# From Co-occurrence to Correspondence

#### Ben Taskar

T. Cour, K. Ganchev, J. Graca, C. Jordan, B. Sapp











University of Pennsylvania







### Learning from Co-Occurrence

Foreign Language Lexicon

Visual Lexicon







HURLEY: Uh ... the Chinese people have water. (Sayid and Kate go to

check it out.)

[EXT. BEACH - CRASH SITE]

(Sayid holds the empty bottle in his hand and questions Sun.)

SAYID: (quietly) Where did you get this? (He looks at her.)

[EXT. JUNGLE]

(Sawyer is walking through the jungle. He reaches a spot. He kneels down and looks back to check that no one's followed him.



**SAYID** 

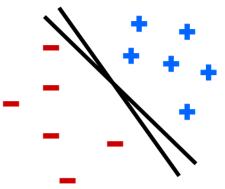


SUN



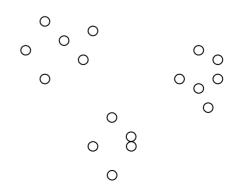
### Supervision in Learning

Supervised



• Co-occurrence?

Unsupervised

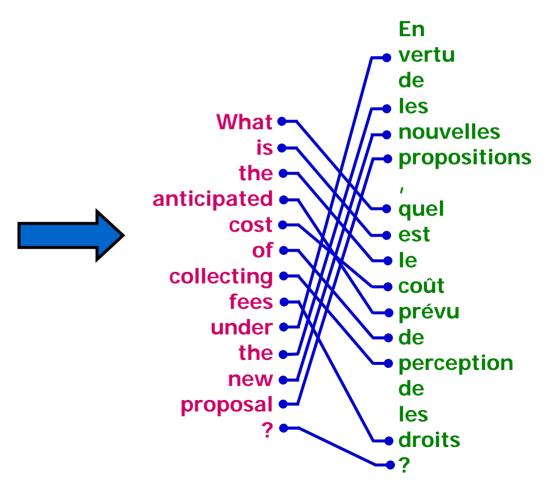


### Word-Level Correspondence

Key step in statistical machine translation systems

What is the anticipated cost of collecting fees under the new proposal?

En vertu des nouvelles propositions, quel est le coût prévu de perception des droits?





shot

[EXT. JUNGLE]

(Sawyer is walking through the jungle. He reaches a

spot. He kneels down and

one's followed him.)

looks back to check that no

### Movie/Script Correspondence



Levels of alignment Temporal:

Scene/Shot/Thread Script/closed captions

Within modalities:

**Pronoun resolution** Face tracking/recognition

**Across modalities:** 

Person/Object/Action correspondence

### Query: "walks"





[M. Everingham+al 06, Laptev+al 08]

### Learning from Ambiguous Labels

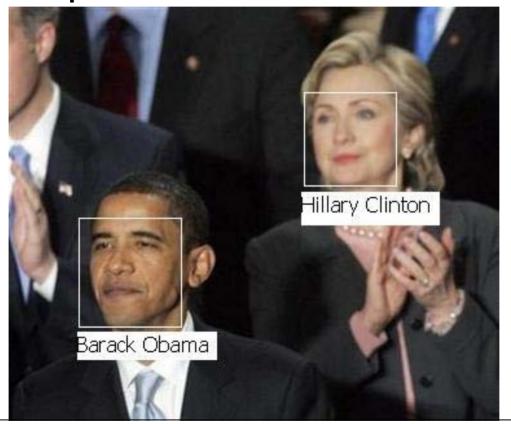
[T. Cour, B. Sapp, C. Jordan, B. Taskar, CVPR09]

Each face has two or more possible labels



#### Faces in the News

Image captions on the web



Hillary Clinton is 100% behind Barack Obama.

### **Ambiguous Labeling Setting**

- x input
- y true label ∈ {1,...,K}
- z extra label(s) ∈ {1,...,K}
- IID samples from unknown P(x,y,z)
- Ambiguous observations: (x, {y,z})



**{y,z}** Jack? Sawyer?



Jack? Sawyer?



Kate?
Jack?



Kate? Jack?



Kate? Sawyer?



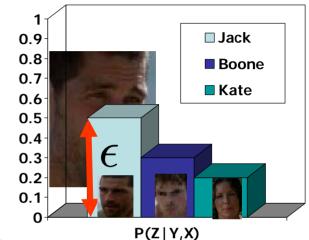
Kate? Sawyer?

[e.g., Jin+Ghahramani 02, Hullermeier+ Beringer 06]

#### Can we learn without true labels?

- No analysis (ttbomk)
- Confounders:





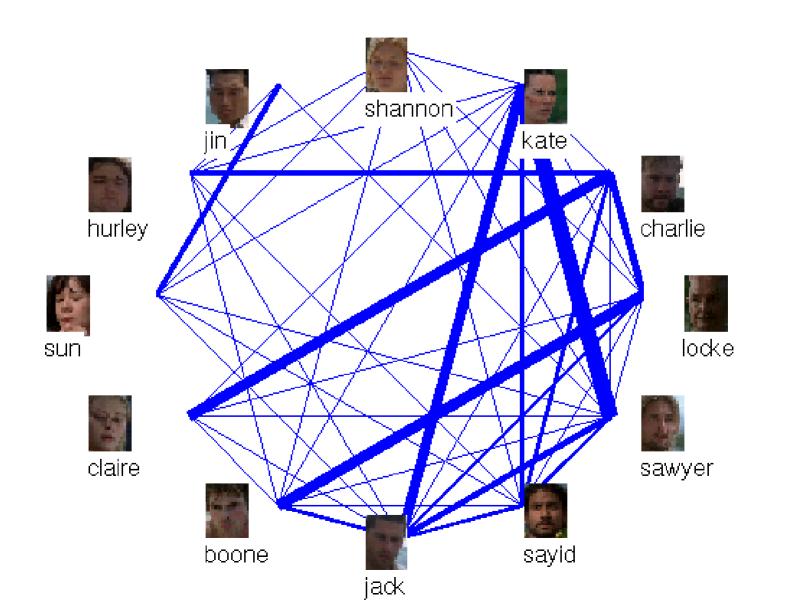
• Assumption:  $(\epsilon, \delta)$  -ambiguity P(z|y,x) is less than 1 (most of the time)

$$\epsilon = \sup_{(x,y)\in G,z} P(z\mid y,x) < 1$$

G – set of good pairs (x,y) where above holds

$$P((x,y) \in G) = 1 - \delta$$

### Ambiguity network for LOST



### Generalization from Ambiguous Samples

Error:  $\mathbf{E}[y \neq f(x)]$  Ambiguous Error:  $\mathbf{E}[y, z \neq f(x)]$ 

$$\mathbf{E}[y \neq f(x)] \ge \mathbf{E}[y, z \neq f(x)]$$

Theorem: (assuming  $(\epsilon, \delta)$ -ambiguity)

$$\mathbf{E}[y \neq f(x)] \le \frac{1}{1 - \epsilon} \mathbf{E}[y, z \neq f(x)] + \delta$$

Theorem: with probability 1 - η

$$\mathbf{E}[y \neq f(x)] \leq \frac{1}{1 - \epsilon} \left( \widehat{\mathbf{E}}_n[\operatorname{margin}(f)] + O(\sqrt{\frac{\ln(1/\eta)}{n}}) \right) + \delta$$

#### **Convex Discriminative Formulation**

- Multiclass Model:  $f(x) = \arg \max f^k(x)$ ;  $f^k(x) = w^k \cdot x$
- One-Against-All Loss:

$$\mathcal{L}(f(x), y) = \ell(f^{y}(x)) + \sum_{k \neq y} \ell(-f^{k}(x))$$

• Multilabel Loss (Waïve' Loss) 
$$\mathcal{L}(f(x), \{y, z\}) = \ell(f^y(x)) + \ell(f^y(x)) + \sum_{k \neq y}^{k \neq y} \ell(-f^k(x))$$

• Proposed Loss (tightest convex bound on ambig err):

$$\mathcal{L}(f(x), \{y, z\}) = \ell(\underbrace{f^y(x) + f^z(x)}_{\frac{1}{2} - \frac{1}{1.5} + \sum_{k \neq y, z} \ell(-f^k(x))$$

where  $\ell(\cdot)$  is standard binary loss (e.g. hinge, exp, log)

### **DVD** to Faces







frontal face detection

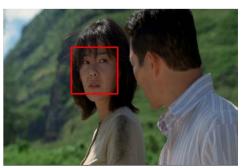


60 x 90





part detection



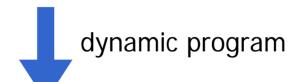


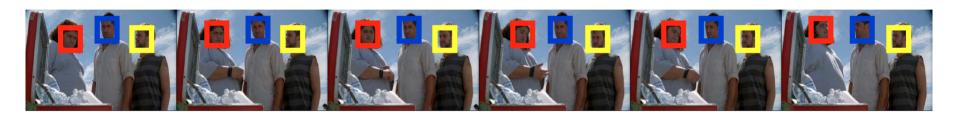


### **Tracking**



false positives false negatives overlapping detections no grouping





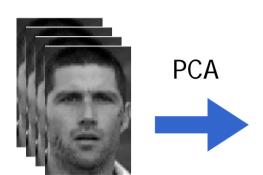


### **Face Features**

eigenfaces

mean







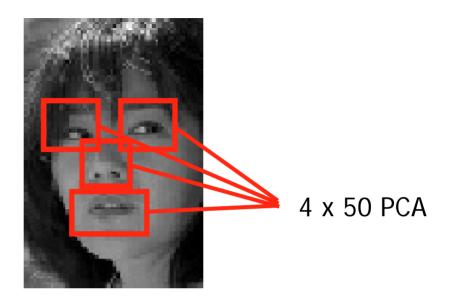
new face

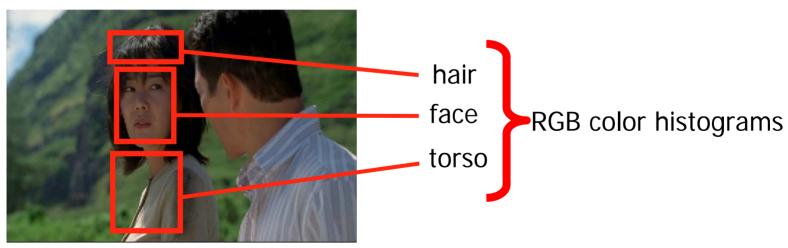




50 PCA

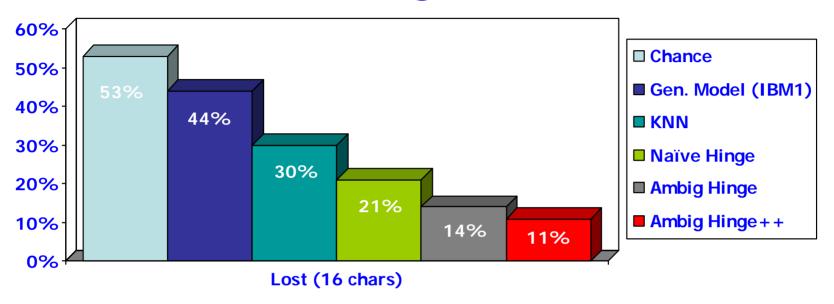
### **Additional Features**



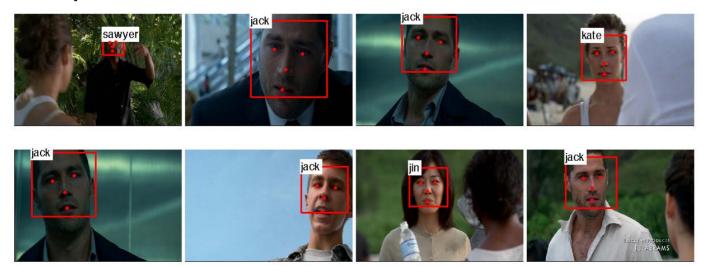


[Everingham et al., 2006] [Ramanan et al., 2007]

### Naming Error

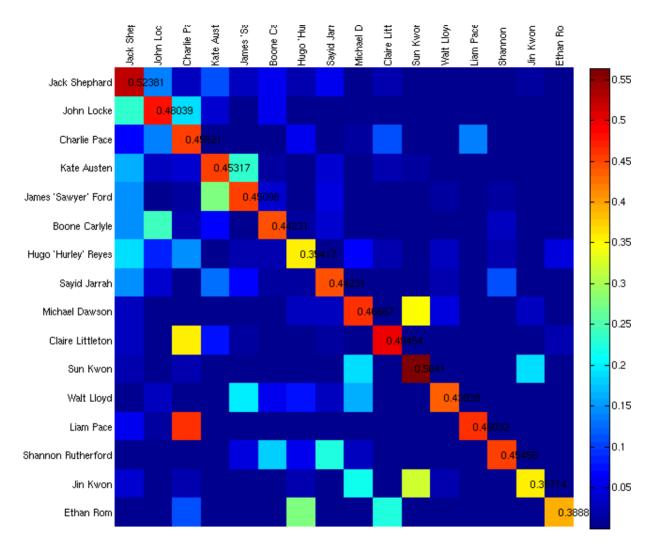


#### 8 episodes

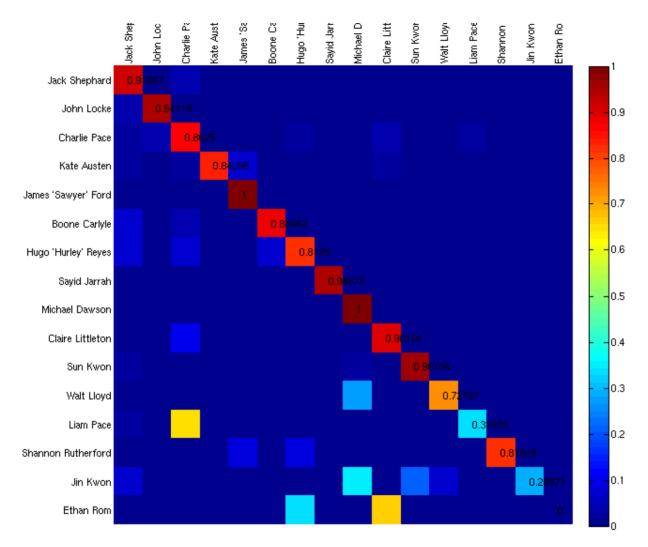


### Scenes from Lost





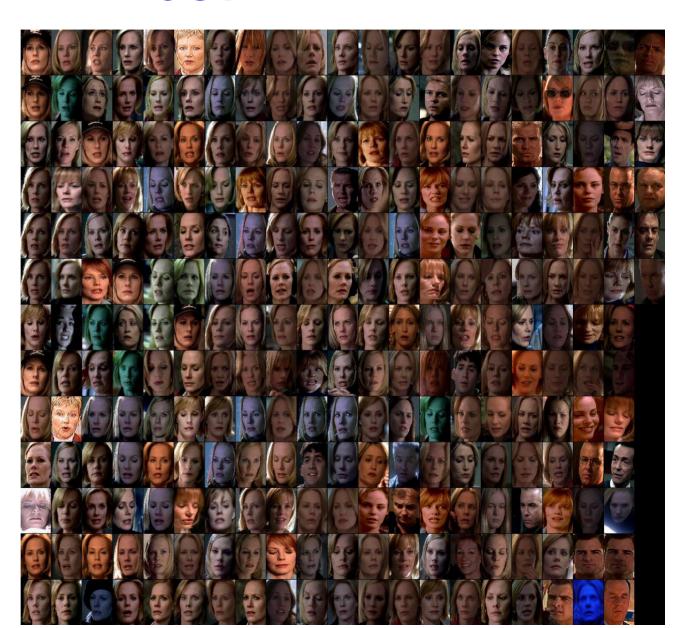
Confusion matrix of chance (row normalized) (i,j): proportion of times i was seen with j



Confusion matrix of learned model (row normalized) (i,j): proportion of times i was seen with j

### CSI

Catharine Willows Precision: 85.3

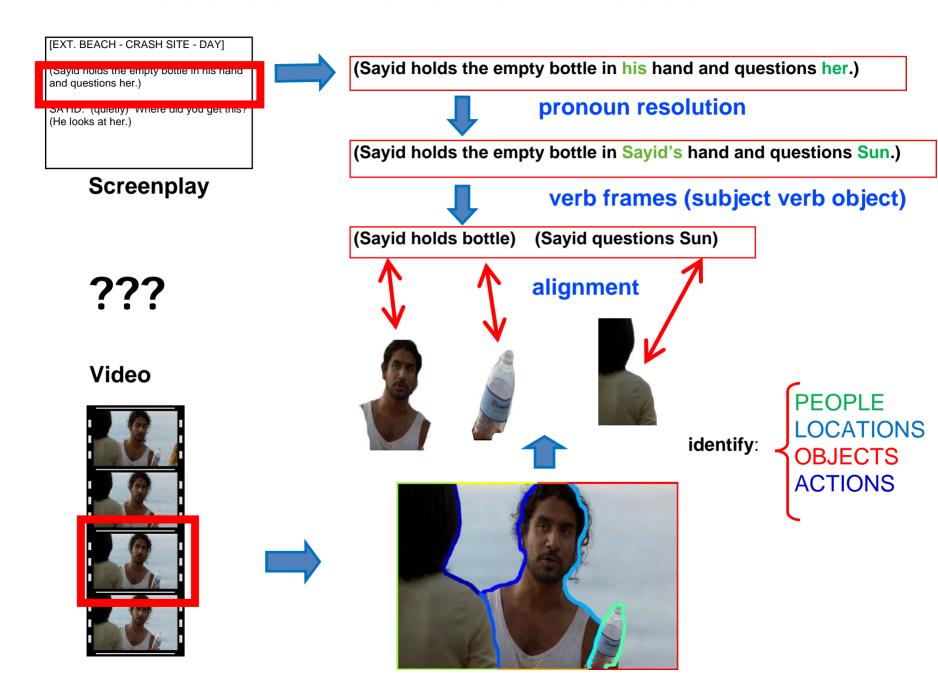


### CSI

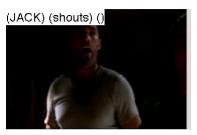
Sarah Sidle Precision: 78.3



#### Labeled Actions from Videos



#### σηουτ



### **Action Dictionary**

Precision: 90%

ωακε



φολλοω



σιτ



σμιλε



σωιμ



γραβ



κισσ



οπεν δοορ



ποιντ



[Cour +al, 08]

[Related: Laptev +al, 08]

### Body Parsing via Locally Parametric CRFs





### Naming without a screenplay

1st person reference



I'm Jack.

2<sup>nd</sup> person reference



Hey, Jack!

3<sup>nd</sup> person reference



Where is Jack?

false positive



Jack-in-the-box

Jack in scene speaking

Jack in scene

not speaking

Jack not in scene not speaking

Supervision from dialogue:

\ indirect

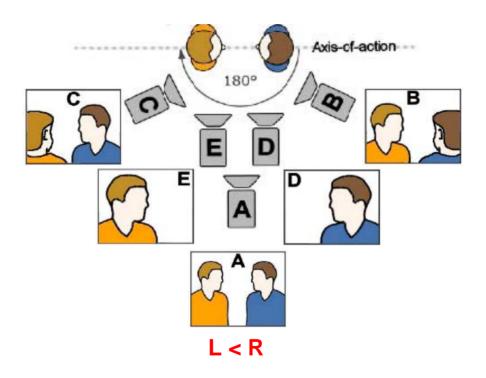
~50 references per episode only

only constraints on possible labels

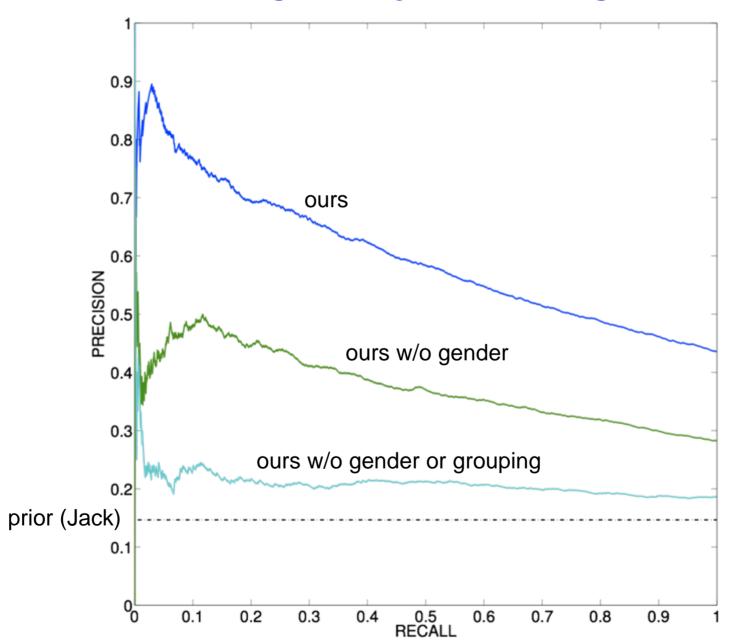
"It's Jack": 1st or 3nd person?

Grouping using continuity editing cues

## Grouping using Gestalt of Continuity Editing 180°-rule



### **Dialog-Only Naming**



### **Understanding Movies**

[With: T. Cour, B. Sapp, C, Jordan, E. Miltsakaki]

- Who, what, where, when?
  - With minimal supervision
  - Novel weak learning models and analysis

- Naming people without a screenplay
  - Dialog only: self-introductions and addresses
  - Using voices and faces, editing cues to group

- Learning articulated action models
  - Human figure parsing in videos

### Learning from Co-Occurrence

Foreign Language Lexicon

Visual Lexicon







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[EXT. BEACH - CRASH SITE]

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**SAYID** 



SUN



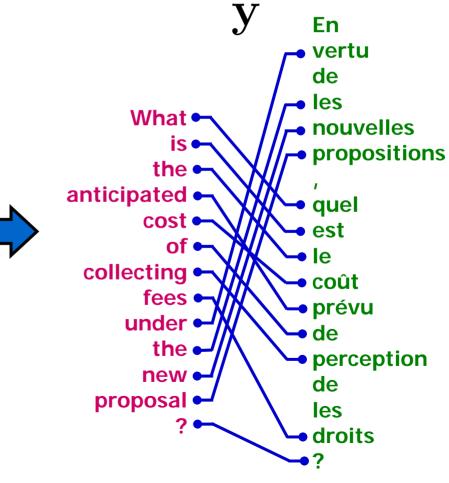
### Word Alignment

Key step in statistical machine translation systems

 $\mathbf{X}$ 

What is the anticipated cost of collecting fees under the new proposal?

En vertu des nouvelles propositions, quel est le coût prévu de perception des droits?



### Supervised Word Alignment

200 train, En/Fr	<u>AER</u>	Prec / Rec
IBM model 4 (intersected)	6.5	98 / 88%
Our Alignment Model	4.3	96 / 95%

Best published accuracy on English-French (Hansards)

[Lacoste-Julien, Taskar, Klein, Jordan 06]

### Unsupervised Alignment

Spanish, German, Finnish, Czech

No supervised data

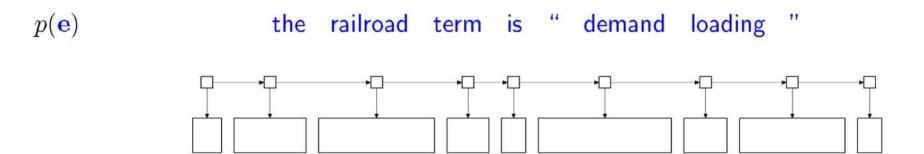
Need to learn from co-occurrence only

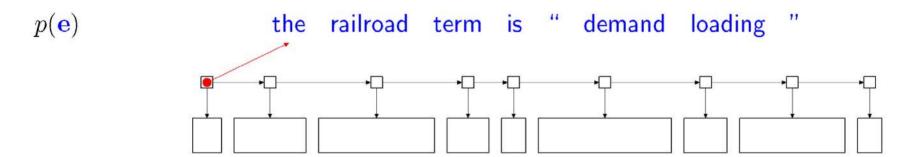
IBM Translation Models: 1-4

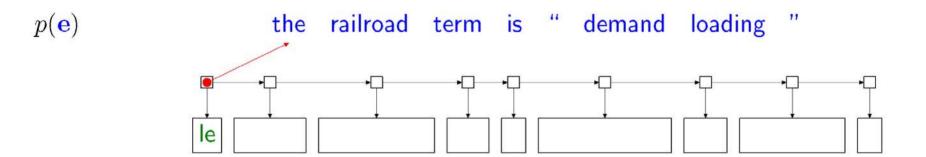
[Brown, Della Pietra, Della Pietra and Mercer, 94]

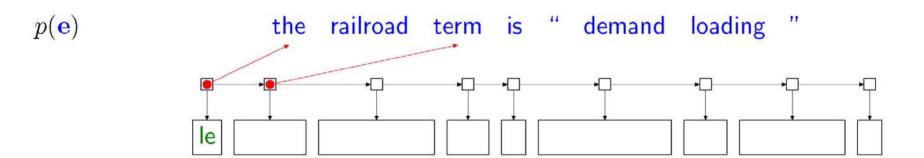
### HMM model [Ney, Vogel '96]

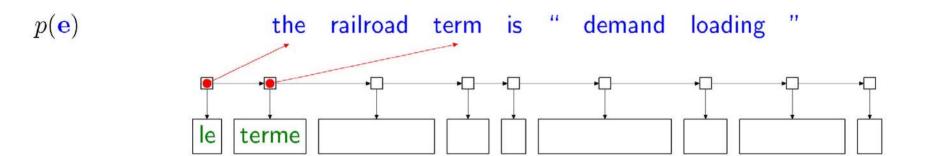
Generative model:  $p(\mathbf{a}, \mathbf{e}, \mathbf{f}; \theta)$ 



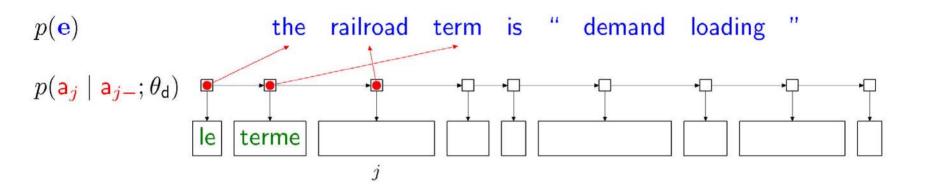








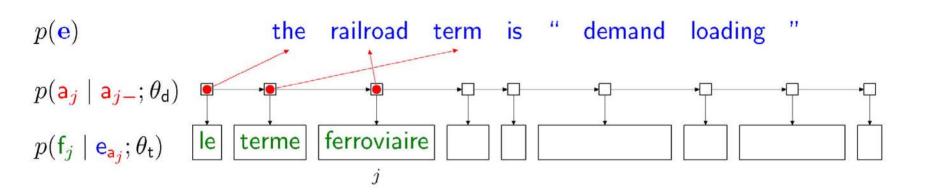
Generative model:  $p(\mathbf{a}, \mathbf{e}, \mathbf{f}; \theta)$ 



#### Distortion $\theta_d$

$$p(\uparrow \uparrow) = 0.6$$
  
 $p(\uparrow ) = 0.2$   
 $p(\searrow ) = 0.1$ 

Generative model:  $p(\mathbf{a}, \mathbf{e}, \mathbf{f}; \theta)$ 



#### Distortion $\theta_d$

$$p(\uparrow \uparrow ) = 0.6$$
  
 $p(\uparrow ) = 0.2$   
 $p(\searrow ) = 0.1$ 

#### Translation $\theta_t$

$$\begin{array}{l} p(\ \mathsf{the} \to \mathsf{le} \qquad ) = 0.53 \\ p(\ \mathsf{the} \to \mathsf{la} \qquad ) = 0.24 \\ p(\ \mathsf{railroad} \to \mathsf{ferroviaire} \,) = \mathbf{0.19} \\ p(\ \mathsf{NULL} \to \mathsf{le} \qquad ) = 0.12 \end{array}$$

Note: model not symmetric

#### EM training

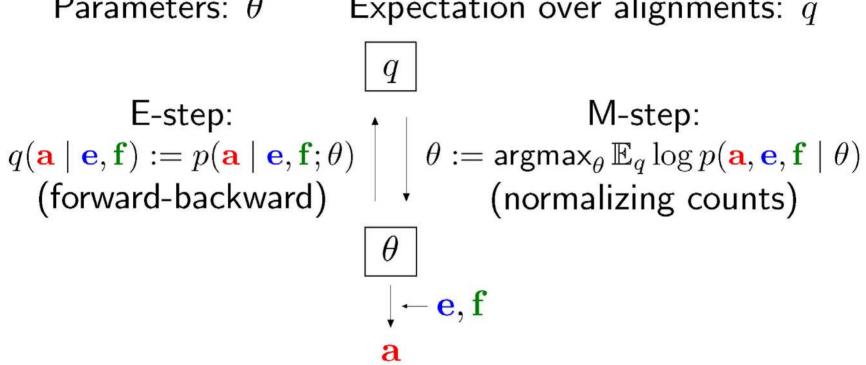
```
Maximize p(\mathbf{e}, \mathbf{f}; \theta)
      Parameters: \theta
                 E-step:
q(\mathbf{a} \mid \mathbf{e}, \mathbf{f}) := p(\mathbf{a} \mid \mathbf{e}, \mathbf{f}; \theta)
    (forward-backward)
```

#### EM training

Maximize  $p(\mathbf{e}, \mathbf{f}; \theta)$ 

Parameters:  $\theta$ 

Expectation over alignments: q

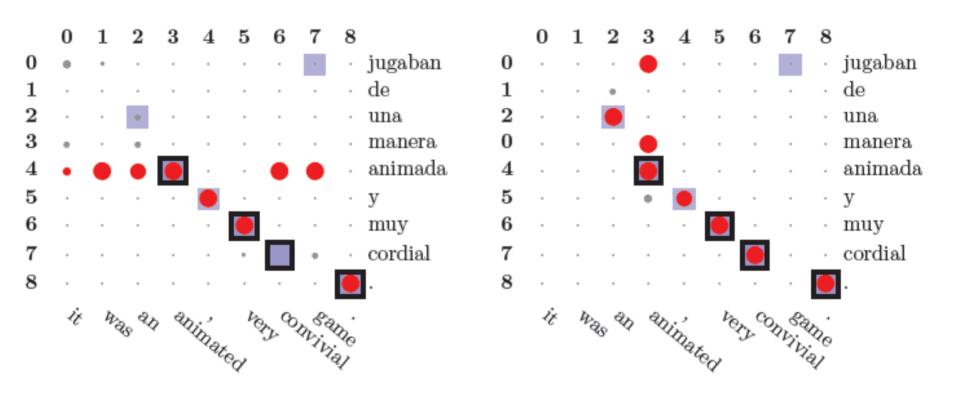


# Posterior Over Alignments

	0	1	2	3	4	5	6	7	8	
<b>0</b>										jugaban
1										de
<b>2</b>			•							una
3	•		•							manera
4	•									animada
5										y
6										muy
7						٠	0.00	•		cordial
8										
	ir	4 <sub>è</sub>	રુ ચે	20	inal	EQ .	Ç, €0,	17 Sa	De U	

Matrix dimensions							
rows	source words						
columns	target words						
Word to word posterior probabilities p							
	0.01 < p						
	$0.01 \le p < 0.05$						
	$0.05 \le p < 0.1$						
	$0.1 \le p < 0.2$						
•	$0.2 \le p < 0.3$						
•	$0.3 \le p < 0.4$						
•	$0.4 \le p < 0.5$						
•	$0.5 \le p < 0.6$						
•	$0.6 \le p < 0.7$						
•	$0.7 \le p < 0.8$						
•	$0.8 \le p < 0.9$						
•	$0.9 \le p < 0.95$						
	$0.95 \leq p$						
Alignment points							
	Sure gold alignment point						
	Possible gold alignment point						

### **Problems**



- Not 1-1 (For En/Sp/Fr/Pt 86-98% are 1-1)
- Not symmetric
- Rare words collect garbage [Moore 05]

#### Fixes?

- More complex models (IBM 4,5,6, etc.)
  - Improper distributions
  - Computing posteriors over bijective alignments is #P-complete (permanent problem)
  - Decoding with symmetric pairwise costs is NP-hard (quadratic assignment problem)

- Post-processing heuristics [Och&Ney 03]
  - Intersection of directional models plus fill-in
  - Procedural, difficult to control

# Controlling Latent Variables

Common problem in generative models:

What do latent variables represent?

- Control via additional features
  - Very indirect and unpredictable outcome
- Control via additional model structure
  - Often makes model intractable or inefficient
- For latent alignment variables, want:
  - Bijectivity
  - Symmetry
- Idea: impose control on directly on posteriors

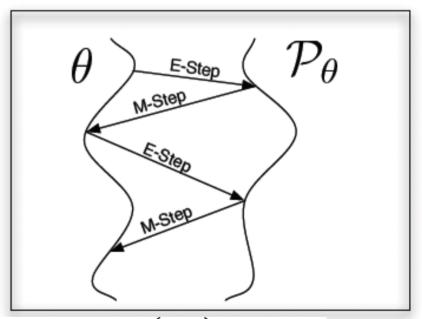
### Standard EM

- Observed: **x** Hidden: **y** Model:  $p_{\theta}(\mathbf{x}, \mathbf{y})$
- Objective:  $L(\theta) = \widehat{\mathbb{E}}_{\mathbf{x}} \log \sum_{\mathbf{y}} p_{\theta}(\mathbf{x}, \mathbf{y}) = \widehat{\mathbb{E}}_{\mathbf{x}} \log p_{\theta}(\mathbf{x})$
- E-step:

$$q_{\mathbf{x}}(\mathbf{y}) = \underset{q}{\operatorname{arg\,min}} KL(q(\mathbf{y})||p_{\theta}(\mathbf{y} \mid \mathbf{x}))$$
$$= p_{\theta}(\mathbf{y} \mid \mathbf{x})$$

• M-step:

$$\max_{\theta} \widehat{\mathbb{E}}_{\mathbf{x}} \mathbb{E}_q \log p_{\theta}(\mathbf{x}, \mathbf{y})$$



- Lower Bound:  $F(\theta,q) = \widehat{\mathbb{E}}_{\mathbf{x}} \mathbb{E}_q \log \frac{p_{\theta}(\mathbf{x},\mathbf{y})}{q_{\mathbf{x}}(\mathbf{y})} \leq L(\theta)$
- A local max of  $F(\theta,q)$  is a local max of  $L(\theta)$

#### ???

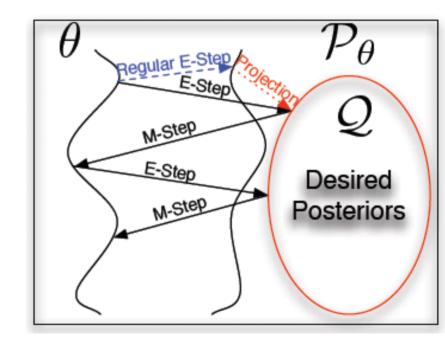
• E-step: (different)

$$q_{\mathbf{x}}(\mathbf{y}) = \operatorname*{arg\,min}_{q \in \mathcal{Q}_{\mathbf{x}}} KL(q(\mathbf{y}) || p_{\theta}(\mathbf{y} \mid \mathbf{x}))$$

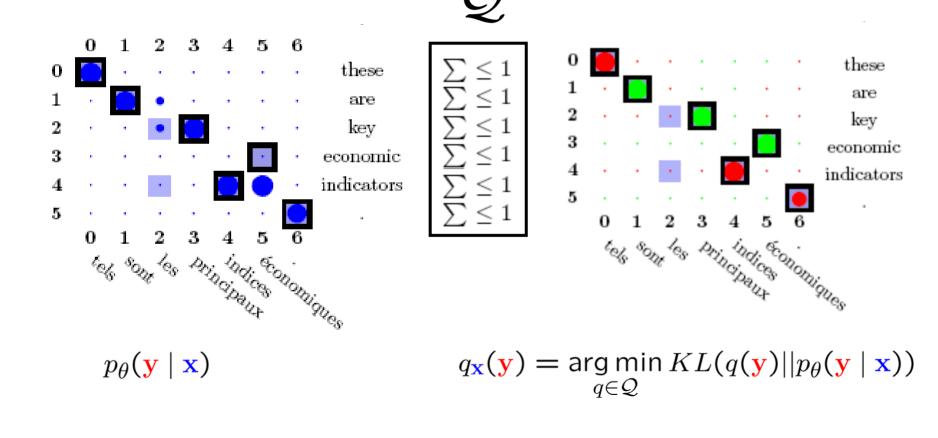
#### constraints

M-step: (same)

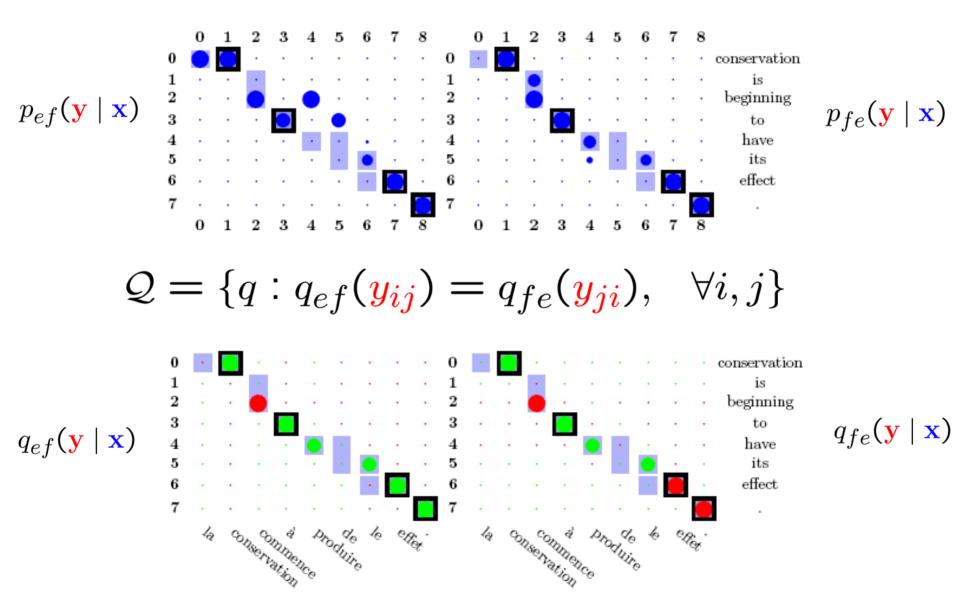
$$\max_{\theta} \widehat{\mathbb{E}}_{\mathbf{x}} \mathbb{E}_q \log p_{\theta}(\mathbf{x}, \mathbf{y})$$



# Bijectivity Constraints



### Symmetry (Agreement) Constraints



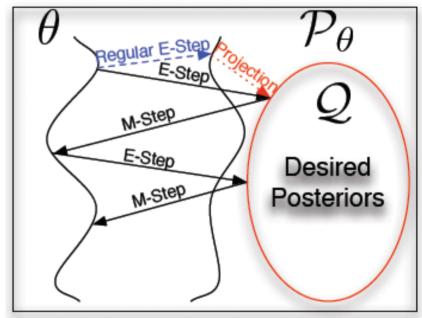
# Posterior Regularization Objective

[Graca, Ganchev, Taskar, NIPS 07]

• E-step:

• M-step:

$$\max_{\theta} \widehat{\mathbb{E}}_{\mathbf{x}} \mathbb{E}_q \log p_{\theta}(\mathbf{x}, \mathbf{y})$$



Theorem: converges to a local max of

$$L(\theta) - \widehat{\mathbb{E}}_{\mathbf{x}} KL(\mathcal{Q}_{\mathbf{x}} || p_{\theta}(\mathbf{y} \mid \mathbf{x}))$$

 $KL(\mathcal{Q}_{\mathbf{x}}||p) = \min_{q \in \mathcal{Q}_{\mathbf{x}}} KL(q||p)$  = penalty for deviation from constraints

# E-step: I-projections

If constraints are linear inequalities (or eqs)

$$Q_{\mathbf{x}} = \{q_{\mathbf{x}}(\mathbf{y}) : \mathbb{E}_q \mathbf{f}(\mathbf{x}, \mathbf{y}) \leq \mathbf{b}\}$$

- Then  $q_{\mathbf{x}}(\mathbf{y}) = \underset{q \in \mathcal{Q}_{\mathbf{x}}}{\arg \min} KL(q(\mathbf{y})||p_{\theta}(\mathbf{y} \mid \mathbf{x}))$  $\propto p_{\theta}(\mathbf{y} \mid \mathbf{x}) \exp(-\lambda \cdot \mathbf{f}(\mathbf{x}, \mathbf{y}))$
- If  $f(\mathbf{x}, \mathbf{y})$  is a sum over factors of  $p_{\theta}(\mathbf{x}, \mathbf{y})$ then  $q_{\mathbf{x}}(\mathbf{y})$  has same graphical structure, complexity
- Projection solved by gradient descent on the dual

# E-step: I-projection Dual

Dual for each example x is:

$$\min_{\lambda \geq 0} \ \lambda \cdot \mathbf{b} + \log \sum_{\mathbf{y}} p_{\theta}(\mathbf{y} \mid \mathbf{x}) \exp(-\lambda \cdot \mathbf{f}(\mathbf{x}, \mathbf{y}))$$

Gradient:

$$\mathbf{b} - \mathbb{E}_q \mathbf{f}(\mathbf{x}, \mathbf{y})$$

where

$$q_{\mathbf{x}}(\mathbf{y}) \propto p_{\theta}(\mathbf{y} \mid \mathbf{x}) \exp(-\lambda \cdot \mathbf{f}(\mathbf{x}, \mathbf{y}))$$

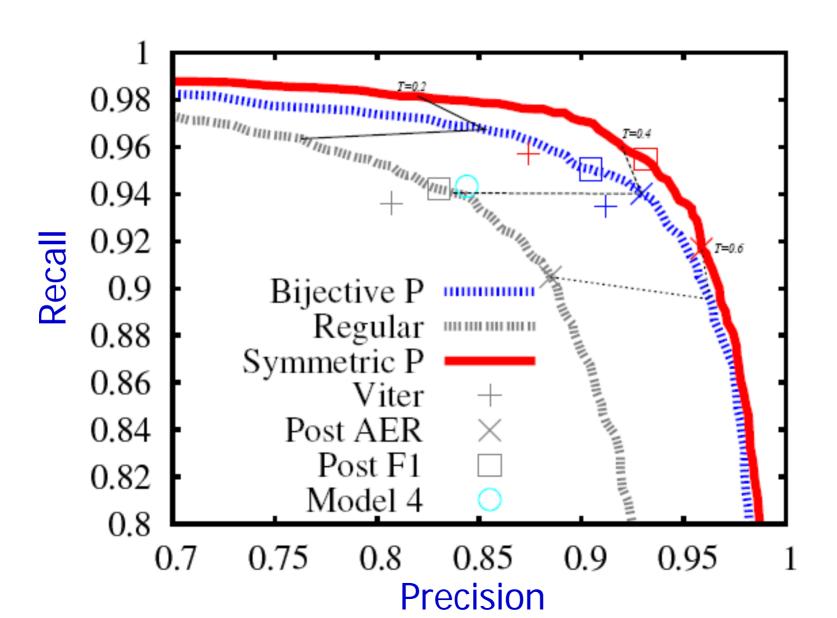
 Since projections are per example, online EM is easy

## Corpora

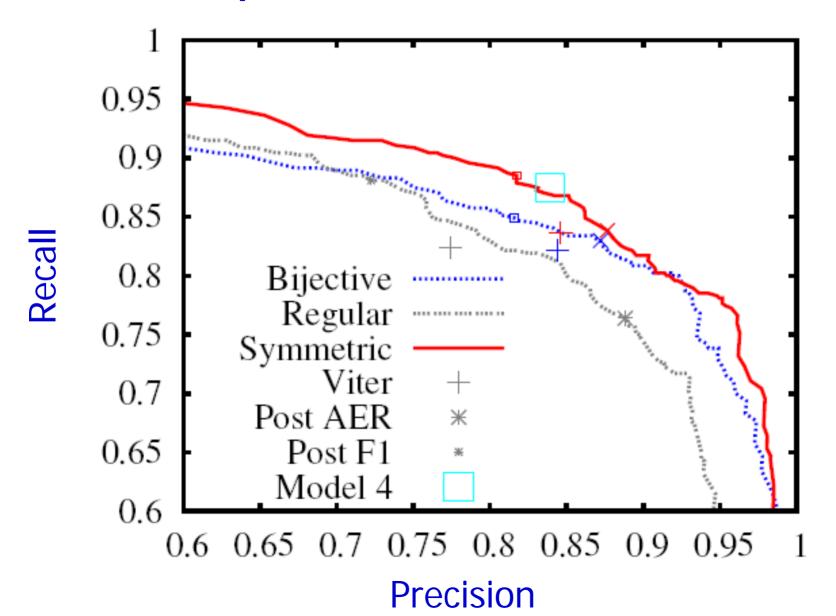
- Hansards, Europarl
- Standard dev set for tuning, test set
- En/Fr, En/Pt, En/Sp

- Metric:
  - Precision/Recall tradeoff is application-driven
  - Generate curves using posterior threshold
- Application-specific metrics:
  - Bleu for MT
  - Accuracy of bitext dependency projection

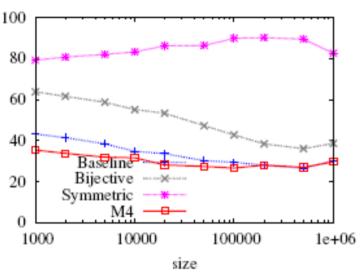
### Hansards (En/Fr, 1m sent.)



# Europarl (Pt/En, 1m sent.)



### Effect on Rare Words (at most 5)



100
80
60
80
40
20
Baseline
Bijective
Symmetric
M4
1000
10000
100000
1e+06
size

**Precision** 

Overall recall set to match Model 4

# Do better alignments help MT?

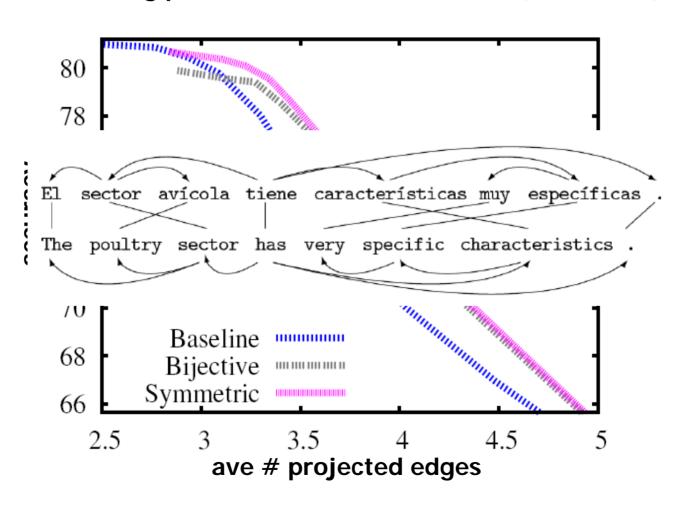
[Ganchev, Graca, Taskar, ACL 08]

- Using MOSES [Koehn+ 07]
  - Phrase-based translation decoder
  - MERT to optimize params
  - 100K sents, using standard heuristics
  - BLEU Metric [Papineni+al 02]

	Regular	Bijective	Symmetric	Model 4
Fr-En	33.42	32.74	33.52	33.12
En-Fr	26.47	26.76	26.27	26.90
Es-En	30.18	30.41	30.32	30.24
En-Es	29.89	30.36	30.27	30.09
Pt-En	28.66	29.27	28.86	28.78
En-Pt	26.59	27.09	26.89	26.90

# Alignments for Bitext Projection

Bulgarian Bitext Corpus (Tiedeman 07), using parsers trained on CONLL 07 (Nivre et al)

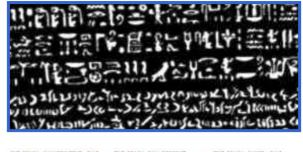


# Posterior Regularization

- Framework for exploiting prior knowledge
  - Without complicating the model
  - Simple EM+projections algorithm
  - Intuitive objective:  $L(\theta) \mathbf{E}_{\mathbf{x}} KL(\mathcal{Q}||p_{\theta}(\mathbf{y} \mid \mathbf{x}))$
- Related work
  - [Structural annealing: Smith & Eisner 04]
  - [Generalized Expectation Criteria: Mann & McCallum 08]
- Can directly enforce intractable constraints
  - Bijectivity, Agreement
  - Any linear constraint (eq/ineq) on posteriors
  - Grammar projection, other machine translation models
- Complementary to informative parameter priors

#### Correspondence across Languages and Modalities

- Words of different languages
- Faces, voices and names
- Movies and scripts
- Sound and transcription





 Towards principled, flexible framework for learning from weak supervision

### Students who did all that:



**Timothee Cour** 

Kuzman Ganchev





João Graça





With help from: Akash Nagle, Eleni Miltsakaki

