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Nabil Simaan, Kai Xu, Wei Wei, Ankur Kapoor, Peter Kazanzides, Russell Taylor and Paul Flint

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Nabil Simaan
Kai Xu
Wei Wei

Advanced Robotics and Mechanism Applications (A.R.M.A.)
Laboratory,
Department of Mechanical Engineering,
Columbia University,
New York, NY 10027,
USA
{ns2236, kx2102, ww2161}@columbia.edu

Ankur Kapoor
Peter Kazanzides
Russell Taylor

Department of Computer Science, ERC-CISST,
Johns Hopkins University,
Baltimore, MD 21218,
USA
{ankurkapoor, pkaz, rht}@jhu.edu

Paul Flint

Department of Otolaryngology, Head and Neck Surgery,
Johns Hopkins School of Medicine,
Baltimore, MD 21287,
USA
pflint@jhmi.edu

Design and Integration of a Telerobotic System for Minimally Invasive Surgery of the Throat

Abstract

In this paper we present the clinical motivation, design specifications, kinematics, statics, and actuation compensation for a newly constructed telerobotic system for Minimally Invasive Surgery (MIS) of the throat. A hybrid dual-arm telesurgical slave, with 20 joint-space Degrees-of-Freedom (DoFs), is used in this telerobotic system to provide the necessary dexterity in deep surgical fields such as the throat. The telerobotic slave uses novel continuum robots that use multiple super-elastic backbones for actuation and structural integrity. We present the kinematics of the telesurgical slave and methods for actuation compensation to cancel the effects of backlash, friction, and flexibility of the actuation lines. A method for actuation compensation

is presented in order to overcome uncertainties of modeling, friction, and backlash. This method uses a tiered hierarchy of two novel approaches of actuation compensation for remotely actuated snake-like robots. The tiered approach for actuation compensation uses compensation in both joint space and configuration space of the continuum robots. These hybrid actuation compensation schemes use intrinsic model information and external data through a recursive linear estimation algorithm and involve compensation using configuration space and joint space variables. Experimental results validate the ability of our integrated telemanipulation system through experiments of suturing and knot tying in confined spaces.

KEY WORDS—dexterity enhancement, continuum robots, telemanipulation, redundancy resolution, suturing.

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1. Introduction

Minimally invasive surgery (MIS) benefits patients with reduced trauma and healing time by providing surgeons with ac-

Table 1. Previous Literature on Distal Dexterity Enhancement

Linkages	Minor and Mukherejee (1999), Yamashita et al. (2003)	Articulated wrists	Schenker et al. (1995), Madhani et al. (1998), Guthart and Salisbury (2000), Asai et al. (2004)
Parallel wrists	Reboulet and Durand-Leguay (1999), Piers et al. (2000), Merlet (2002)	Snake-like robots	Reynaerts et al. (1999), Ikuta et al. (2003), Piers et al. (2003), Simaan et al. (2004a, b), Harada et al. (2005)

Table 2. Literature on Distal Dexterity Enhancement Listed by Medical Application

Laparoscopy/arthroscopy	Dario et al. (1997), Madhani et al. (1998), Cavusoglu et al. (2001), Yamashita et al. (2003)
Gastro-intestinal surgery	Dario et al. (1999), Reynaerts et al. (1999), Phee et al. (2002)
Microsurgery, Neurosurgery, fetal surgery	Schenker et al. (1995), Mitsuishi et al. (1997), Ikuta et al. (2003), Asai et al. (2004), Harada et al. (2005)
Needle steering	Okazawa et al. (2005), Webster et al. (2006), Sears and Dupont (2007)
Deep surgical fields	Ikuta et al. (2003), Simaan et al. (2004a, b), Kapoor et al. (2005), Simaan (2005)
Upper airways/ENT	

cess to patients' internal organs via a limited number of access ports. These access ports constrain MIS instruments to only four degrees-of-freedom (DoFs) and limit their distal dexterity. To help surgeons overcome these difficulties, a large number of robotic devices and systems have been designed for MIS. Comprehensive reviews of these systems, and others, were given by Howe and Matsuoka (1999) and Taylor and Stoianovici (2003).

Since distal dexterity of surgical tools is a necessary enabler for complex operations in MIS (e.g. intracorporeal suturing), it received considerable attention from the medical robotics research community. Table 1 lists some of the existing literature on distal dexterity enhancement in MIS. The designs of instruments for distal dexterity include planar and spatial linkages, parallel wrists, serial articulated wrists, and snake-like devices. Target clinical applications for robotically enhanced distal dexterity in MIS are listed in Table 2. These clinical applications include laparoscopy, arthroscopy, gastro-intestinal surgery, neurosurgery, fetal surgery, microsurgery, needle steering, and ear, nose, and throat (ENT) surgery.

Wrists for dexterity enhancement offered a partial solution to the distal dexterity problem and proved to be successful in laparoscopy. For example, Intuitive-Surgical offers a wide range of $\varnothing 5$ and $\varnothing 8$ mm wire-actuated wrists (*EndoWrist*[®]), based on the designs of Guthart and Salisbury (2000) and Cooper et al. (2004). These wrists provide three wrist DoFs in addition to the traditional four DoFs of MIS instruments.

Despite the large number of previous works, current robotic instruments are still too large and/or have insufficient dexterity for some clinical applications. Cavusoglu et al. (2001) showed that certain wrist designs are optimal for shallow suturing approach angles (as in thoracoscopy) while other wrist designs are suitable for steep approach angles (as in laparoscopy). Cost-Maniere et al. (2001), Adhami and Maniere (2003), and

Cannon et al. (2003) also showed that it is beneficial to optimize the location of the access ports in MIS to ensure optimal performance using existing robotic systems such as the *da Vinci* system. Faraz and Payandeh (2003), Simaan et al. (2004b), and Simaan (2005) showed that snake-like devices offer better dexterity than articulated wrists.

Clinical applications characterized by deep and narrow surgical fields are beyond the capabilities of existing commercial surgical systems owing to size and dexterity limitations. Examples of such challenging clinical applications include neurosurgery, fetal surgery, skull base surgery, and MIS of the throat and the upper airways. Of these challenging clinical applications we chose MIS of the throat since it requires dexterous operation inside the throat while using the patient's mouth as a pre-determined access port. This target clinical application shares much in common with newly arising surgical approaches such as single port surgery (less invasive surgery (LIS)) and natural orifice trans-luminal endoscopic surgery (NOTES) in which surgeons try to eliminate or reduce the number of access ports used.

In this paper we present our integrated robotic system for MIS of the throat and the upper airways. This system includes a *da Vinci* master, a stereoscopic capture and display subsystem along with our dual-arm robotic slave. The dual-arm robotic slave of this system has 20 DoFs and implements both kinematic and actuation redundancy for distal dexterity enhancement using miniature multi-segment continuum robots. Section 2 presents the driving clinical motivation, Section 3 presents the design and performance specifications for our system, Section 4 presents the system overview, Section 5 presents the kinematics of the dual-arm slave robots, Section 6 presents the statics and a novel method for actuation compensation for multi-segment continuum robots, and, finally, Section 7 presents our preliminary experience

using the first integrated telemanipulation prototype of our system.

The contribution of this paper is in presenting the kinematics of our integrated telerobotic system and a method for actuation compensation and telemanipulation of multi-segment snake-like continuum robots. This method allows successful implementation of a special mode of operation that allows suturing in extremely confined spaces and involves rotation about the backbone curve of the multi-segment continuum robots. The paper also presents the telemanipulation framework used in our system with preliminary experimental validation of the integrated telerobotic system through demonstrations of dual-arm suturing and intracorporeal knot tying in confined spaces.

2. Clinical Motivation

The upper airway is a long, narrow, and irregularly shaped organ that includes the pharynx (throat), hypopharynx, and larynx, commonly referred to as the voice box. These areas are subject to a variety of benign and malignant growths, paralysis, and scar tissue formation requiring surgical interventions for excision and/or reconstruction. These procedures (e.g. partial or total laryngectomy, vocal fold repositioning, and laryngotracheal reconstruction) are routinely performed using open surgical techniques at the expense of damaging the integrity of the framework supporting the laryngeal cartilage, muscle, and the connective tissue vital to normal function. Minimally invasive endoscopic procedures are generally preferred over open procedures, thereby preserving laryngeal framework integrity, promoting faster recovery, and frequently overcoming the need for tracheostomy. Open surgery of the larynx provides good exposure and dexterity of instrumentation; however, healthy tissue, especially the delicate framework of the larynx, is often damaged by this approach. In contrast, endoscopic laryngeal surgery utilizes natural body openings and therefore minimizes trauma.

Other than minor advancements in tooling (e.g. the powered microdebrider (Myer et al. 1999; Patel et al. 2003)), endoscopic laryngeal surgery has evolved little in the past 30 years. As seen from Figure 1, the surgery is performed using an array of long instruments (180–250 mm for laryngeal and 240–350 mm for subglottic and tracheal surgery) through a laryngoscope that is inserted into the patient's mouth and serves as a visualization tool and a guide for surgical instrumentation. Laryngologists remain restricted by the operator's distance from the surgical field, the laryngoscope's relatively small exposure, and reduced depth perception. These combine to restrict the surgeon's ability to manipulate instruments across the long distance from the oral cavity to the larynx, resulting in poor sensory feedback (both visual and tactile) and magnification of the operator tremor. While microsurgical instruments have been miniaturized, they otherwise remain unchanged. They still have long handles and lack distal dexterity,



Fig. 1. A typical surgical setup.

which often results in damage to surrounding healthy tissue and limits healing from surgical trauma in endoscopic laryngeal surgery.

Although Woo et al. (1995) and Plinkert and Lowenheim (1997) established distinct laryngeal endosuture techniques, suture repair of vocal fold wounds remains challenging and has yet to be accepted owing to technical complexities and the increased operative time required. The inability to suture such wounds results in larger scar formation. A study by Fleming et al. (2001) demonstrated a 75% larger scar area when laryngeal defects were healed with secondary intention versus primary intention. A larger scar, likely a result of unhindered collagen deposition, results in worse voice outcomes. At this time, endoscopic laryngeal surgery has reached an impasse as the lack of distal instrument mobility, complexity of suture technique, and poor three-dimensional (3D) viewing field limit surgical techniques that are routine in other surgical subspecialties. Our current work addresses these needs by developing a telerobotic system to allow surgeons to perform complex functional reconstruction tasks and suturing in MIS of the upper airway.

3. Design and Performance Specifications

The clinical task requirements drove the design and performance specifications of our robotic slave for MIS of the throat. We adopted the standard manual setup of Figure 1 in which a laryngoscope is used to access the anatomy and to support an endoscope for visualization of the surgical field. Based on the dual-arm operation observed during surgery (e.g. Figure 1), a three-armed slave robot design was conceived in which two robotic arms are used for manipulation and a third robotic arm is used for suction, Figure 2(a). The individual design of each robotic arm was guided by the specific limitations of MIS of the throat and the upper airways as shown in Figure 2(b) and (c). The narrow and long laryngoscope reduces the traditional four DoFs of minimally invasive tools to only two unconstrained DoFs (translation along and rotation about the longitudinal axis of the robotic arms). The two remaining DoFs of

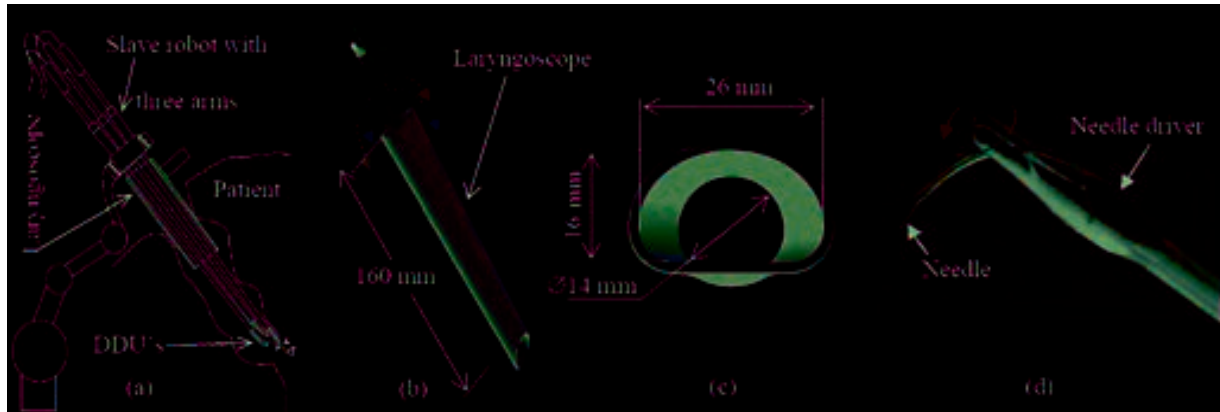


Fig. 2. (a) Our original concept for a three-armed robot with three DDUs included two robot arms for manipulation and a third arm for controllable suction. (b) A rigid instrument passing through a laryngoscope is afforded only two unconstrained DoFs out of the four DoFs of rigid tools in MIS. (c) Cross-sectional dimensions of a typical laryngoscope. (d) A semicircular needle held by a needle driver.

Table 3. Task Specifications Used in the Design of the Robotic Slaves

Reachable workspace	Orientation workspace	Maximal Speed
Ø40 mm cylinder 50 mm long located 180–250 mm axially down the throat	$\pm 90^\circ$ pitch and yaw and $\pm 180^\circ$ roll about longitudinal axis of the gripper.	Bend each snake segment $\pm 90^\circ$ in 1 second
Precision	Tool tip forces	Gripper forces
± 0.5 mm translation, $\pm 1^\circ$ in orientation.	1 N force in any direction	40 N jaw clamping force.

tilting are severely limited and provide limited motion inside the throat.

In addition to these considerations, we use the fact that surgeons use semicircular needles for suturing by using rotation about the longitudinal axis of needle drivers as shown in Figure 2(d). To achieve the task of passing the suture with minimal translation, rotation about the longitudinal axis of the gripper is desirable. Hence, our design specification for the DoFs of the distal dexterity units (DDUs) called for at least four DoFs including one DoF of rotation about the gripper's longitudinal axis.

Specifications of the desired reachable workspace were derived from the anatomical limitations of the throat, see Table 3. Other specifications of the required precision, speed, and forces were derived from *in-vivo* observations of several procedures and measurements performed using existing surgical needle drivers. The orientation workspace was specified to allow desirable distal dexterity inside the throat while delivering desirable rotation about the longitudinal axis of the gripper for suturing. The maximal gripper force was specified to ensure stabilization of triangular cross section semi circular needles such as that in Figure 2(d). This gripping force was determined experimentally using standard needle drivers. Finally, the specifications for precision were

such to allow accurate reconstruction of tissue (e.g. vocal folds).

4. System Overview

To address the challenges of MIS of the throat and upper airways, we designed and constructed the prototype telerobotic system of Figure 3. This system includes an Intuitive Surgical *da Vinci* master interface equipped with two- and three-dimensional displays, a novel high-dexterity dual arm robotic slave, and a teleoperation system capable of providing bilateral teleoperation.

The telemanipulation system shown in Figure 3 is comprised of a network of computers connected through a local area network. Each computer is connected to one robotic arm and runs an instance of the teleoperation control using an admittance-type slave robot and an impedance-type master. The control includes a low-level position servo and a high-level controller. The high-level controllers communicate with each other, and thus the state of the connected robots is available to the high-level controller. Currently the state of the other slave is used by the high-level controller for collision avoidance. A fifth computer hosts the image and display acquisition

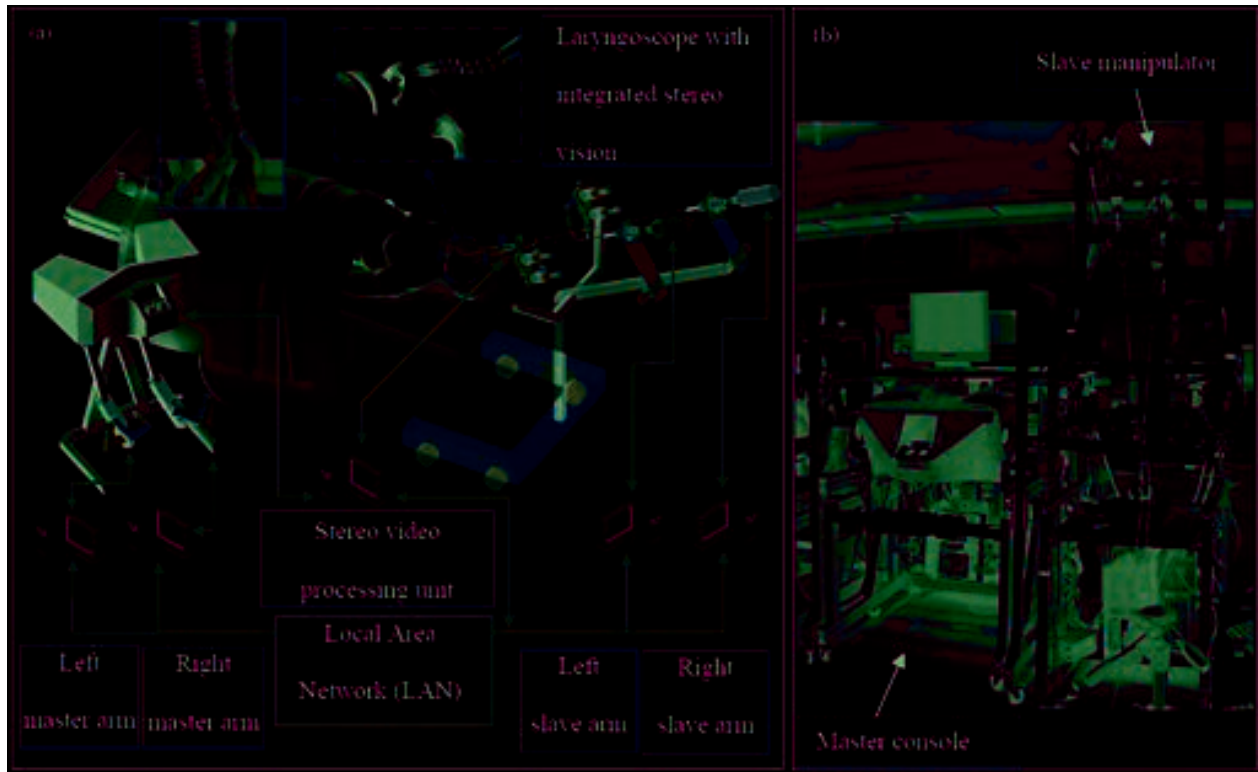


Fig. 3. (a) An outline of the telerobotic system for MIS of the throat and upper airways. (b) The system prototype.

hardware. A stereo laparoscope is connected to two image capture cards, and a dual video stream is generated for a surgeon display (a head mounted display (HMD), a two-dimensional display or a three-dimensional display can be used). Although currently no image processing is performed, our future goal is to allow the high-level controllers to incorporate information from the video processing unit. Using a separate controller for each robotic arm allows modular expansion of the system, such as addition of a third slave arm, with minimal changes to the existing system.

4.1. Dual-arm Robotic Slave for MIS of the Throat

A bi-manual design of the slave robot was chosen to enable tissue functional reconstruction operations such as suturing and intra-laryngeal knot tying, Figure 4(c). This design is a simplification of the initial three-arm concept depicted in Figure 2(a) since the function of the third suction arm in Figure 2(a) can be replaced by a flexible tube that is temporarily manipulated by one of the two remaining robot arms. The bi-manual slave robot of Figure 4(c) is composed of two similar robotic arms, two identical parallel robots (five bar mechanisms), two cylindrical actuators (z - θ stages), and a base frame.

Each robotic arm is composed of an actuation unit connected to a DDU through a flexible stem (DDU holder). Each actuation unit controls one DDU and its gripper. The DDU is used to provide the necessary dexterity inside the throat. The DDU holder is a flexible channel that serves several purposes. First, it transmits mechanical actuation to the DDU. Second, it allows remotizing the actuation units from the entry point to the laryngoscope in order to provide easy visualization of the larynx. Third, it allows the size of the actuation units to be accommodated, which when placed next to each other require an opening bigger than the opening of a laryngoscope.

The z - θ stages provide rotation about and translation along the longitudinal axis of their corresponding DDU holders. This rotation about the axis of the DDU holder is converted by the DDU into rotation about the longitudinal axis of the gripper through a special mode of operation called *rotation about the backbone*. This generalization of the operation described in Figure 2(d) is explained in detail in Section 4.2.

The five-bar parallel robots provide precise control of the DDU holder inside the laryngoscope. Although we considered using the parallel robots to manipulate the actuation units (Simaan et al. 2007), we reconfigured our experimental setup as in Figure 4(c) owing to collision problems between the moving actuation units. In the current setup the actuation units are rigidly fixed to a stationary base frame and five-bar parallel ro-

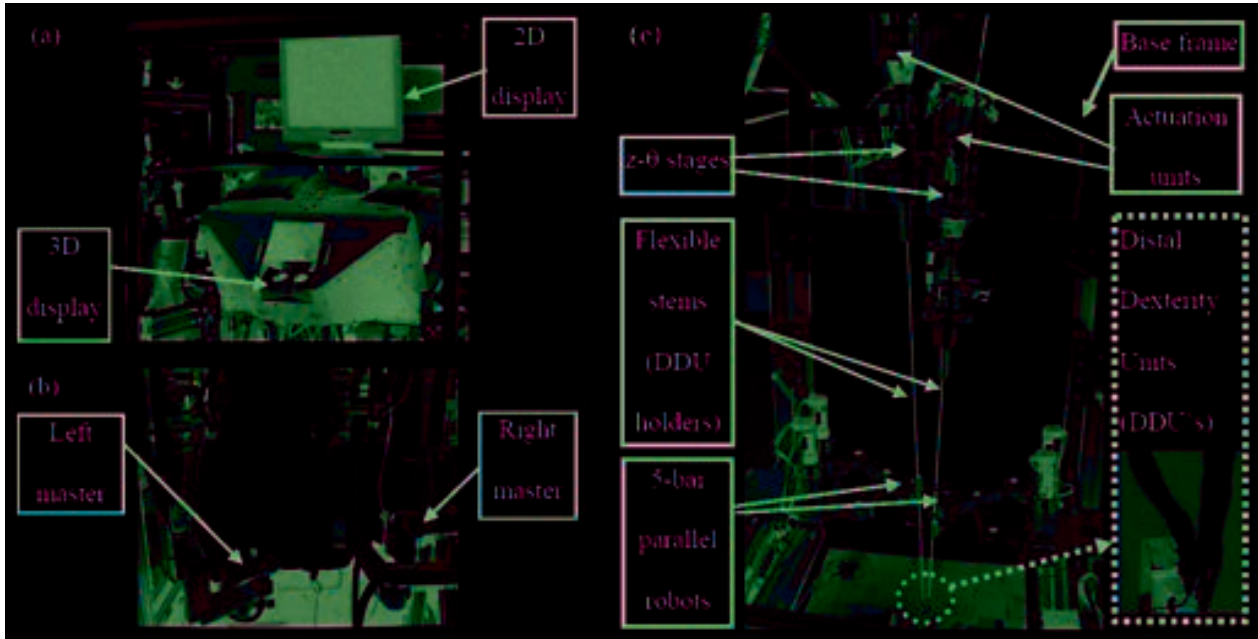


Fig. 4. (a) The user two- and three-dimensional display console. (b) The *da Vinci* master interface used in our system. (c) The dual arm slave manipulator for MIS of the throat.

bots use the flexibility of the DDU holders in order to precisely manipulate the distal ends of the DDU holders.

Each robotic arm has seven actuated joints used to control the DDU and its gripper while providing actuation redundancy to optimize the load between the actuating members of the DDU (see Section 6.1). The complete dual-arm robotic slave has 20 actuated joints that provide the necessary collision avoidance between the DDU holders while imparting six DoFs of task-space motion to each gripper. Two additional controlled joints are used for controlling end effectors (grippers, dissectors, etc.).

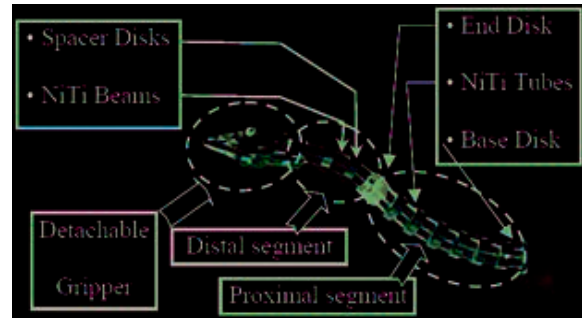


Fig. 5. The Distal Dexterity Unit (DDU)

4.2. Distal dexterity units

Figure 5 presents the Distal dexterity unit (DDU) of our system. It is composed of two flexible snake-like segments. Each segment is a flexible multi-backbone continuum robot. Earlier prototypes were composed from a single section snake-like robot and a flexible parallel robot at its tip (Simaan et al. 2004a, b, 2007). Owing to limited dexterity and manufacturing constraints, we changed our design according to the prototype shown in Figure 5.

Each snake-like segment is composed of a base disk, several spacer disks, an end disk, and four flexible super-elastic beams that we call *backbones*. The central backbone is rigidly attached to the base and the end disk of the segment, Figure 5. This backbone is called the *primary backbone*. The three other

backbones are called *secondary backbones* and they are circumferentially and equidistantly distributed around the central backbone. All secondary backbones are connected only to the end disk. The spacer disks maintain a fixed radial distance between the secondary backbones and the primary backbone. The distal segment of the DDU is similar to the proximal segment with the exception that its backbones are thin beams that pass through the tubular backbones of the proximal segment.

By actively changing the lengths of two out of the three secondary backbones, the end disk of each segment can be oriented in any direction. Instead of the minimal number of two actuated secondary backbones, three secondary backbones are actuated in each DDU segment. This allows for optimal load

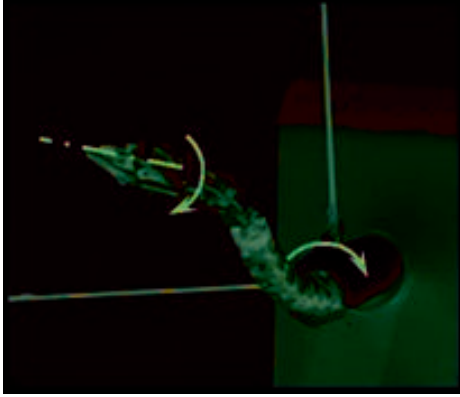


Fig. 6. The DDUs were designed to transmit rotation along their backbone.

distribution among the DDU backbones by using actuation redundancy. Also, each DDU is capable of transmitting rotation about its backbone. This *rotation about the backbone* mode of operation is demonstrated in Figure 6. The DDU of Figure 5 provides four DoFs of motion since it has two segments. The added capability of transmitting rotation about the DDU backbone allows using the rotation about and the translation along the axis of the DDU holder in Figure 4(c) to provide the gripper with six motion DoFs while enabling suturing through rotation about the longitudinal axis of the gripper in any direction within the orientation workspace of the DDU.

The advantages of this design include enhanced miniaturization and payload carrying capability. This advantage stems from the bidirectional actuation of the secondary backbones (push-pull actuation) compared with the unidirectional actuation using wires. Another advantage is backlash elimination by disposing of small pivots and gears used in articulated designs. Further advantages include MRI compatibility (since the snake is made from NiTi and the disks are from aluminum), and support of multiple modalities of use including drug/light/laser delivery through the tubes of the secondary backbones. Our slave robot is not designed to be magnetic resonance imaging (MRI) compatible, but the design of the DDUs can be adapted for potential applications requiring MRI compatibility (e.g. neurosurgery).

The push-pull actuation of the secondary backbones provides actuation redundancy that allows optimization of the load on all backbones in order to support enhanced payload carrying capability despite miniaturization. Simaan (2005) showed that different actuation redundancy schemes can reduce the compressive load on the backbones while providing improved load carrying capabilities compared with wire-actuated designs using a flexible central backbone. The current design of our snake has spacer disks 4.2 mm in diameter and a pitch diameter of 3.0 mm (the diameter of the circumference around which the secondary backbones are distributed). The

length of the proximal segment is 23 mm and the length of the distal segment is 12 mm. The diameter of the proximal segment backbones is 0.635 mm (outer diameter) and 0.508 mm (inner diameter). The diameter of the backbones of the distal segment is 0.406 mm. The minimal bending radius that corresponds to 5% strain in the super-elastic backbones is 12.7 mm for the proximal segment and 8.13 mm for the distal segment. This strain limit was established based on our experimental evaluation and recent literature on fatigue of super-elastic wires (e.g. Nemat-Nasser and Guo (2006)).

4.3. DDU Actuation Unit

Each segment of the DDU is actuated using three secondary backbones. The DDU gripper requires one additional actuated joint. Hence, we designed a compact actuation unit having seven controlled joints. Since the backbones of the distal segment of the DDU pass through the backbones of the proximal segment, a compact design that allowed actuating two coaxial backbones was required. The actuation unit is composed of three similar two-DoF actuation units that are radially arranged around one central cylinder, Figure 7. Each two-DoF actuation unit drives a pair of concentric secondary backbones. The outer backbone is the secondary backbone of the proximal segment of the DDU. The inner backbone is the secondary backbone of the distal segment of the DDU. The central cylinder is used to actuate the detachable gripper.

Each concentric backbone's two-DoF actuation unit is composed of a main cylinder and a secondary cylinder. The main cylinder controls a secondary backbone of the proximal DDU segment while the secondary cylinder controls a secondary backbone of the distal DDU segment. The secondary cylinder is carried on two carrier blocks that slide along the axis of the main cylinder. One of these carrier blocks is connected to the piston of the main cylinder through a shear pin. When the position of the main piston is controlled, the secondary cylinder is moved up and down to control the secondary backbones of the proximal segment of the DDU. The piston of the secondary cylinder is actuated independently in order to actuate the secondary backbone of the distal DDU segment.

5. Kinematics of the Dual-arm Slave Robot

This section presents the kinematics of the dual-arm slave robot of Figure 4(c). Part of these results have been presented by Simaan et al. (2004a, b) for the DDU kinematics. The overall kinematic architecture of one robotic arm of the slave robot includes serial and parallel kinematic mechanisms and flexible components.

The flexible stem of the DDU holder moves inside the limited cross section of the laryngoscope. This geometric constraint corresponds to a deflection range of less than ± 40 mm

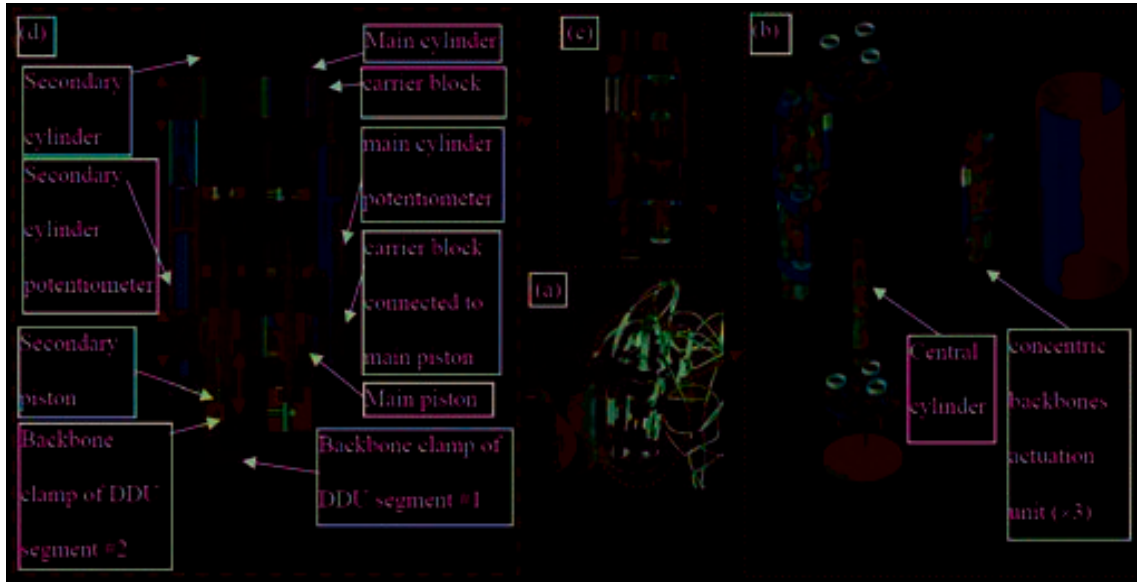


Fig. 7. A seven-DoF actuation unit for a two-section snake-like DDU with a detachable gripper: (a) the assembled prototype; (b) an exploded view; (c) actuation unit for two coaxial backbones; (d) cross section of the two-DoF actuation unit of two coaxial backbones.

over a flexible stem that is about 800 mm long. Therefore, we adopt the simplified linear beam deflection model to describe the kinematics of the flexible DDU holder.

In addition, we make an assumption that the gravitational energy of the DDU is negligible compared with its elastic energy. This assumption is further tested and justified in Section 6.1. The friction between the spacer disks and the secondary backbones is also neglected. This friction was minimized through proper design of the height of the spacer disks to minimize friction effects and to eliminate mechanical lock. Our experiments indicate that this assumption is reasonable as is evident from our ability to easily move the spacer disks axially along the central backbone of the DDU; even when the DDU is bent at a general configuration.

5.1. Kinematic Nomenclature

We use the following nomenclature throughout the paper.

- $\{A\}$ – a right handed coordinate frame with $\{\hat{x}_a, \hat{y}_a, \hat{z}_a\}$ as its associated unit vectors.
- ${}^C \mathbf{v}_{A/B}, {}^C \boldsymbol{\omega}_{A/B}$ – linear and angular velocities of frame $\{A\}$ with respect to frame $\{B\}$ expressed in frame $\{C\}$. Unless specifically stated, all vectors in this work are expressed in World Coordinate System (WCS) $\{0\}$.
- $\dot{\mathbf{a}}$ – time derivative of \mathbf{a}

- ${}^C \dot{\mathbf{x}}_{A/B}$ – twist¹ of frame $\{A\}$ with respect to frame $\{B\}$ expressed in frame $\{C\}$:

$${}^C \dot{\mathbf{x}}_{A/B} = [{}^C \mathbf{v}_{A/B}^T, {}^C \boldsymbol{\omega}_{A/B}^T]^T.$$

- ${}^A \mathbf{R}_B$ – rotation matrix of frame $\{B\}$ relative to frame $\{A\}$.
- $(\mathbf{a})^\wedge$ – skew-symmetric cross-product matrix of vector \mathbf{a} such that $\mathbf{a} \times \mathbf{b} = (\mathbf{a})^\wedge \mathbf{b}$.
- ${}^A \mathbf{p}_{ab}$ – a position vector pointing from point \mathbf{a} to point \mathbf{b} , expressed in frame $\{A\}$.
- \mathbf{J}_{xy} – a Jacobian matrix such that $[\mathbf{J}_{xy}]_{i,j} = \partial x_i / \partial y_j$.
- $\mathbf{q}_{z\theta} = [q_{z\theta_1}, q_{z\theta_2}]^T$ – the vector of joint variables for the z - θ stage (first joint is prismatic, second joint is revolute).
- $\mathbf{q}_{5bar} = [q_{5bar_1}, q_{5bar_2}]^T$ – the vector of active joint variables for the five-bar parallel robot.
- $\mathbf{q}_{s_j} = [q_{s_{j_1}}, q_{s_{j_2}}, q_{s_{j_3}}]^T$ – the vector of active joint variables for DDU segment j .

1. Throughout this paper, a twist is defined as a six-dimensional column vector with linear velocity preceding the angular velocity.

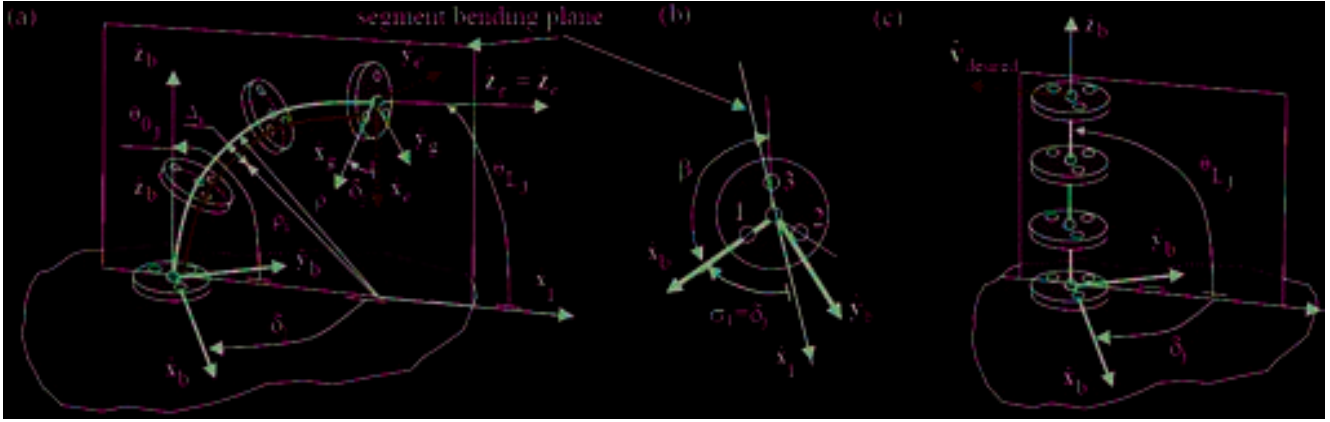


Fig. 8. Kinematic nomenclature for the j th segment of the DDU: (a) a projection of one secondary backbone and the primary backbone on the segment bending plane; (b) top view of the base disk of the DDU segment; (c) the definition of the angle δ_j at a fully extended configuration is based on the desired (commanded) linear velocity (or angular velocity) of the end disk.

- $\boldsymbol{\psi}_j = [\theta_{L_j}, \delta_j]^T$, $j = 1, 2$, represents the configuration variables of the j th segment of the DDU where θ_{L_j} is the bending angle of the j th segment of the DDU, $j = 1, 2$ and δ_j is the angle characterizing the plane in which the j th segment of the DDU bends with respect to the unit vector the central backbone with the first b, $j = 1, 2$, see Figure 8.
- θ_{0_j} – the angle of the backbone tangent in the bending plane of the j th DDU segment as shown in Figure 8:

$$\theta_{0_1} = \theta_{0_2} = \pi/2.$$
- L_j – length of the central (primary) backbone of DDU segment j , $j = 1, 2$.
- L_{s_i} – length of the secondary backbone of DDU segment, $i = 1, 2, 3$.

5.2. Kinematics of a Single DDU Segment

Figure 8 shows one segment of the DDU (we assume it is the j th segment). Since the DDU segment is a continuum robot, its shape is given by its minimal elastic and potential energy. When the secondary backbones are actuated, the snake segment bends in a plane perpendicular to the base disk of the segment. This planar bending occurs since all backbone curves remain parallel to each other and because the gravitational energy of the DDU segment is negligible (see Section 6.1 for details). The position and the orientation of the end disk of the DDU segment with respect to the base disk are therefore parameterized by two configuration variables δ_j and θ_{L_j} as defined in the nomenclature and in Figure 8.

The angular coordinate σ_i of each secondary backbone about $\hat{\mathbf{z}}_b$ is related to δ_j according to the following equation and Figure 8(b):

$$\sigma_i = \delta_j + (i - 1)\beta, \quad i = 1, 2, 3 \quad \text{where} \quad \beta = \frac{2\pi}{3}. \quad (1)$$

The radius of curvature of the central backbone is $\rho(s)$ where s is the arc length measured from the base disk. The projection of the i th secondary backbone on the segment bending plane is a curve, which is offset by $\Delta_i = r \cos(\sigma_i)$ from the primary backbone. The radius of curvature and arc-length of this curve are, respectively, $\rho_i(s_i)$ and s_i . The radius of curvature of the primary backbone is related to the radius of curvature of the i th secondary backbone according to

$$\rho(s) = \rho_i(s) + \Delta_i, \quad i = 1, 2, 3. \quad (2)$$

Using (2) yields the following result for the length of the i th secondary backbone L_{s_i} :

$$\begin{aligned} L_{s_i} &= \int ds_i = \int ds_i - ds + ds \\ &= L_j + \int_{\theta_{L_j}}^{\theta_{0_j}} (\rho_i(s) - \rho(s)) d\theta \\ &= L_j + \Delta_i(\theta_{L_j} - \theta_{0_j}) \quad \theta_{L_j} \in [0, \theta_{0_j}]. \end{aligned} \quad (3)$$

Substituting the definition of the joint value, $q_{s_{j_i}} = L_{s_i} - L_j$, into (3) yields the angle θ_{L_j} :

$$\theta_{L_j} = \theta_{0_j} + \frac{q_{s_{j_i}}}{\Delta_i}, \quad i = 1, 2, 3. \quad (4)$$

Since all of the local tangents of the backbones are always parallel to each other, one may use (4) for backbones 1 and 2 to define a kinematic compatibility condition of achieving the same θ_{L_j} as one traverses backbone 1 and backbone 2. This kinematic compatibility condition

$$\underbrace{[(L_j - L_{s1}) \cos(\beta) - (L_j - L_{s2})]}_A \cos(\delta_j) - \underbrace{[(L_j - L_{s1}) \sin(\beta)]}_B \sin(\delta_j) = 0 \quad (5)$$

also holds for any pair of secondary backbones. Equation (5) is used to solve for the angle δ_j of the segment bending plane:

$$\delta_j = \text{atan2}(A, B) \quad (\text{or another physically similar solution } \delta_j = \text{atan2}(-A, -B)) \quad (6)$$

where atan2 follows the convention $\theta = \text{atan2}(\sin(\theta), \cos(\theta))$.

For a given vector of joint values \mathbf{q}_{s_j} , the segment configuration $\boldsymbol{\psi}_j = [\theta_{L_j} \ \delta_j]^T$ is given by (4) and (6). The time derivative of (4) for $i = 1, 2, 3$ yields the Jacobian relating configuration space and joint space speeds:

$$\dot{\mathbf{q}}_{s_j} = \mathbf{J}_{q\boldsymbol{\psi}_j} \dot{\boldsymbol{\psi}}_j \quad \text{where}$$

$$\mathbf{J}_{q\boldsymbol{\psi}_j} = \begin{bmatrix} r \cos(\delta_j) & -r(\theta_{L_j} - \theta_{0_j}) \sin(\delta_j) \\ r \cos(\delta_j + \beta) & -r(\theta_{L_j} - \theta_{0_j}) \sin(\delta_j + \beta) \\ r \cos(\delta_j + 2\beta) & -r(\theta_{L_j} - \theta_{0_j}) \sin(\delta_j + 2\beta) \end{bmatrix}. \quad (7)$$

Note that $\text{rank}(\mathbf{J}_{q\boldsymbol{\psi}_j}) = 2$ in the whole configuration space.

The position, \mathbf{p}_L , and the orientation, ${}^b\mathbf{R}_e$, of the end disk with respect to the base are found by integrating along the tangent of the backbone and by a successive rotation sequence as in

$$\mathbf{p}_{L_j} = {}^b\mathbf{R}_1 \left[\int_0^{L_j} \cos(\theta(s)) ds, 0, \int_0^{L_j} \sin(\theta(s)) ds \right]^T,$$

$${}^b\mathbf{R}_e = {}^b\mathbf{R}_1 {}^1\mathbf{R}_e. \quad (8)$$

The matrix ${}^b\mathbf{R}_1$ is a rotation matrix of $(-\delta_j)$ about $\hat{\mathbf{z}}_b$ and ${}^1\mathbf{R}_e$ is a rotation matrix of $(\theta_{0_j} - \theta_{L_j})$ about $\hat{\mathbf{y}}_1$, see Figure 8.

The shape of the backbone is a function of θ_{L_j} and $\theta(s) = f(\theta_{L_j}, s)$. By taking the time derivative of this function one obtains a distribution of bending speed along the backbone as a function of the bending speed of the tip. This distribution is designated by $g(\theta_{L_j}, s)$:

$$\dot{\theta}(s) = \frac{\partial f}{\partial \theta_{L_j}} \frac{\partial \theta_{L_j}}{\partial t} + \underbrace{\frac{\partial f}{\partial s} \frac{\partial s}{\partial t}}_0 = g(\theta_{L_j}, s) \dot{\theta}_{L_j}. \quad (9)$$

Taking the time derivative of (8) results in the configuration space inverse kinematics Jacobian $\mathbf{J}_{x\boldsymbol{\psi}_j}$ where $\dot{\mathbf{x}}_j \in \mathfrak{R}^{6 \times 1}$ is the twist of the end disk of DDU segment j with respect to the center of its base disk:

$$\dot{\mathbf{x}}_j = \mathbf{J}_{x\boldsymbol{\psi}_j} \dot{\boldsymbol{\psi}}_j. \quad (10)$$

We use the approximation that the shape of the DDU at any configuration may be described by a circular segment. This approximation was validated by Xu and Simaan (2008). The bending distribution function $g(\theta_{L_j}, s)$ for a DDU that bends in a circular shape is $g(\theta_{L_j}, s) = s/L_j$. This distribution function results in the explicit expression for the Jacobian $\mathbf{J}_{x\boldsymbol{\psi}_j}$:

$$\mathbf{J}_{x\boldsymbol{\psi}_j} = \begin{bmatrix} L_j c_{\delta_j} \chi_1 & -L_j s_{\delta_j} \chi_3 \\ -L_j s_{\delta_j} \chi_1 & -L_j c_{\delta_j} \chi_3 \\ L_j \chi_2 & 0 \\ -s_{\delta_j} & c_{\delta_j} c_{\theta_{L_j}} \\ -c_{\delta_j} & -s_{\delta_j} c_{\theta_{L_j}} \\ 0 & -1 + s_{\theta_{L_j}} \end{bmatrix} \quad \text{where}$$

$$\chi_1 = \frac{(\theta_{L_j} - \theta_{0_j}) c_{\theta_{L_j}} - s_{\theta_{L_j}} + 1}{(\theta_{L_j} - \theta_{0_j})^2}$$

$$\chi_2 = \frac{(\theta_{L_j} - \theta_{0_j}) s_{\theta_{L_j}} + c_{\theta_{L_j}}}{(\theta_{L_j} - \theta_{0_j})^2}$$

$$\chi_3 = \frac{(s_{\theta_{L_j}} - 1)}{\theta_{L_j} - \theta_{0_j}}. \quad (11)$$

Equation (11) is ill-defined when $\theta_{L_j} = \theta_{0_j} = \pi/2$. This singularity is resolved by applying L'Hopital rule, as in

$$\lim_{\theta_{L_j} \rightarrow \theta_{0_j} = \frac{\pi}{2}} \mathbf{J}_{x\boldsymbol{\psi}_j} = \begin{bmatrix} -\frac{L_j}{2} c_{\delta_j} & \frac{L_j}{2} s_{\delta_j} & 0 & -s_{\delta_j} & -c_{\delta_j} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}^T. \quad (12)$$

For this configuration, the angle δ_j of the DDU segment bending plane is defined based on the unit vector $\hat{\mathbf{v}}_{desired}$ of the desired (commanded) end disk linear velocity such that $\delta_j = \text{atan2}(\hat{\mathbf{v}}_{desired}^T \hat{\mathbf{y}}_b, -\hat{\mathbf{v}}_{desired}^T \hat{\mathbf{x}}_b)$. A comparison of Figure 8(a) and (c) shows that this definition maintains consistency of δ_j as the bending angle θ_{L_j} grows from zero to $\theta_{0_j} = \pi/2$ (straight configuration).

5.3. Kinematics of One Single Robotic Arm

The kinematic nomenclature for one robotic arm of the slave robot is shown in Figure 9. The three serially attached portions

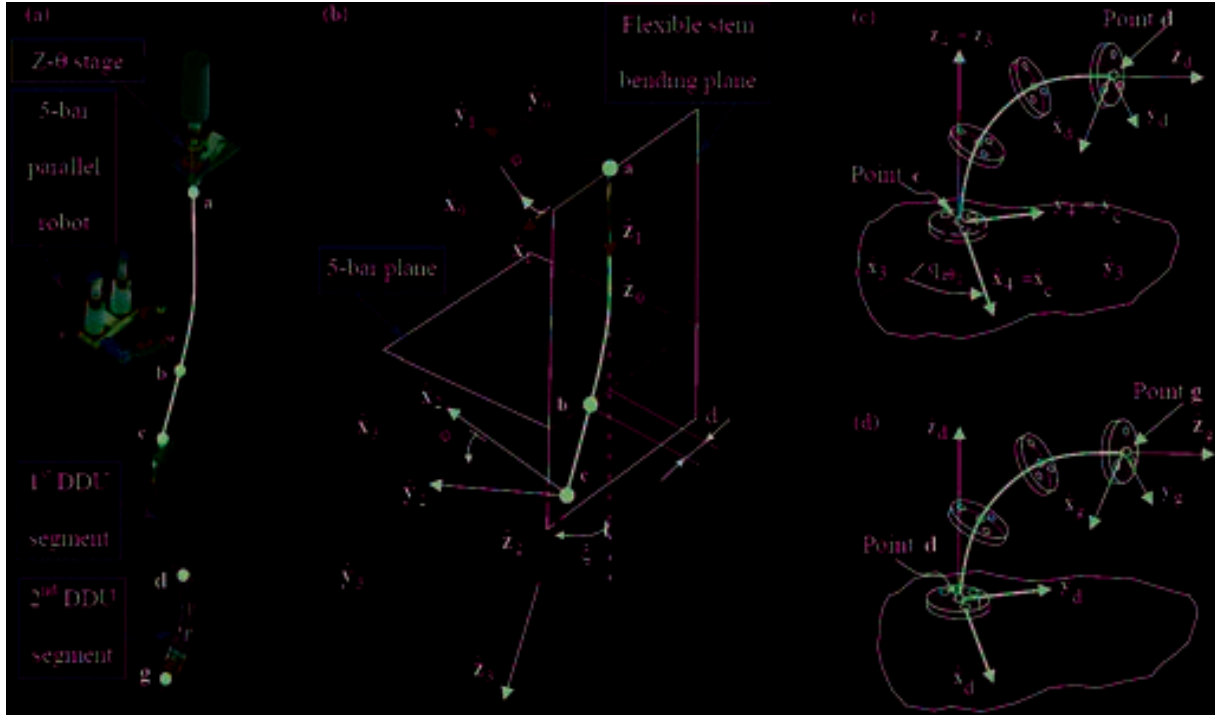


Fig. 9. Kinematic notation for a single arm of the surgical slave robot: (a) designation of points along the backbone of the arm; (b) kinematic notation for the flexible DDU stem; (c) kinematic notation for the proximal segment of the DDU; (d) kinematic notation for the distal segment of the DDU.

of the robotic arm are the flexible stem (DDU holder) and two similar snake-like segments of the DDU. The manipulation of the flexible stem is achieved by passing it through a spherical joint (point **b**) that is manipulated by a planar five-bar parallel robot. The stem has an additional DoF of sliding inside the bore of the spherical joint.

To describe the kinematics of one robotic arm an augmented vector $\dot{\mathbf{q}} = [\dot{\mathbf{q}}_{z\theta}^T, \dot{\mathbf{q}}_{5bar}^T, \dot{\boldsymbol{\psi}}_1^T, \dot{\boldsymbol{\psi}}_2^T]^T \in \mathfrak{R}^{8 \times 1}$ is defined. The kinematic derivation proceeds with solving the kinematics of the flexible stem as a function of the five-bar and the z - θ stage. It is assumed that the flexible stem is rigid enough to deliver the rotation of the z - θ stage to its distal point (point **c**). This rotation is represented in Figure 9(c) by an equivalent rotation of the base disk of the proximal segment of the DDU.

The kinematics of the five-bar parallel robot is described using its inverse kinematics Jacobian (13). The derivation of this Jacobian for parallel robots is trivial using statics or derivatives of loop closure equations (Simaan et al. 1998). For brevity this derivation is not included here. In (13) $\tilde{\mathbf{x}}_{5bar} \in \mathfrak{R}^{2 \times 1}$ designates the two-dimensional linear velocity of the end effector (point **b**) in the plane of the five-bar.

$$\dot{\mathbf{q}}_{5bar} = \mathbf{J}_{5bar} \tilde{\mathbf{x}}_{5bar}, \quad \mathbf{J}_{5bar} \in \mathfrak{R}^{2 \times 2}, \quad \tilde{\mathbf{x}}_{5bar} \in \mathfrak{R}^{2 \times 1}. \quad (13)$$

When the flexible stem is bent using the five-bar parallel robot, its shape is characterized by the angle φ defining the plane in which it bends and the deflection angle ζ at its tip, Figure 9(b). Since only a point force is applied at point **b** and the forces applied by the snake on the flexible stem are small, we neglect the deflection of **bc** since it is significantly shorter than the segment **ab**. Using the linear elastic model,

$$d = \frac{FL_{ab}^3}{3EI}, \quad \zeta = \frac{FL_{ab}^2}{2EI} \quad (14)$$

for a beam subject to load F at point **b**, we are able to find the deflection angle as a function of the linear deflection d ,

$$\zeta = \frac{3}{2} \frac{d}{L_{ab}}. \quad (15)$$

In (15), L_{ab} designates the length of the stem from point **a** to point **b**, E designates Young's modulus, and I designates the bending moment of inertia of the beam. The angle of the bending plane φ is given by the deflection of the beam²:

$$\varphi = -\text{atan2}((\mathbf{b} - \mathbf{a})^T \hat{\mathbf{y}}_0, (\mathbf{b} - \mathbf{a})^T \hat{\mathbf{x}}_0). \quad (16)$$

Three coordinate systems are defined in addition to WCS $\{0\}$, see Figure 9(b). These coordinate systems describe a rotation

2. We follow the notation $\theta = \text{atan2}(\sin(\theta), \cos(\theta))$.

sequence that provides the orientation of the tip of a bent beam without considering the rotation caused by the z - θ stage. The rotation matrices defining these frames are

$${}^0\mathbf{R}_1 = \text{Rot}(\hat{\mathbf{z}}_0, -\varphi), \tag{17}$$

$${}^1\mathbf{R}_2 = \text{Rot}(\hat{\mathbf{y}}_1, \xi), \tag{18}$$

$${}^2\mathbf{R}_3 = \text{Rot}(\hat{\mathbf{z}}_2, \varphi). \tag{19}$$

The absolute velocity of point \mathbf{b} as a function of the five-bar parallel robot kinematics (13) is described in $\{0\}$ using the components of motion in the bending plane and the component perpendicular to the bending plane (see Figure 9):

$${}^0\mathbf{v}_{b/0} = \underbrace{({}^0\hat{\mathbf{x}}_1^T \mathbf{E} \mathbf{J}_{5bar}^{-1} \dot{\mathbf{q}}_{5bar})}_{v_{\parallel}} {}^0\hat{\mathbf{x}}_1 + \underbrace{({}^0\hat{\mathbf{y}}_1^T \mathbf{E} \mathbf{J}_{5bar}^{-1} \dot{\mathbf{q}}_{5bar})}_{v_{\perp}} {}^0\hat{\mathbf{y}}_1, \tag{20}$$

$$\mathbf{E} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 0 \end{bmatrix}.$$

The velocity of point \mathbf{b} perpendicular to the bending plane is also given by $\dot{\varphi}$ as a result of the rotation of the bending plane about axis $\hat{\mathbf{z}}_0$,

$$v_{\perp} {}^0\hat{\mathbf{y}}_1 = {}^0\boldsymbol{\omega}_{1/0} \times ((\mathbf{b} - \mathbf{a})^T {}^0\hat{\mathbf{x}}_1) {}^0\hat{\mathbf{x}}_1. \tag{21}$$

Using (20) and (21) one obtains $\dot{\varphi}$ as a function of the five-bar parallel robot kinematics,

$${}^0\boldsymbol{\omega}_{1/0} = -\dot{\varphi} \hat{\mathbf{z}}_0, \tag{22}$$

$$\dot{\varphi} = \frac{-{}^0\hat{\mathbf{y}}_1^T \mathbf{E} \mathbf{J}_{5bar}^{-1} \dot{\mathbf{q}}_{5bar}}{[{}^0\hat{\mathbf{z}}_0 \times ((\mathbf{b} - \mathbf{a})^T {}^0\hat{\mathbf{x}}_1) {}^0\hat{\mathbf{x}}_1]^T {}^0\hat{\mathbf{y}}_1} = A_{\varphi} \dot{\mathbf{q}}_{5bar}. \tag{23}$$

In (23) the simplification ${}^0\hat{\mathbf{z}}_0 \times {}^0\hat{\mathbf{x}}_1 = {}^0\hat{\mathbf{y}}_1$ was used to define

$$\mathbf{A}_{\varphi} \equiv \frac{-{}^0\hat{\mathbf{y}}_1^T \mathbf{E} \mathbf{J}_{5bar}^{-1}}{d} \in \mathfrak{R}^{1 \times 2}.$$

By differentiating (15) with respect to time, one obtains the bending angle rate as a function of the five-bar robot kinematics, where $\mathbf{A}_d \equiv {}^0\hat{\mathbf{x}}_1^T \mathbf{E} \mathbf{J}_{5bar}^{-1} \in \mathfrak{R}^{1 \times 2}$:

$$\dot{\xi} = \frac{3}{2L_{ab}} \mathbf{A}_d \dot{\mathbf{q}}_{5bar}. \tag{24}$$

In obtaining (24) the deflection rate $\dot{d} = {}^0\hat{\mathbf{x}}_1^T \mathbf{E} \mathbf{J}_{5bar}^{-1} \dot{\mathbf{q}}_{5bar}$ was used. The relative velocity of point \mathbf{b} with respect to $\{1\}$ written in $\{1\}$ is only in the direction of the deflection along $\hat{\mathbf{x}}_1$,

$${}^1\mathbf{v}_{b/1} = ({}^0\hat{\mathbf{x}}_1^T \mathbf{E} \mathbf{J}_{5bar}^{-1} \dot{\mathbf{q}}_{5bar})^1 \hat{\mathbf{x}}_1 = \dot{d} {}^1\hat{\mathbf{x}}_1 \tag{25}$$

This is due to the small deflection assumption in which the movement of point \mathbf{b} in the $\hat{\mathbf{z}}_1$ is neglected. The relative angular velocity of segment \mathbf{bc} in $\{1\}$ is given by the rate of the configuration variable ξ ,

$${}^1\boldsymbol{\omega}_{bc/1} = \dot{\xi} {}^1\hat{\mathbf{y}}_1. \tag{26}$$

Using the rigid body kinematics of segment \mathbf{bc} one obtains the velocity of the tip of the flexible stem,

$${}^1\mathbf{v}_{c/1} = \dot{d} {}^1\hat{\mathbf{x}}_1 + {}^1\boldsymbol{\omega}_{bc/1} \times {}^1\mathbf{p}_{bc} = \mathbf{A}_d \dot{\mathbf{q}}_{5bar} {}^1\hat{\mathbf{x}}_1 + \frac{3}{2L_{ab}} \mathbf{A}_d \dot{\mathbf{q}}_{5bar} ({}^1\hat{\mathbf{y}}_1 \times \|\mathbf{p}_{bc}\| {}^1\mathbf{R}_2 {}^2\hat{\mathbf{z}}_2). \tag{27}$$

The absolute velocity of the tip of the flexible stem (point \mathbf{c}) is given by adding the velocity due to the rotation of $\{1\}$:

$${}^0\mathbf{v}_{c/0} = {}^0\mathbf{R}_1 {}^1\mathbf{v}_{c/1} + {}^0\boldsymbol{\omega}_{1/0} \times {}^0\mathbf{p}_{ac} = {}^0\mathbf{R}_1 {}^1\hat{\mathbf{x}}_1 \mathbf{A}_d \dot{\mathbf{q}}_{5bar} + {}^0\mathbf{R}_1 ({}^1\hat{\mathbf{y}}_1 \times {}^1\mathbf{R}_2 {}^2\hat{\mathbf{z}}_2) \frac{3 \|\mathbf{p}_{bc}\|}{2L_{ab}} \mathbf{A}_d \dot{\mathbf{q}}_{5bar} + {}^0\mathbf{p}_{ac} \times {}^0\hat{\mathbf{z}}_0 \mathbf{A}_{\varphi} \dot{\mathbf{q}}_{5bar}. \tag{28}$$

The absolute angular velocity of $\{3\}$ is given by

$${}^0\boldsymbol{\omega}_{3/0} = -\dot{\varphi} {}^0\hat{\mathbf{z}}_0 + \dot{\xi} {}^0\mathbf{R}_1 {}^1\hat{\mathbf{y}}_1 + \dot{\varphi} {}^0\mathbf{R}_2 {}^2\hat{\mathbf{z}}_2 = ({}^0\mathbf{R}_2 {}^2\hat{\mathbf{z}}_2 - {}^0\hat{\mathbf{z}}_0) \mathbf{A}_{\varphi} \dot{\mathbf{q}}_{5bar} + \frac{3}{2L_{ab}} {}^0\mathbf{R}_1 {}^1\hat{\mathbf{y}}_1 \mathbf{A}_d \dot{\mathbf{q}}_{5bar}. \tag{29}$$

Using (28) and (29) we can find the Jacobian \mathbf{J}_s relating the joint speeds of the five-bar parallel robot with the twist of point $\{3\}$. Here \mathbf{J}_{s_v} and $\mathbf{J}_{s_{\omega}}$ designate the linear and angular velocity Jacobians:

$$\dot{\mathbf{x}}_{3/0} = \begin{bmatrix} {}^0\mathbf{R}_1 {}^1\hat{\mathbf{x}}_1 \mathbf{A}_d + {}^0\mathbf{R}_1 ({}^1\hat{\mathbf{y}}_1 \times {}^1\mathbf{R}_2 {}^2\hat{\mathbf{z}}_2) \frac{3 \|\mathbf{p}_{bc}\|}{2L_{ab}} \mathbf{A}_d \\ + {}^0\mathbf{p}_{ac} \times {}^0\hat{\mathbf{z}}_0 \mathbf{A}_{\varphi} \\ ({}^0\mathbf{R}_2 {}^2\hat{\mathbf{z}}_2 - {}^0\hat{\mathbf{z}}_0) \mathbf{A}_{\varphi} + \frac{3}{2L_{ab}} {}^0\mathbf{R}_1 {}^1\hat{\mathbf{y}}_1 \mathbf{A}_d \end{bmatrix} \dot{\mathbf{q}}_{5bar} = \underbrace{\begin{bmatrix} \mathbf{J}_{s_v} \\ \mathbf{J}_{s_{\omega}} \end{bmatrix}}_{\mathbf{J}_s} \dot{\mathbf{q}}_{5bar}, \quad \mathbf{J}_{s_v}, \mathbf{J}_{s_{\omega}} \in \mathfrak{R}^{3 \times 2}. \tag{30}$$

The z - θ stage contributes to the twist of the flexible stem by providing axial speed $\dot{q}_{z\theta_1}$ along and angular speed $\dot{q}_{z\theta_2}$ about $\hat{\mathbf{z}}_2$. To capture this we define frame $\{4\}$ using a simple translation $q_{z\theta_1}$ and rotation $q_{z\theta_2}$ about and along $\hat{\mathbf{z}}_3$. We also assume that the base disk of the proximal DDU segment is attached to the flexible stem such that $\{4\} = \{c\}$. The Jacobian relating the

contribution of the joint speeds of the z - θ stage to the twist of the flexible stem is

$$\mathbf{J}_{z\theta} = \begin{bmatrix} \mathbf{J}_{z\theta v} \\ \mathbf{J}_{z\theta\omega} \end{bmatrix} = \begin{bmatrix} {}^0\mathbf{R}_2 {}^2\hat{\mathbf{z}}_2 & \mathbf{0}_{3 \times 1} \\ \mathbf{0}_{3 \times 1} & {}^0\mathbf{R}_2 {}^2\hat{\mathbf{z}}_2 \end{bmatrix}. \quad (31)$$

Superimposing the twist generated by the z - θ stage with the twist caused by the five-bar mechanism we obtain the kinematic model for the twist of the distal end of the flexible stem as it is described in terms of the kinematics of the five-bar and the z - θ stage,

$${}^0\dot{\mathbf{x}}_{c/0} = \underbrace{\begin{bmatrix} \mathbf{J}_{z\theta v} & \mathbf{J}_{sv} \\ \mathbf{J}_{z\theta\omega} & \mathbf{J}_{s\omega} \end{bmatrix}}_{\mathbf{J}_f} \begin{bmatrix} \dot{\mathbf{q}}_{z\theta} \\ \dot{\mathbf{q}}_{5bar} \end{bmatrix}, \quad \mathbf{J}_f \in \mathfrak{R}^{6 \times 4}. \quad (32)$$

Two-dimensional configuration vectors $\dot{\boldsymbol{\psi}}_j = [\theta_{Lj}, \delta_j]^T$ are used to describe the kinematics of the j th segment of the DDU as defined in Section 5.2,

$$\begin{aligned} {}^c\dot{\mathbf{x}}_{d/c} &= \mathbf{J}_{x\psi_1} \dot{\boldsymbol{\psi}}_1, & {}^d\dot{\mathbf{x}}_{g/d} &= \mathbf{J}_{x\psi_2} \dot{\boldsymbol{\psi}}_2, \\ \mathbf{J}_{x\psi_1}, \mathbf{J}_{x\psi_2} &\in \mathfrak{R}^{6 \times 2}. \end{aligned} \quad (33)$$

Using the twist transformations to account for the translation and rotation from the base of the distal DDU segment (point \mathbf{d}) to the gripper (point \mathbf{g}) one obtains the relative twist of the gripper with respect to the end point of the flexible stem,

$${}^c\dot{\mathbf{x}}_{g/c} = \mathbf{S}_1 {}^c\dot{\mathbf{x}}_{d/c} + \mathbf{S}_2 {}^d\dot{\mathbf{x}}_{g/d}, \quad (34)$$

where \mathbf{S}_1 and \mathbf{S}_2 are twist transformation matrices given in

$$\mathbf{S}_1 = \begin{bmatrix} \mathbf{I} & {}^c\mathbf{R}_d ({}^d\mathbf{p}_{gd})^\wedge \\ \mathbf{0} & \mathbf{I} \end{bmatrix}, \quad \mathbf{S}_2 = \begin{bmatrix} {}^c\mathbf{R}_d & \mathbf{0} \\ \mathbf{0} & {}^c\mathbf{R}_d \end{bmatrix}. \quad (35)$$

The absolute twist of the gripper in $\{0\}$ is given by superimposing the relative twist in (34) with the twist of the flexible stem (32), while accounting for the necessary twist transformations \mathbf{S}_3 and \mathbf{S}_4 ,

$${}^0\dot{\mathbf{x}}_{g/0} = \mathbf{S}_3 {}^0\dot{\mathbf{x}}_{c/0} + \mathbf{S}_4 {}^c\dot{\mathbf{x}}_{g/c}, \quad (36)$$

$$\mathbf{S}_3 = \begin{bmatrix} \mathbf{I} & {}^0\mathbf{R}_c ({}^c\mathbf{p}_{gc})^\wedge \\ \mathbf{0} & \mathbf{I} \end{bmatrix}, \quad \mathbf{S}_4 = \begin{bmatrix} {}^0\mathbf{R}_c & \mathbf{0} \\ \mathbf{0} & {}^0\mathbf{R}_c \end{bmatrix}. \quad (37)$$

Equations (32), (33), (34) are used to derive the overall kinematics Jacobian \mathbf{J}_{arm} of a single robotic arm:

$$\begin{aligned} {}^0\dot{\mathbf{x}}_{g/0} &= \underbrace{[\mathbf{S}_3 \mathbf{J}_f \mid \mathbf{S}_4 \mathbf{S}_1 \mathbf{J}_{x\psi_1} \mid \mathbf{S}_4 \mathbf{S}_2 \mathbf{J}_{x\psi_2}]}_{\mathbf{J}_{arm}} \dot{\mathbf{q}}, \\ \mathbf{J}_{arm} &\in \mathfrak{R}^{6 \times 8}. \end{aligned} \quad (38)$$

Equation (38) defines the inverse kinematics of a single robotic arm in terms of the augmented vector $\dot{\mathbf{q}} = [\dot{\mathbf{q}}_{z\theta}^T, \dot{\mathbf{q}}_{5bar}^T, \dot{\boldsymbol{\psi}}_1^T, \dot{\boldsymbol{\psi}}_2^T]^T \in \mathfrak{R}^{8 \times 1}$. The solution for individual joint speeds is obtained through kinematic redundancy resolution

$$\dot{\mathbf{q}} = (\mathbf{J}_{arm})^+ {}^0\dot{\mathbf{x}}_{g/0} + (\mathbf{I} - (\mathbf{J}_{arm})^+ (\mathbf{J}_{arm})) \mathbf{h}. \quad (39)$$

The null space vector \mathbf{h} can be used to satisfy obstacle avoidance or to maximize dexterity (Kapoor et al. 2005). In (39) $(\mathbf{J}_{arm})^+$ designates the generalized inverse. While other methods for obtaining redundancy resolution for (38) exist, we use the pseudo-inverse method. Our experience as indicated in Section 7 suggests that this method works quite well for our application.

Each DDU segment has a Jacobian relating its joint rates (the backbone lengths) with the rates of its configuration variables (Simaan et al. 2004a). Once (38) is solved, the joint rates \dot{q}_j of each DDU segment ($j = 1, 2$) are calculated using (7).

6. Actuation Compensation

Figure 9 introduced a desirable mode of operation of the DDU for suturing in confined spaces. We called this mode of operation *rotation about the backbone*. During this mode of operation, the desired configuration variables δ_j , $j = 1, 2$, must be precisely changed at the same rotation rate of the z - θ stage (Simaan 2005). To support rotation about the backbone, precise coordination of all actuation joints controlling the configuration vectors $\boldsymbol{\psi}_j$ ($j = 1..2$) of each DDU segment is essential to prevent the gripper wobbling.

Despite its advantages mentioned in Section 4.2, the design of the DDU presents several challenges. The long and flexible backbones introduce modeling uncertainties that include friction and flexibility in the actuation lines. Regardless of the method used to actuate the DDU (either using wire actuation or push-pull actuation), it is necessary to compensate for modeling uncertainties since there is no direct means to measure and provide closed loop control on the configuration vectors $\boldsymbol{\psi}_j$ of the DDU segments. Instead, position control is carried out in joint space.

Each backbone connects to the actuation unit by passing through the long flexible stem of the DDU holder and dedicated channels in the actuation cone, Figure 10. Bending each segment of the DDU requires significant actuation forces that produce a significant axial extension along the long actuation path between the DDU and the actuation unit. To obtain the desired configuration $\boldsymbol{\psi}_j$ of each DDU segment, the commanded joint vectors \mathbf{q}_j must be corrected using an actuation compensation vector $\boldsymbol{\epsilon}_k$ that accounts for the backbone extension, friction, and backlash. Since actuation errors in the proximal segment directly affect the length of the backbones of the distal

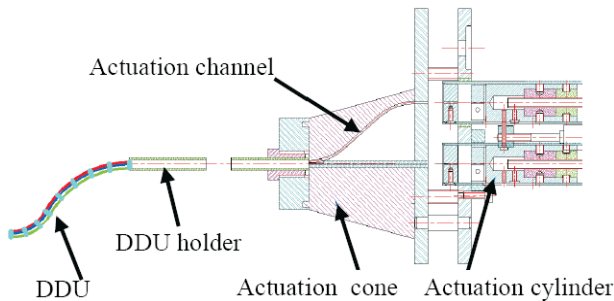


Fig. 10. A schematic of the snake-like unit and its actuation unit.

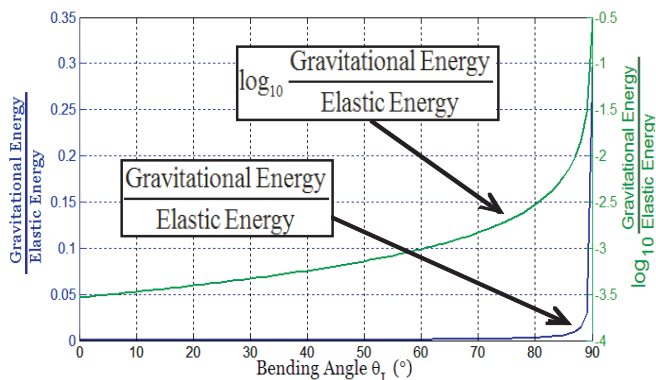


Fig. 11. Gravitational energy over the elastic energy ratio.

segment, the following equation is used for the actuation compensation model:

$$\tilde{\mathbf{q}}_j = \mathbf{q}_j + \sum_{k=1}^j \boldsymbol{\varepsilon}_k, \quad j = 1, 2. \quad (40)$$

Determining the actuation compensation vectors $\boldsymbol{\varepsilon}_1$ and $\boldsymbol{\varepsilon}_2$ may be carried out based on estimation schemes in joint space \mathbf{q}_j or in configuration space $\boldsymbol{\psi}_j$. Xu and Simaan (2006) presented actuation compensation methods for a single DDU segment using model-based and combined model-based with recursive linear squares estimation methods. The following sections extend these results and provide joint-space and configuration-space compensation algorithms for multiple segment DDUs. The choice of what compensation algorithm to use depends on the availability of external data (e.g. visual tracking of the gripper) to update the recursive estimation approaches that use $\boldsymbol{\psi}_j$ in the process.

6.1. Statics Modeling

The static analysis of the DDU is derived using the virtual work model. Twisting of backbones and the friction between

spacer disk and the secondary backbones are neglected. Each snake-like unit in Figure 5 weighs 6.72 g. Given the circular bending shape of the DDU segments, the ratio of gravitational energy to elastic energy as a function of the bending angle $\theta_L = \theta_{L1} = \theta_{L2}$ is plotted in Figure 11. The elastic energy of the j th DDU segment is calculated based on the elastic bending energy of all of the backbones,

$$U_j = \int_L \frac{EI}{2} \left(\frac{d\theta}{ds} \right)^2 ds$$

$$= (\theta_{Lj} - \theta_{0j})^2 \left(\frac{E_p I_p}{2L} + \sum_{i=1}^3 \left(\frac{E_s I_s}{2L_i} \right) \right). \quad (41)$$

Even when the robot is only bent to $\theta_L = \theta_{L1} = \theta_{L2} = 87^\circ$ this ratio is as small as 0.0099 (0.99%). Hence, gravity is neglected in the analysis. In (41) E denotes Young’s modulus of the super-elastic NiTi backbones, I_p and I_s are the bending cross-sectional moment of inertia of the primary and the secondary backbones, L is the length of the primary backbone, L_i is the length of the i th backbone. The required actuation forces, $\boldsymbol{\tau}_j$, were found by Simaan (2005) using the virtual work principle, which results in the static equilibrium condition

$$\mathbf{J}_{q\boldsymbol{\psi}_j}^T \boldsymbol{\tau}_j + \mathbf{J}_{x\boldsymbol{\psi}_j}^T \mathbf{W}_e = \nabla U_j. \quad (42)$$

In (42), \mathbf{W}_e is the wrench acting on the end disk. These equations constitute two equations with a vector of three unknowns $\boldsymbol{\tau}_j$. The vector $\boldsymbol{\tau}_j$ is found using the solution

$$\boldsymbol{\tau}_j = \left(\mathbf{J}_{q\boldsymbol{\psi}_j}^T \right)^+ \left(\nabla U_j - \mathbf{J}_{x\boldsymbol{\psi}_j}^T \mathbf{W}_e \right) + \left(\mathbf{I} - \left(\mathbf{J}_{q\boldsymbol{\psi}_j}^T \right)^+ \mathbf{J}_{q\boldsymbol{\psi}_j}^T \right) \mathbf{h}_\tau. \quad (43)$$

$\mathbf{h}_\tau \in \mathfrak{R}^{3 \times 1}$ is a vector of homogeneous actuation forces used to optimize the loads on the backbones.

The vector of joint actuation forces $\boldsymbol{\tau}_j$ is important for determining the required actuation compensation owing to the backbone flexibility. Without loss of generality and for simplicity, we assume that $\mathbf{h}_\tau = \mathbf{0} \in \mathfrak{R}^{3 \times 1}$, i.e. we use the minimum-norm redundancy resolution for the following sections dealing with the actuation compensation methods.

6.2. Actuation Compensation in Joint-space

The model of backbones of segment j of the DDU includes two portions, Figure 10. The first portion is along the DDU holder and it is subject to forces vector $\boldsymbol{\tau}_j \in \mathfrak{R}^{3 \times 1}$ that is determined based on the static model in (43). The second portion is along the actuation channel in the DDU actuation cone and it is subject to the force $\boldsymbol{\tau}_j + \mathbf{f}_j$ where \mathbf{f}_j designates the vector of

friction forces in the actuation channels of the DDU actuation cone. The model for \mathbf{f}_j

$$\mathbf{f}_j = (\boldsymbol{\tau}_j + \mathbf{f}_{s,j}) e^{2\mu\phi} \quad (44)$$

is based on the resemblance of a bent backbone passing through an actuation channel in the DDU cone to the model of a band brake (Juvinal and Marshek 2003). In (44), ϕ represents the contact angle along the actuation channel, μ is the coefficient of coulomb friction, and $\mathbf{f}_{s,j}$ is the vector of static friction forces that results from bending the backbone along the curvature of the actuation channels. The values of ϕ , μ , and $\mathbf{f}_{s,j}$ were determined by Xu and Simaan (2006).

The stiffness matrices representing the first and second portion of each backbone in the j th segment of the DDU are respectively designated by $\mathbf{K}_{s,j}$ and $\mathbf{K}_{c,j}$, $j = 1, 2$. These matrices are given by the linear elastic model of the backbones,

$$\begin{aligned} \mathbf{K}_{c,j} &= E_{s,j} A_{s,j} / L_c \cdot \text{diag}(1, 1, 1) \\ \mathbf{K}_{s,j} &= E_{s,j} A_{s,j} / L_s \cdot \text{diag}(1, 1, 1), \quad j = 1, 2. \end{aligned} \quad (45)$$

In (45) $A_{s,j}$ represents the area of the cross section of the secondary backbone of DDU segment j , L_s represents the length of the DDU holder, L_c represents the length of the actuation channel in the DDU cone and up to the connection point with the actuation unit.

The models of the stiffness and the forces acting on each portion of the backbones can be combined to produce a model for the extension vector $\boldsymbol{\varepsilon}_j$ for segment j ,

$$\boldsymbol{\varepsilon}_j = \eta_j \mathbf{K}_{s,j}^{-1} \boldsymbol{\tau}_j + e^{2\mu\phi} \mathbf{K}_{c,j}^{-1} (\eta_j \boldsymbol{\tau}_j + \mathbf{f}_{s,j}) + \boldsymbol{\lambda}_j. \quad (46)$$

In (46), η_j is a scale factor that corrects for uncertainties in the static model of the DDU owing to uncertainties in material properties of the NiTi, $\boldsymbol{\lambda}_j$ compensates for backlash in the actuation lines of the j th segment of the DDU. The unknown parameters in (46) are $\boldsymbol{\lambda}_j$ and η_j . These parameters can be estimated using a recursive linear estimation approach by casting (46) in the standard form for recursive linear estimation as was shown by Xu and Simaan (2006).

The linear estimation has to be carried out independently for each segment of the DDU while keeping all of the other DDU segments straight and commanding the j th segment to bend at a desired angle $\theta_{L,j}$. The estimated vector in recursion k , $[\eta_j^{[k]}, \boldsymbol{\lambda}_j^{[k]}]^T$, is refined by using the k th measurement of the bending angle, $\theta_{L,j}^{[k]}$, to calculate the theoretical extension of the backbones $\boldsymbol{\varepsilon}_j$. The calculation of $\boldsymbol{\varepsilon}_j$ is based on the inverse kinematics of the DDU segment as presented by Simaan et al. (2004a). Once the estimation of $\boldsymbol{\lambda}_j$ and η_j converge, $\boldsymbol{\varepsilon}_j$ is calculated using (46) and the corrected value of the joint command is found using (40).

This recursive estimation has been shown to converge in less than 10 iterations while providing tracking errors of less than 1° for a single segment of the DDU (Xu and Simaan

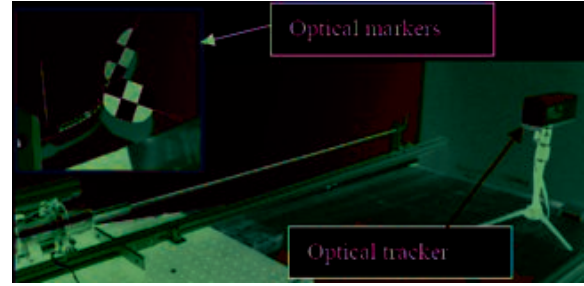


Fig. 12. Experimental setup using an optical tracker for compensation in configuration space.

2006). The results of this compensation method are satisfactory for providing good tracking on the bending angles $\theta_{L,j}$ of each segment of the DDU. Since the estimation is carried out using only the measurement of $\theta_{L,j}$ while assuming that configuration angle δ_j does not require compensation, this approach does not work as well when trying to perform rotation about the backbone with multi-segment DDU. For this reason, we adopted another approach of directly applying the compensation in configuration space.

6.3. Combined Configuration and Joint-space Actuation Compensation

It is possible to apply the compensation in configuration space $\boldsymbol{\psi}_j = [\theta_{L,j}, \delta_j]^T$ of the DDU segments prior to applying the compensation in joint space. For the two-segment DDU of Figure 5 this correction is applied on the vector $[\boldsymbol{\psi}_1^T \quad \boldsymbol{\psi}_2^T]^T$.

This method requires the complete configuration vector $\boldsymbol{\psi}_j = [\theta_{L,j}, \delta_j]^T$ of each segment of the DDU to be measured. This was achieved using a Micron[®] optical tracker, Figure 12. The compensation process was carried out serially while changing $\theta_{L,j}$ in increments of 15° in $[0^\circ, 90^\circ]$. For each $\theta_{L,j}$, δ_j was changed in increments of 5° in $[-180^\circ, 180^\circ]$. For example, the compensation process for $\theta_{L,j} = 45^\circ$ was implemented as follows: $\theta_{L,j}$ was bent to 45° and δ_j was changed from -180° to $+180^\circ$, the errors on $\theta_{L,j}$ were recorded and fitted to a series of cosine functions of δ_j ; this intermediate compensation was then implemented while $\theta_{L,j}$ was bent to 45° and δ_j was actuated between -180° and $+180^\circ$; the errors on δ_j were then fitted into a series of cosine functions of desired value of δ_j . It was noted that the errors on δ_j had different values when δ_j was actuated in clockwise or counterclockwise directions. Hence, the compensation has different expressions for the two actuation directions. Finally, this dual compensation can be written as

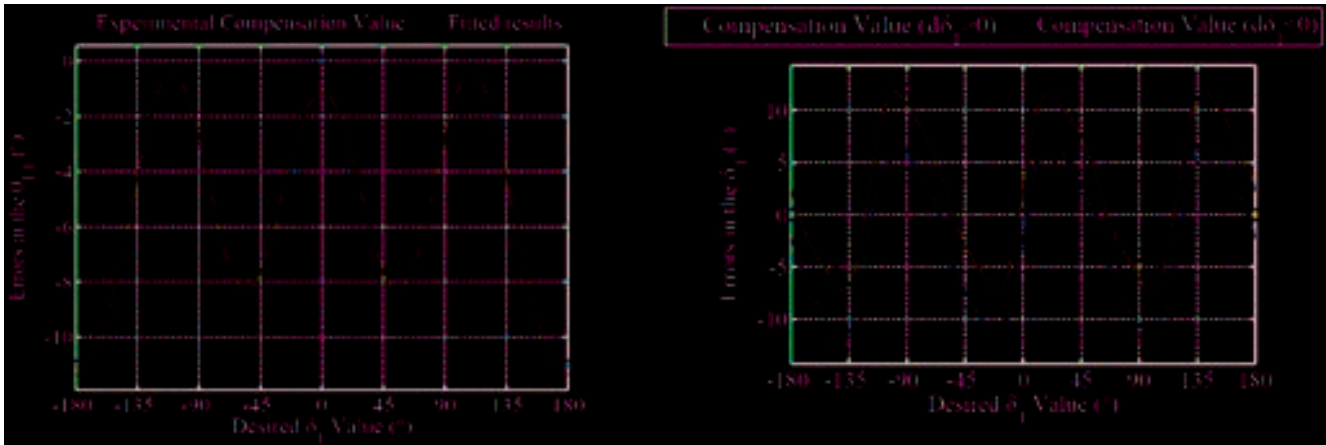


Fig. 13. Experimental errors in both δ_1 and θ_{L_1} plotted with respect to desired δ_1 when desired $\hat{\theta}_{L_1} = 45^\circ$.

$$\Delta \psi_j = \begin{bmatrix} \Delta \theta_{L_j} \\ \Delta \delta_j \end{bmatrix}$$

$$= \frac{\pi/2 - \theta_{L_j}}{\pi/2 - \pi/4} \begin{bmatrix} \sum_{i=1}^6 A_{ij} \cos((i-1)\delta_j) \\ \sum_{i=1}^3 B_{ij} \sin((3i)\delta_j) + \gamma_j \operatorname{sgn}(d\delta_j) \end{bmatrix},$$

$j = 1, 2,$ (47)

where $d\delta_j$ represents the desired incremental change in δ_j and its sign is used to determine the rotation direction of δ_j and

$$\mathbf{A} = \begin{bmatrix} -0.09096, 0.02345, -0.03043, 0.07091, \\ 0.01254, -0.004739, \\ -0.05387, 0.02927, -0.005337, 0.05041, \\ -0.001495, -0.01001 \end{bmatrix}, \quad (48)$$

$$\mathbf{B} = \begin{bmatrix} 0.1595, 0.3274, 0.01454 \\ 0.1067, 0.01511, 0.002909 \end{bmatrix},$$

$$\gamma = [0.03962, 0.03396]^T. \quad (49)$$

In the implemented compensation, the corrected configuration vector is obtained as $\psi_j = \psi_j + \Delta \psi_j$. The corrected configuration vector $\tilde{\psi}_j$ is substituted back to the joint-space compensation equation (40) to achieve the desired motion tracking. Figure 13 compares the result of (47) for θ_{L_1} and δ_1 with the observed errors. It is clearly seen that the experimental values for both θ_L and δ agree with the fitting produced by

(47). Figure 14 shows the results of this compensation used to perform rotation about the backbone of the two-segment DDU of Figure 5. Figure 15 shows the movement of the longitudinal axis of the gripper with or without compensation. The DDU during this experiment was bent such that $\theta_{L_1} = \theta_{L_2} = 30^\circ$ (60° bending) and δ_1 was varied from 0° to 720° while δ_2 was varied from -45° to 675° . The different starting points for δ_1 and δ_2 were due to the fact the proximal and distal DDU segments were not coplanar (the DDU was bent into a spatial S shape). The results of Figure 15 show that when no compensation was used, the axis of the gripper wiggled within an elliptical cone $\pm 3.5^\circ$ in horizontal direction and $\pm 5.7^\circ$ in vertical direction. When compensation was applied, the wiggle was reduced to less than $\pm 1.5^\circ$ in all directions. The accuracy of the tracker and the markers used during the configuration space compensation was $\pm 1.2^\circ$. This demonstrates the effectiveness of our approach since the algorithm almost converged within the tracking error of the tracker used to define the actuation compensation model.

7. Preliminary Experience

Figure 16 shows our most recent experiments on passing a circular suture through a mockup setup and performing knot tying using the telemanipulation system prototype of Figure 3. The figure shows that the surgeon using the master manipulator was able to effectively pass sutures and tie knots using the telemanipulation system of Figure 3. The details of the telemanipulation used in this system were presented in Kapoor et al. (2006) and so are not repeated here.

We experimentally determined the flexibility of the DDUs and we noticed that the lowest bending stiffness of the DDU is when it is fully extended. This stiffness is about 0.5 N mm^{-1} . Since the side forces applied by the DDU are no more than

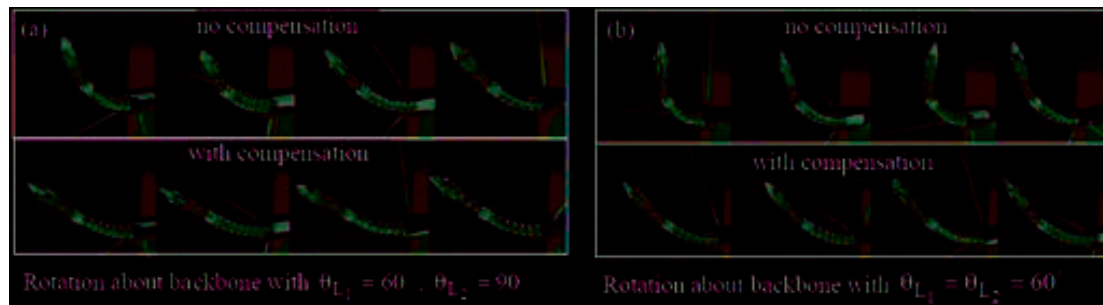


Fig. 14. Rotation about the backbone with and without actuation compensation.

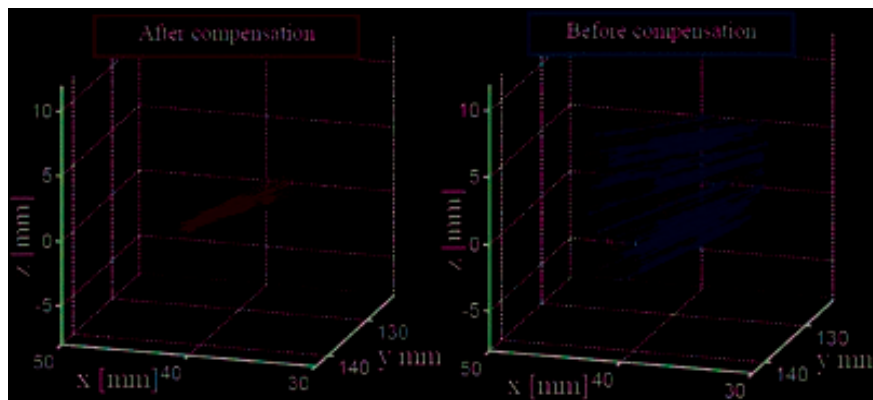


Fig. 15. Spatial motions of the longitudinal axis of the gripper during a rotation about the backbone of the DDU.

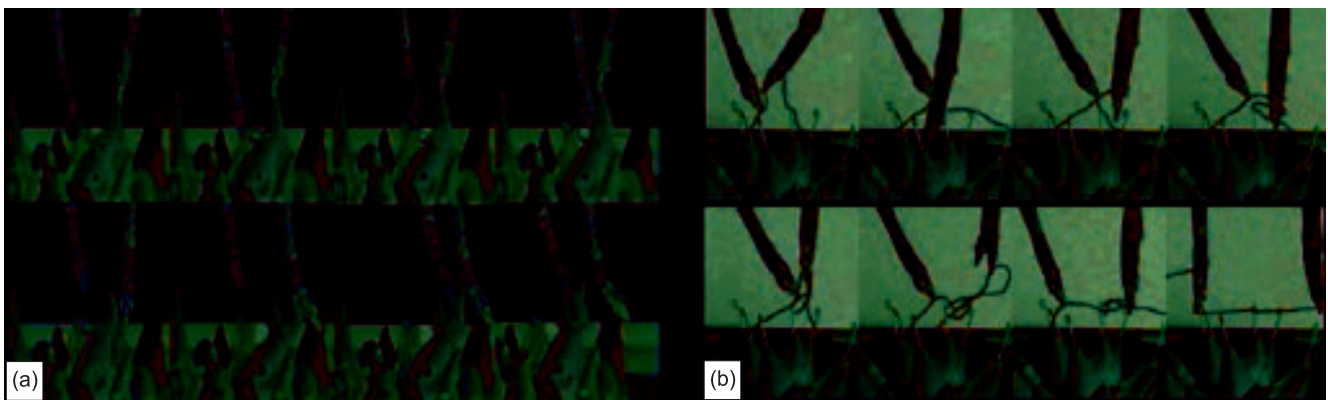


Fig. 16. Telemanipulation experiments showing: (a) passing a circular suture; (b) bi-manual knot tying. Extension 1 presents a video of the knot tying process using the robotic system of Figure 3.

1 N, we did not experience major deflections that prevented the surgeon from being able to use the system effectively. The repeatability of the slave robot using the actuation compensation is 1° in orientation and 0.5 mm in positioning. This repeatability, however, is not maintained when the DDU performs rolling

motion about its backbone. The observed repeatability after actuation compensation is better than $\pm 1.5^\circ$ in orientation and ± 0.8 mm in positioning. This repeatability depends on the accuracy of the tracker used during the actuation compensation calibration experiments.

The maximal bending rates of the DDU's were validated. Our experience shows that the DDU's proximal segments were able to bend 90° in 1 second in any direction. The distal segments were able to bend 60° in any direction within 0.3 seconds. The time for tying a knot depends heavily on the user and his familiarity with the master interface and the visualization interface used. The users were not able to complete a knot using a two-dimensional display. When using a three-dimensional display, the estimated time for passing a suture was 10 seconds and the time for tying a knot was 18 seconds (see Extension 1 for a video of knot tying).

8. Conclusions

Despite the efforts of the robotics community to provide robotic assistance for MIS, there are some challenging areas that do not yield to existing robot designs due to limitations on dexterity, size, and availability of suitable DoFs. One of these challenging areas (namely MIS of the throat) has been addressed in this work. The clinical motivation driving our research highlights the importance of intracorporeal knot tying and suturing in order to effectively enable various minimally invasive procedures for the throat.

A novel design of dual-arm robotic slave with 20 joint-space DoFs has been presented. This robotic slave was designed to provide dexterity through the use of continuum snake-like robots (DDUs). The kinematics of the system includes flexible continuum robots (the DDU's) and flexible stems manipulated by five-bar parallel robots. The statics and actuation compensation supporting enhanced miniaturization, increased payload carrying capability, and precision tracking have been presented. Specifically, a special mode of operation suitable for intracorporeal suturing has been presented. This mode of operation involves using the snake-like robot (DDU) to provide rotation about the longitudinal axis of the gripper by transmitting rotation from its base along its central backbone. Successful execution of this mode of operation is predicated on a precise synchronous actuation of all backbones actuating the continuum robot (DDU). A method for actuation compensation was presented in order to overcome uncertainties of modeling, friction, and backlash. This method uses a tiered hierarchy of two novel approaches of actuation compensation for remotely actuated snake-like robots. The first tier of our actuation compensation uses intrinsic joint-space information together with extrinsic pose measurement of the DDU in order to provide a linear recursive estimation of the compensation parameters. The results of this first tier are suitable for single-segment DDU's. In order to account for coupling effects among adjacent DDU segments, a second tier of actuation compensation was presented. This second tier uses configuration-space compensation approach in order to provide precise actuation compensation for multi-segment flexible snake-like robots (DDU's).

The design specifications, kinematics, control, and actuation compensation presented in this paper have been experimentally validated on an integrated prototype telemanipulation system that includes a *da Vinci* master, a stereoscopic capture and display subsystem along with our dual-arm slave. All of the components of this prototype system have been tested to work in conjunction with each other under realistic surgical task scenarios. These experiments show that the compensation algorithms presented can support rotation about the central backbone of complex multi-segment continuum robots and that the accuracy of the compensation is close to the error of the extrinsic information used to calibrate the actuation models. Telemanipulation experiments show that the prototype system is capable of passing sutures in constrained spaces such as the throat. Future work will include experiments and performance validation of the prototype system in performing specific surgical tasks for throat surgery in animal or cadaver models.

The methods presented in this paper were designed specifically for our system. However, these methods extend to robotic systems that use flexible members, systems that use mechanically remote actuation of snake-like robots (e.g. MRI compatible robots), and any telemanipulation system that uses high-DoF snake-like slaves for telemanipulation.

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Appendix: Appendix of Multimedia Extensions

The multimedia extension page is found at <http://www.ijrr.org>.

Table of Multimedia Extensions

Extension	Type	Description
1	Video	Dual-arm suturing and knot tying using the robotic system of Figure 3.

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