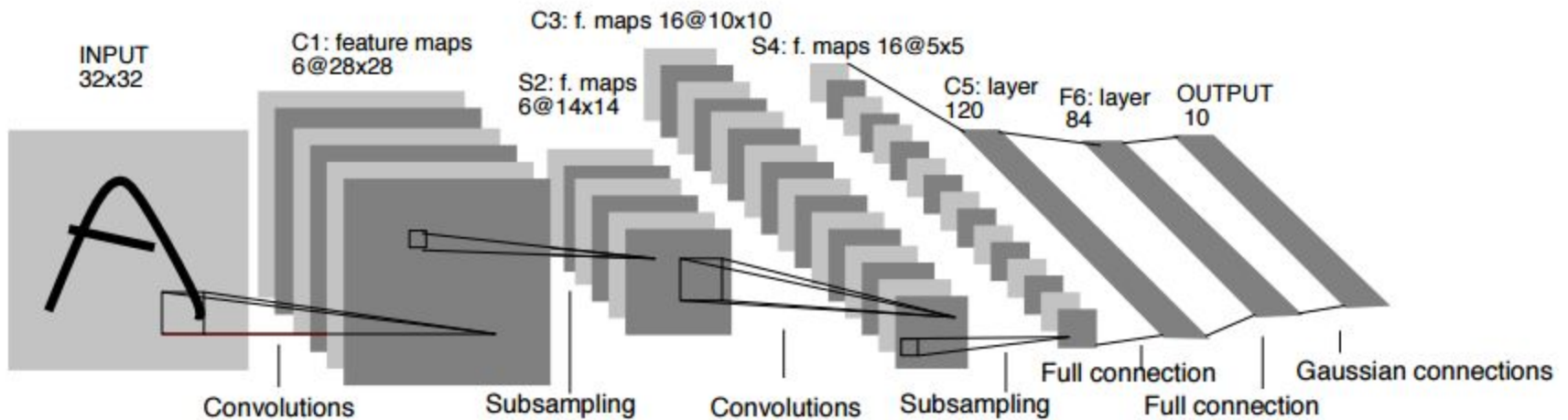
$$h_j^n(x, y) = \sqrt{\sum_{\bar{x} \in N(x), \bar{y} \in N(y)} h_j^{n-1}(\bar{x}, \bar{y})^2}$$

L2-pooling over features:

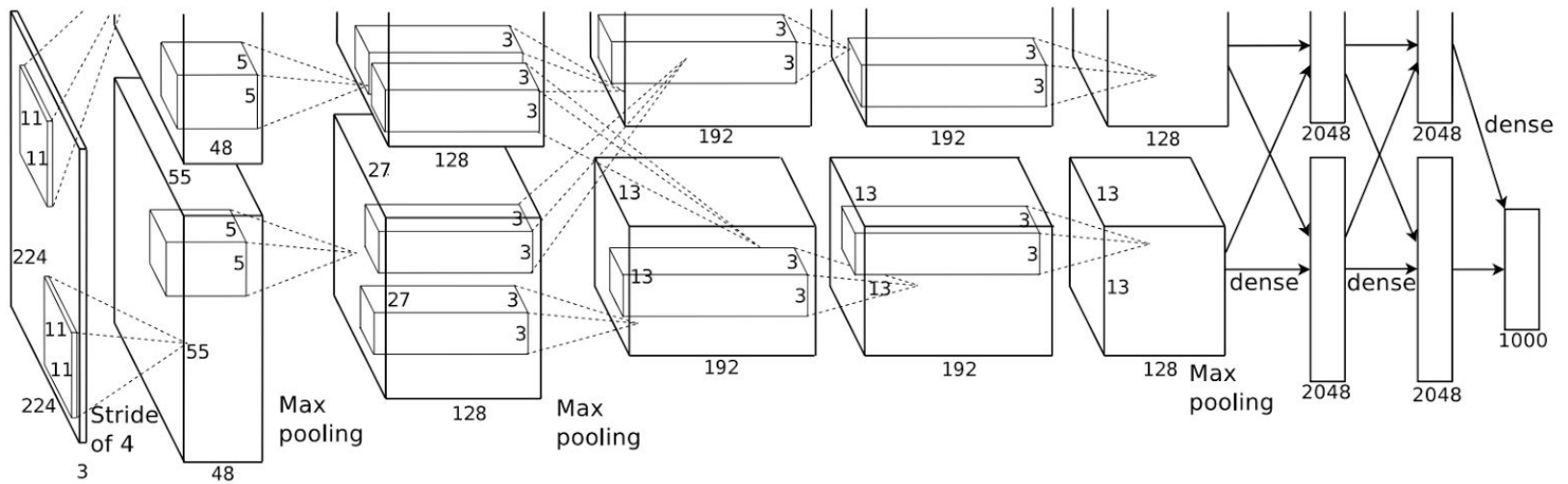
$$h_j^n(x, y) = \sqrt{\sum_{k \in N(j)} h_k^{n-1}(x, y)^2}$$

Convolutional Nets

- Example:
 - <http://yann.lecun.com/exdb/lenet/index.html>

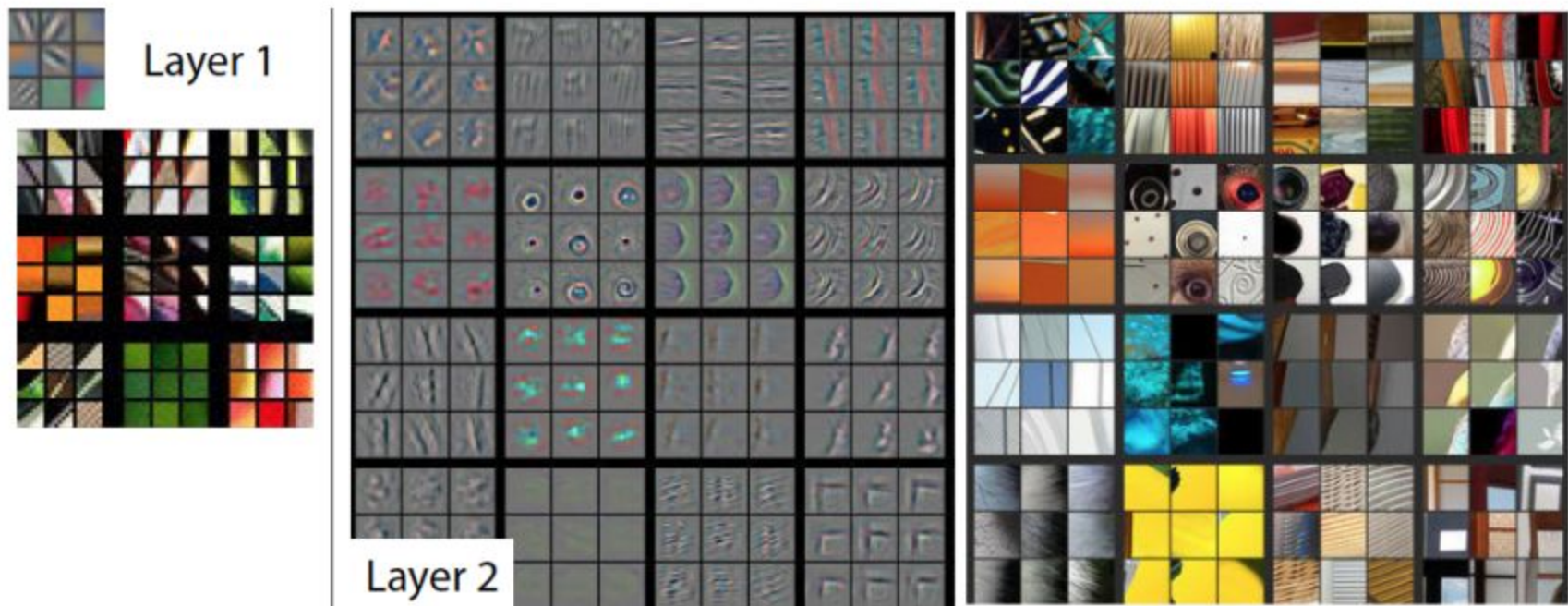


Alex Net

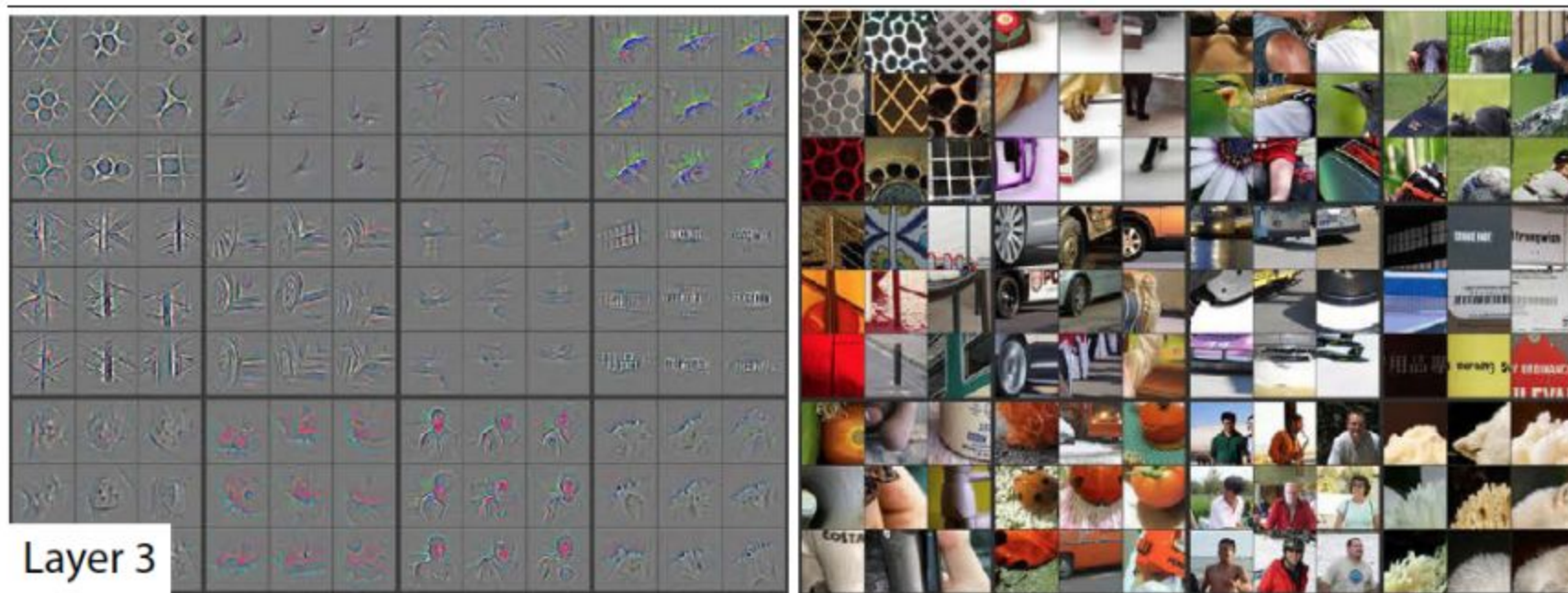


Krizhevsky et al. NIPS 2012

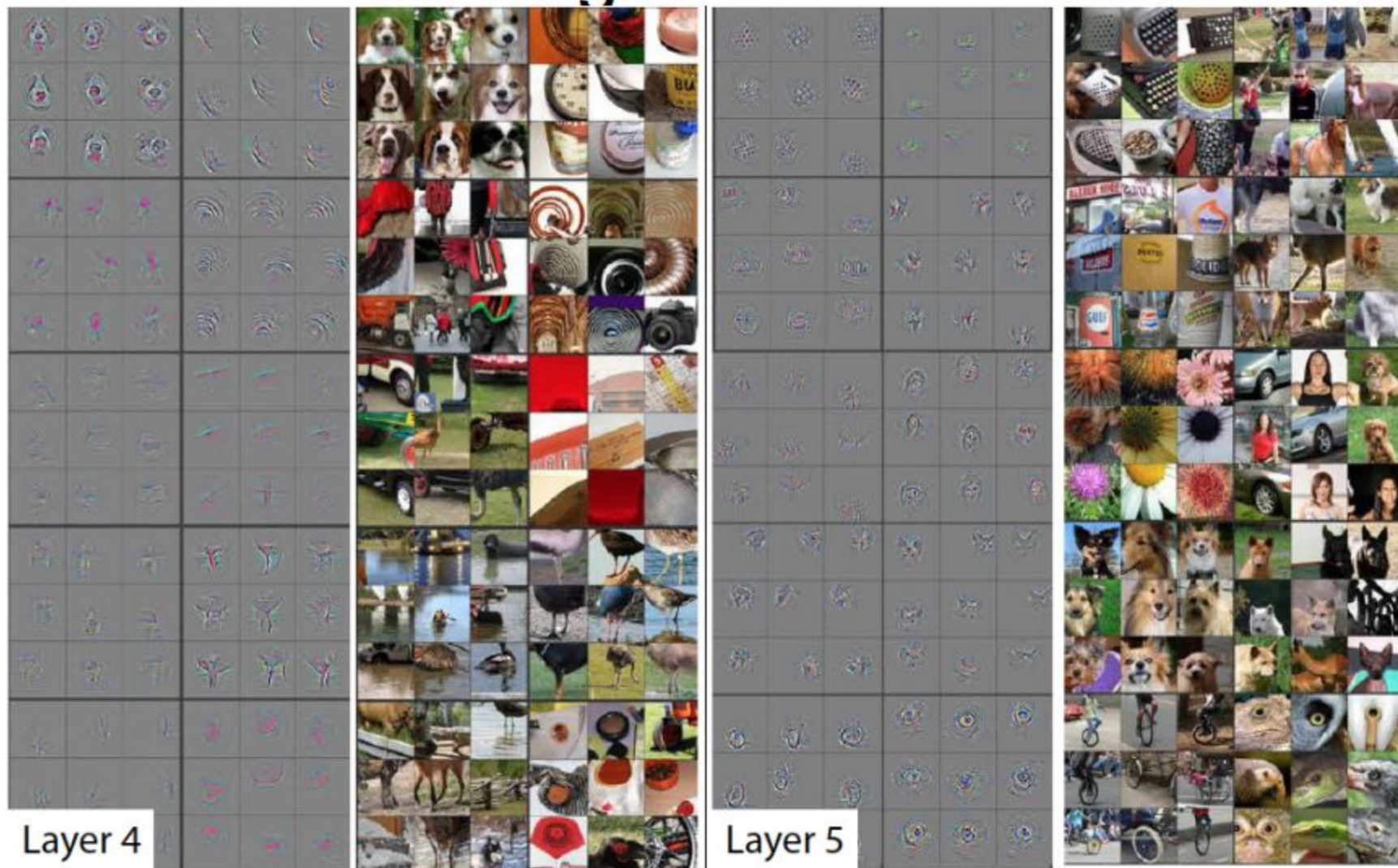
Visualizing Learned Filters



Visualizing Learned Filters

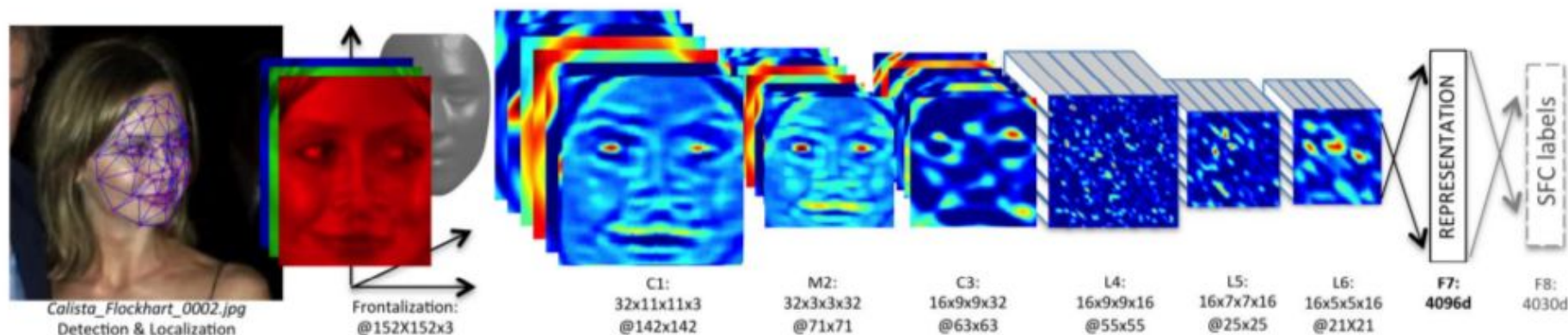


Visualizing Learned Filters



Industry Deployment

- Used in Facebook, Google, Microsoft
- Image Recognition, Speech Recognition,
- Fast at test time



Taigman et al. DeepFace: Closing the Gap to Human-Level Performance in Face Verification, CVPR'14