

0	Papa	1
0 ROOT . S	0 NP Papa .	
0 S . NP VP	0 S NP . VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP	1 VP . V NP	
0 NP . Papa	1 VP . VP PP	
0 Det . the	1 PP . P NP	
0 Det . a	1 V . ate	
	1 V . drank	
	1 V . snorted	

predict

- Every .VP adds all VP → ... rules again.
- Before adding a rule, check it's not a duplicate.
- Slow if there are > 700 VP → ... rules, so what will you do in Homework 4?

0	Papa	1
0 ROOT . S	0 NP Papa .	
0 S . NP VP	0 S NP . VP	
0 NP . Det N	0 NP NP . PP	
0 NP . NP PP	1 VP . V NP	
0 NP . Papa	1 VP . VP PP	
0 Det . the	1 PP . P NP	
0 Det . a	1 V . ate	
	1 V . drank	
	1 V . snorted	
	1 P . with	

predict

- .P makes us add all the prepositions ...

1-word lookahead would help

0	Papa	1	ate
0 ROOT . S	0 NP Papa .		
0 S . NP VP	0 S NP . VP		
0 NP . Det N	0 NP NP . PP		
0 NP . NP PP	1 VP . V NP		
0 NP . Papa	1 VP . VP PP		
0 Det . the	1 PP . P NP		
0 Det . a	1 V . ate		
	1 V . drank		
	1 V . snorted		
	1 P . with		

No point in adding words other than ate

1-word lookahead would help

0	Papa	1	ate
0 ROOT . S	0 NP Papa .		
0 S . NP VP	0 S NP . VP		
0 NP . Det N	0 NP NP . PP		
0 NP . NP PP	1 VP . V NP		
0 NP . Papa	1 VP . VP PP		
0 Det . the	1 PP . P NP		
0 Det . a	1 V . ate		
	1 V . drank		
	1 V . snorted		
	1 P . with		

In fact, no point in adding any constituent that can't start with ate
Don't bother adding PP, P, etc.

No point in adding words other than ate

With Left-Corner Filter

0	Papa	1	ate
0 ROOT . S	0 NP Papa .		
0 S . NP VP	0 S NP . VP		
0 NP . Det N	0 NP NP . PP		
0 NP . NP PP	1 VP . V NP		
0 NP . Papa			
0 Det . the			
0 Det . a			

attach

PP can't start with ate

Birth control – now we won't predict

1 PP . P NP

1 P . with

either!

Need to know that ate can't start PP

Take closure of all categories that it does start ...

0	Papa	1	ate
0 ROOT . S	0 NP Papa .		
0 S . NP VP	0 S NP . VP		
0 NP . Det N	0 NP NP . PP		
0 NP . NP PP	1 VP . V NP		
0 NP . Papa	1 VP . VP PP		
0 Det . the			
0 Det . a			

predict

0	Papa	1	ate
0 ROOT . S	0 NP Papa .		
0 S . NP VP	0 S NP . VP		
0 NP . Det N	0 NP NP . PP		
0 NP . NP PP	1 VP . V NP	predict	
0 NP . Papa	1 VP . VP PP		
0 Det . the	1 V . ate		
0 Det . a	1 V . drank		
	1 V . spotted		

0	Papa	1	ate
0 ROOT . S	0 NP Papa .		
0 S . NP VP	0 S NP . VP		
0 NP . Det N	0 NP NP . PP		
0 NP . NP PP	1 VP . V NP	predict	
0 NP . Papa	1 VP . VP PP		
0 Det . the	1 V . ate		
0 Det . a	1 V . drank		
	1 V . spotted		

Merging Right-Hand Sides

- Grammar might have rules
 - $X \rightarrow A G H P$
 - $X \rightarrow B G H P$
- Could end up with both of these in chart:
 - (2, $X \rightarrow A . G H P$) in column 5
 - (2, $X \rightarrow B . G H P$) in column 5
- But these are now interchangeable: if one produces X then so will the other
- To avoid this redundancy, can always use dotted rules of this form: $X \rightarrow \dots G H P$

Merging Right-Hand Sides

- Similarly, grammar might have rules
 - $X \rightarrow A G H P$
 - $X \rightarrow A G H Q$
- Could end up with both of these in chart:
 - (2, $X \rightarrow A . G H P$) in column 5
 - (2, $X \rightarrow A . G H Q$) in column 5
- Not interchangeable, but we'll be processing them in parallel for a while ...
- Solution: write grammar as $X \rightarrow A G H (P | Q)$

Merging Right-Hand Sides

- Combining the two previous cases:
 - $X \rightarrow A G H P$
 - $X \rightarrow A G H Q$
 - $X \rightarrow B G H P$
 - $X \rightarrow B G H Q$
- becomes
 - $X \rightarrow (A | B) G H (P | Q)$
- And often nice to write stuff like
 - $NP \rightarrow (Det | \epsilon) Adj^* N$

Merging Right-Hand Sides

- $X \rightarrow (A | B) G H (P | Q)$
- $NP \rightarrow (Det | \epsilon) Adj^* N$
- These are regular expressions!
- Build their minimal DFAs:
 -
 -
- Automaton states replace dotted rules ($X \rightarrow A G . H P$)

Merging Right-Hand Sides

Indeed, *all* NP → rules can be unioned into a single DFA!

NP → ADJP ADJP JJ JJ NN NNS
 NP → ADJP DT NN
 NP → ADJP JJ NN
 NP → ADJP JJ NN NNS
 NP → ADJP JJ NNS
 NP → ADJP NN
 NP → ADJP NN NN
 NP → ADJP NN NNS
 NP → ADJP NNS
 NP → ADJP NPR
 NP → ADJP NPRS
 NP → DT
 NP → DT ADJP
 NP → DT ADJP, JJ NN
 NP → DT ADJP ADJP NN
 NP → DT ADJP JJ JJ NN
 NP → DT ADJP JJ NN
 NP → DT ADJP JJ NN NN

etc.

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Merging Right-Hand Sides

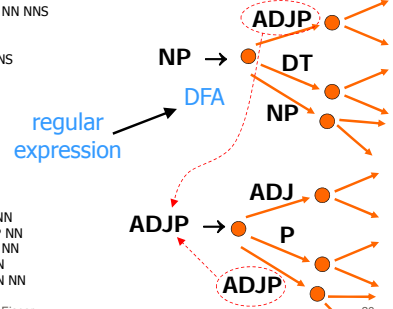
Indeed, *all* NP → rules can be unioned into a single DFA!

NP → ADJP ADJP JJ JJ NN NNS
 ADJP DT NN
 ADJP JJ NN
 ADJP JJ NN NNS
 ADJP JJ NNS
 ADJP NN
 ADJP NN NN
 ADJP NN NNS
 ADJP NNS
 ADJP NPR
 ADJP NPRS
 DT
 DT ADJP
 DT ADJP, JJ NN
 DT ADJP ADJP NN
 DT ADJP JJ JJ NN
 DT ADJP JJ NN
 DT ADJP JJ NN NN

etc.

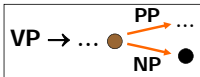
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Earley's Algorithm on DFAs

- What does Earley's algorithm now look like?



Column 4
...
(2, ●) predict

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Earley's Algorithm on DFAs

- What does Earley's algorithm now look like?



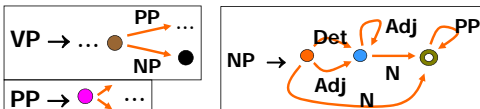
Column 4
...
(2, ●) predict
(4, ●) attach
(4, ●) attach

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Earley's Algorithm on DFAs

- What does Earley's algorithm now look like?



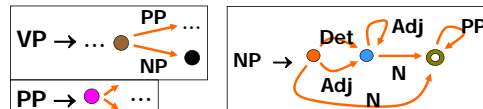
Column 4	Column 5	...	Column 7
...	...		
(2, ●) predict			(4, ●) predict or attach?
(4, ●) attach			
(4, ●) attach	→(4, ●)		

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Earley's Algorithm on DFAs

- What does Earley's algorithm now look like?



Column 4	Column 5	...	Column 7
...	...		
(2, ●) predict			(4, ●) predict or attach?
(4, ●) attach			(7, ●) attach
(4, ●) attach	→(4, ●)		(2, ●) attach

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Pruning and Prioritization

- **Heuristically throw away** constituents that probably won't make it into best complete parse.
- Use **probabilities** to decide which ones.
 - So probs are useful for speed as well as accuracy!
- **Both safe and unsafe methods exist**
 - **Iterative deepening:** Throw x away if $p(x) < 10^{-200}$ (and lower this threshold if we don't get a parse)
 - **Heuristic pruning:** Throw x away if $p(x) < 0.01 * p(y)$ for some y that spans the same set of words (for example)
 - **Prioritization:** If $p(x)$ is low, don't throw x away; just postpone using it until you need it (hopefully you won't).

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Prioritization continued: Agenda-Based Parsing

- **Prioritization:** If $p(x)$ is low, don't throw x away; just postpone using it until you need it.
 - In other words, explore best options first.
 - Should get some good parses early on; then stop!

time	1	files	2	like	3	an	4	arrow	5
0	NP 3		NP 10						NP 24
	Vst 3	S 8							S 22
1			NP 4						NP 18
			VP 4						S 21
									VP 18
2					P 2				PP 12
					V 5				VP 16
3						Det 1			NP 10
4									N 8

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Prioritization continued: Agenda-Based Parsing

- until we pop a parse ${}_0S_5$ or fail with empty agenda
 - pop top element ${}_iY_j$ from agenda into chart
 - for each right neighbor ${}_iZ_k$
 - for each rule $X \rightarrow YZ$ in grammar
 - put ${}_iX_k$ onto the agenda
 - for each left neighbor ${}_hZ_l$
 - for each rule $X \rightarrow ZY$
 - put ${}_hX_j$ onto the agenda

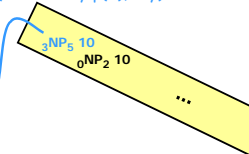
chart of good constituents

time	1	files	2	like	3	an	4	arrow	5
0	NP 3		NP 10						NP 24
	Vst 3	S 8							S 22
1			NP 4						NP 18
			VP 4						S 21
2					P 2				PP 12
					V 5				VP 16
3						Det 1			NP 10
4									N 8

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prioritized agenda of pending constituents (ordered by $p(x)$, say)



Prioritization continued: Agenda-Based Parsing

- until we pop a parse ${}_0S_5$ or fail with empty agenda
 - pop top element ${}_iY_j$ from agenda into chart
 - for each right neighbor ${}_iZ_k$
 - for each rule $X \rightarrow YZ$ in grammar
 - put ${}_iX_k$ onto the agenda
 - for each left neighbor ${}_hZ_l$
 - for each rule $X \rightarrow ZY$
 - put ${}_hX_j$ onto the agenda

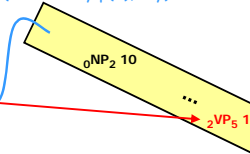
chart of good constituents

time	1	files	2	like	3	an	4	arrow	5
0	NP 3		NP 10						NP 24
	Vst 3	S 8							S 22
1			NP 4						NP 18
			VP 4						S 21
2					P 2				PP 12
					V 5				VP 16
3						Det 1			NP 10
4									N 8

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prioritized agenda of pending constituents (ordered by $p(x)$, say)



Prioritization continued: Agenda-Based Parsing

always finds best parse!
analogous to Dijkstra's
shortest-path algorithm

- until we pop a parse ${}_0S_5$ or fail with empty agenda
 - pop top element ${}_iY_j$ from agenda into chart
 - for each right neighbor ${}_iZ_k$
 - for each rule $X \rightarrow YZ$ in grammar
 - put ${}_iX_k$ onto the agenda
 - for each left neighbor ${}_hZ_l$
 - for each rule $X \rightarrow ZY$
 - put ${}_hX_j$ onto the agenda

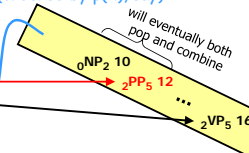
chart of good constituents

time	1	files	2	like	3	an	4	arrow	5
0	NP 3		NP 10						NP 24
	Vst 3	S 8							S 22
1			NP 4						NP 18
			VP 4						S 21
2					P 2				PP 12
					V 5				VP 16
3						Det 1			NP 10
4									N 8

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prioritized agenda of pending constituents (ordered by $p(x)$, say)



Outside Estimates for better Pruning and Prioritization

- **Iterative deepening:** Throw x away if $p(x)*q(x) < 10^{-200}$ (lower this threshold if we don't get a parse)
- **Heuristic pruning:** Throw x away if $p(x)*q(x) < 0.01*p(y)*q(y)$ for some y that spans the same set of words
- **Prioritized agenda:** Priority of x on agenda is $p(x)*q(x)$; stop at first parse

- In general, the "inside prob" $p(x)$ will be higher for smaller constituents
 - Not many rule probabilities inside them
- The "outside prob" $q(x)$ is intended to correct for this
 - Estimates the prob of all the rest of the rules needed to build x into full parse
 - So $p(x)*q(x)$ estimates prob of the best parse that contains x
- If we take $q(x)$ to be the best estimate we can get
 - Methods may no longer be safe (but may be fast!)
 - Prioritized agenda is then called a "best-first algorithm"
- But if we take $q(x)=1$, that's just the methods from previous slides
 - And iterative deepening and prioritization were safe there
- If we take $q(x)$ to be an "optimistic estimate" (always \geq true prob)
 - Still safe! Prioritized agenda is then an example of an "A* algorithm"

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Disallow Center-Embedding?

- Center-embedding seems to be in the grammar, but people have trouble processing more than 1 level of it.
- You can limit # levels of center-embedding via features: e.g., $S[S_DEPTH=n+1] \rightarrow A S[S_DEPTH=n] B$
- If a CFG limits # levels of embedding, then it can be compiled into a finite-state machine – we don't need a stack at all!
 - Finite-state recognizers run in linear time.
 - However, it's tricky to turn them into parsers for the original CFG from which the recognizer was compiled.
 - And compiling a **small** grammar into a much **larger** FSA may be a net loss – structure sharing in the parse chart is expanded out to duplicate structure all over the FSA.

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Parsing Algs for non-CFG

- If you're going to make up a new kind of grammar, you should also describe how to parse it.
- Such algorithms exist, e.g.,
 - for TAG (where the grammar specifies not just rules but larger tree fragments, which can be combined by "substitution" and "adjunction" operations)
 - for CCG (where the grammar only specifies preterminal rules, and there are generic operations to combine slashed nonterminals like X/Y or $(X/Z)/(Y/W)$)

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