

# On Communication Models and Best-Achievable Security in Two-Round MPC

Aarushi Goel

Abhishek Jain

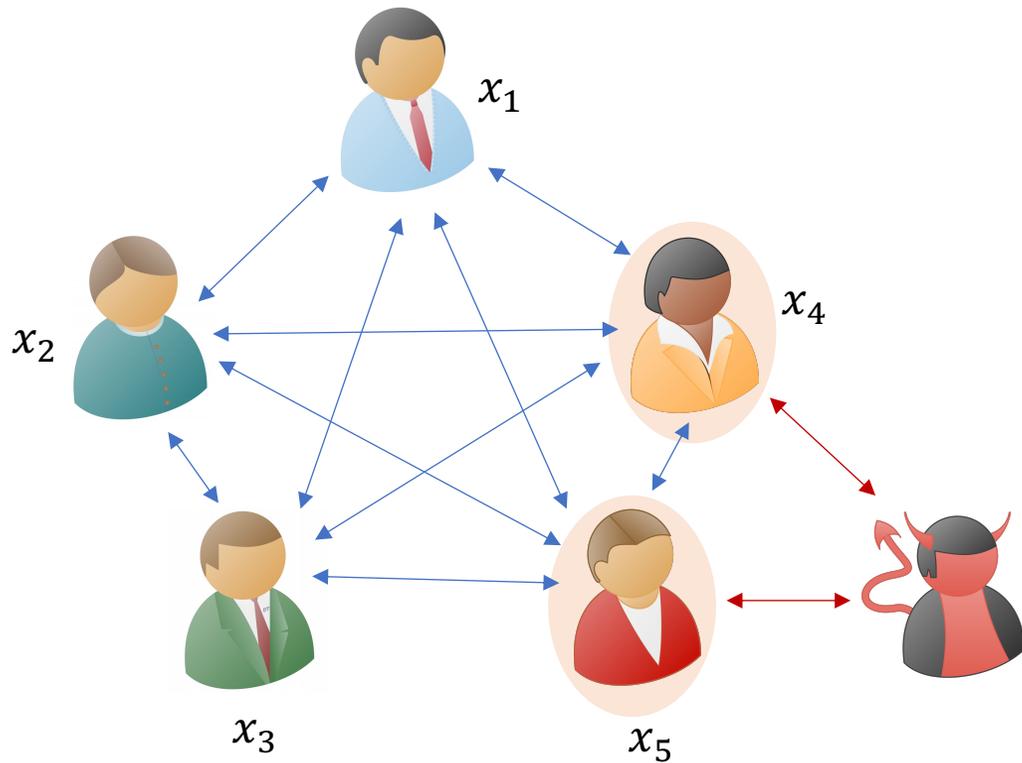
Manoj Prabhakaran

Rajeev Raghunath



Indian Institute of  
Technology Bombay

# Secure Multiparty Computation (MPC)

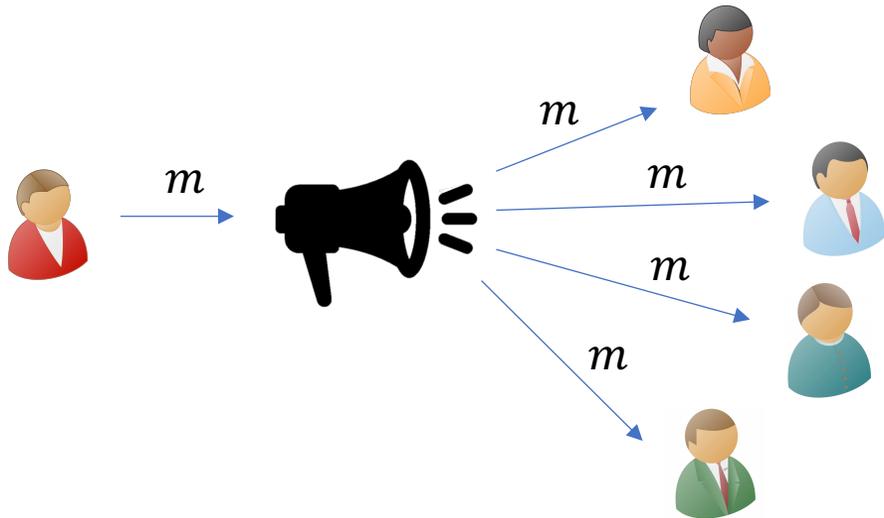


Adversary learns nothing beyond the output  $y$

MPC protocol for computing  $y = f(x_1, x_2, x_3, x_4, x_5)$

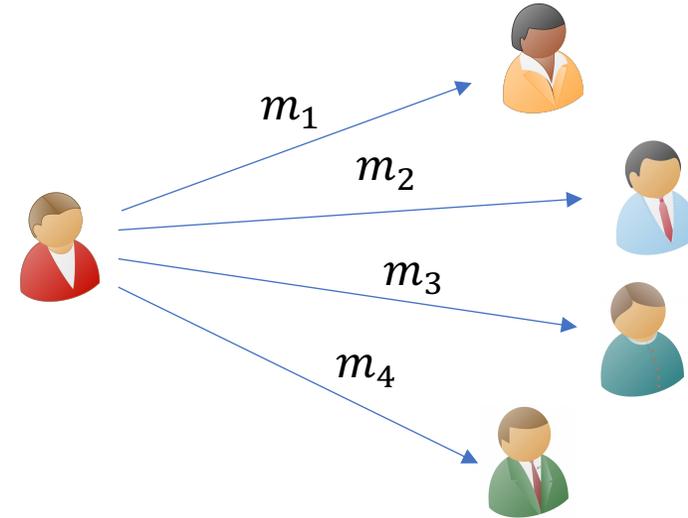
# Communication Models

Broadcast Channel



Necessary for achieving security against  $t > n/3$  corruptions

Private Point-to-Point (P2P) Channels



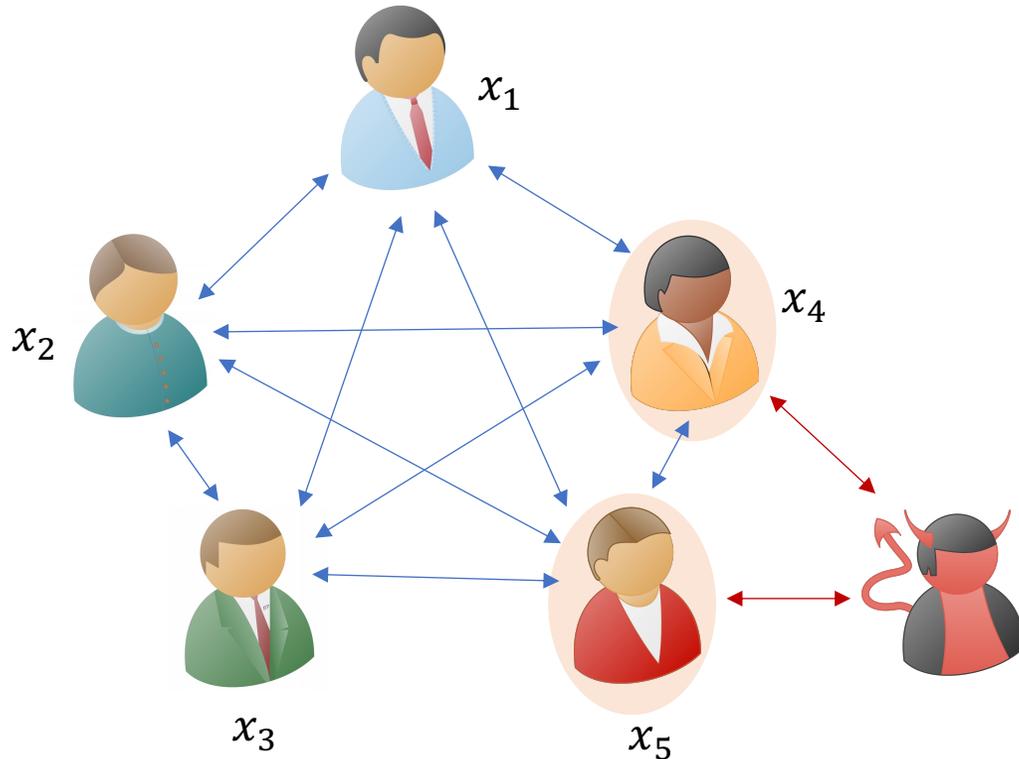
Necessary for achieving information theoretic security

# Our Setting: Two-Rounds

Minimal Rounds, since one-round MPC is impossible [HLP'11]

A lot of advancement in recent years  
[GS'18, BL'18, PR18, ACGJ'18, ABT'18, GIS'18, ACGJ'19, ABT'19]

# Our Setting: Honest Majority [BGW88]



## Advantages

Enables stronger security guarantees

Can be designed using only symmetric-key primitives

Can be designed in fewer Rounds

Often holds up in practice

Adversary corrupts a **minority** of the parties

# Main Question

In two-round honest-majority MPC, in the different communication models involving broadcast and P2P channels:

What levels of security are achievable for general computation?

Under what assumptions?

In this work we focus on the plain model (no setup) and sometimes augment it to use a bare public-key infrastructure (bare PKI)

# Different Security Notions

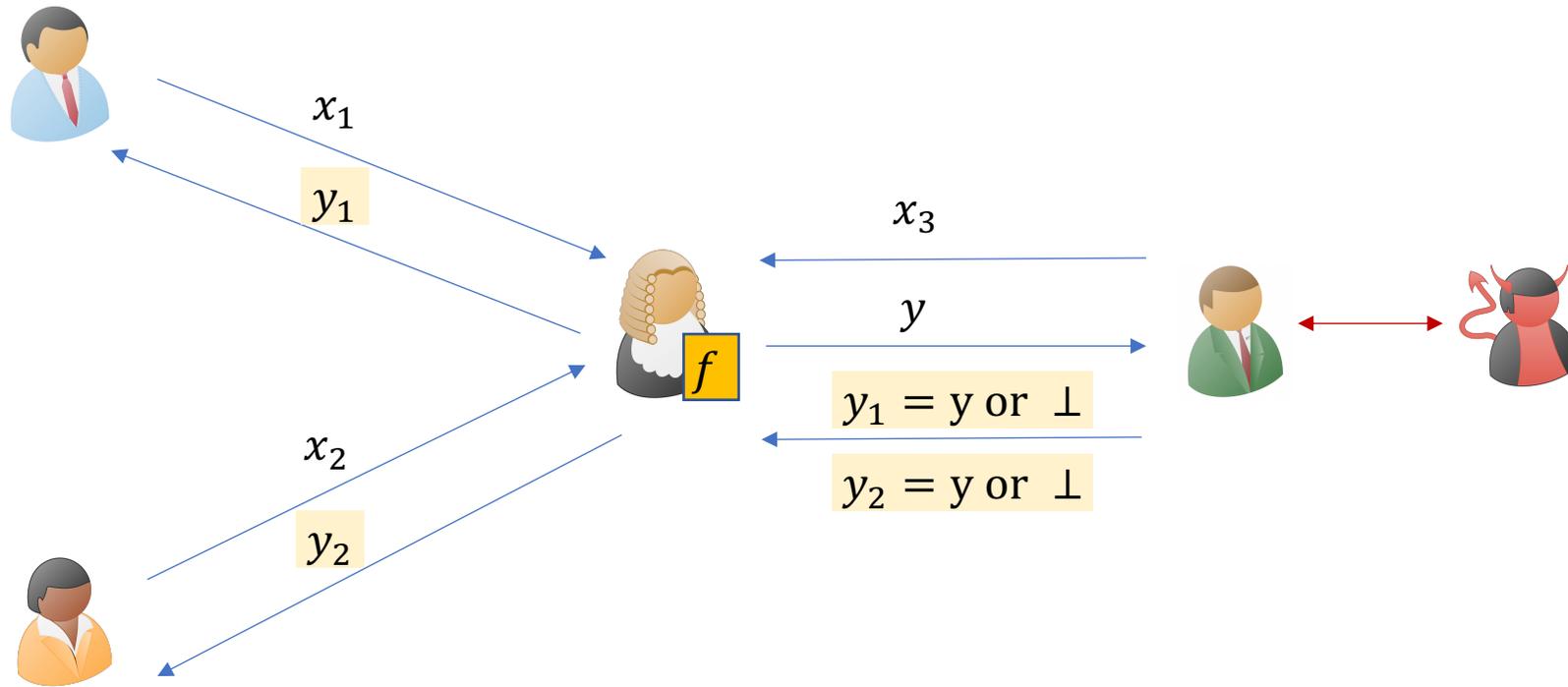
Privacy against semi-honest adversaries

# Different Security Notions

Privacy against semi-honest adversaries

Security with (**Selective/Unanimous/Identifiable**) abort against malicious adversaries

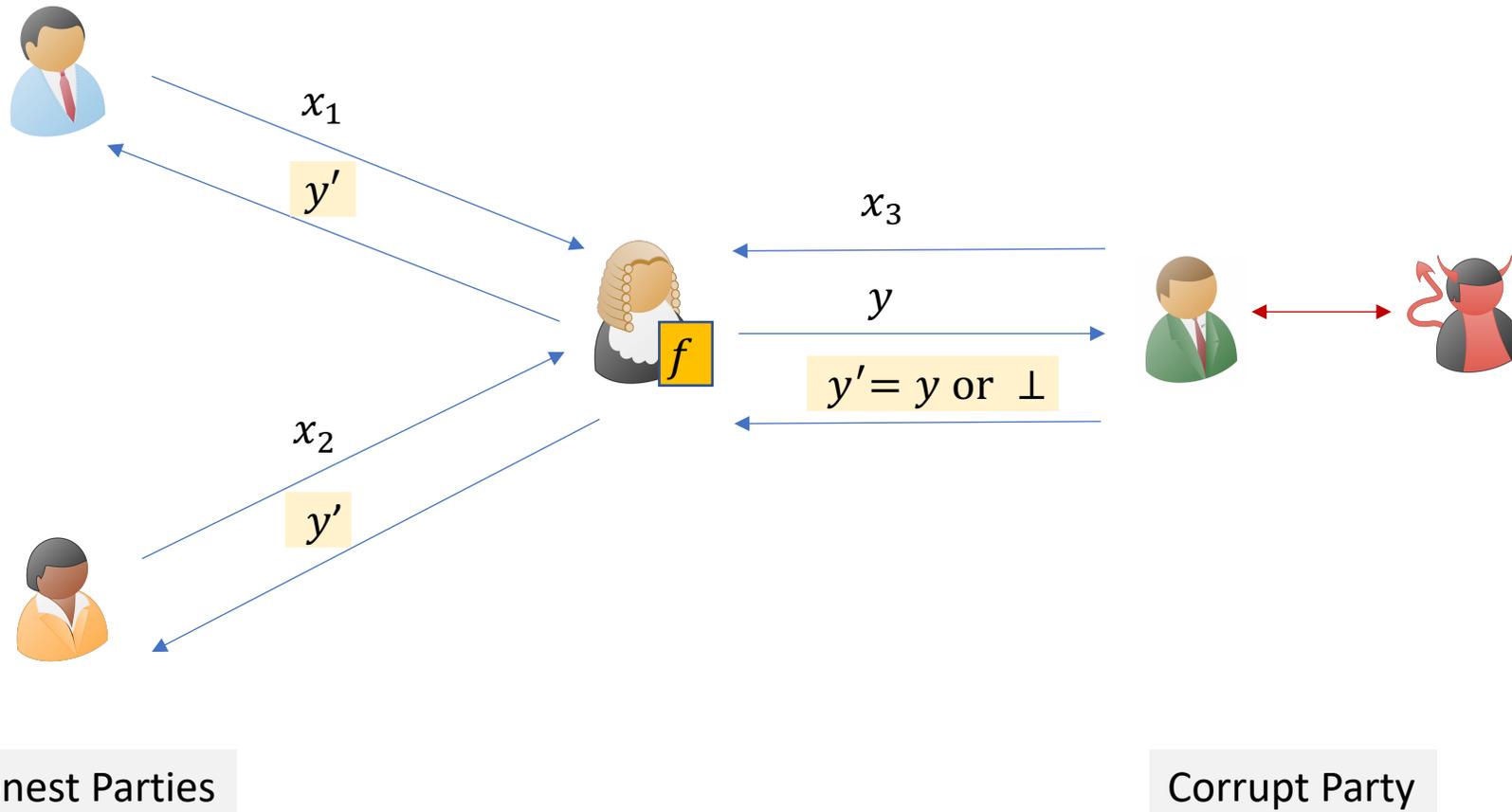
# Security with Selective Abort



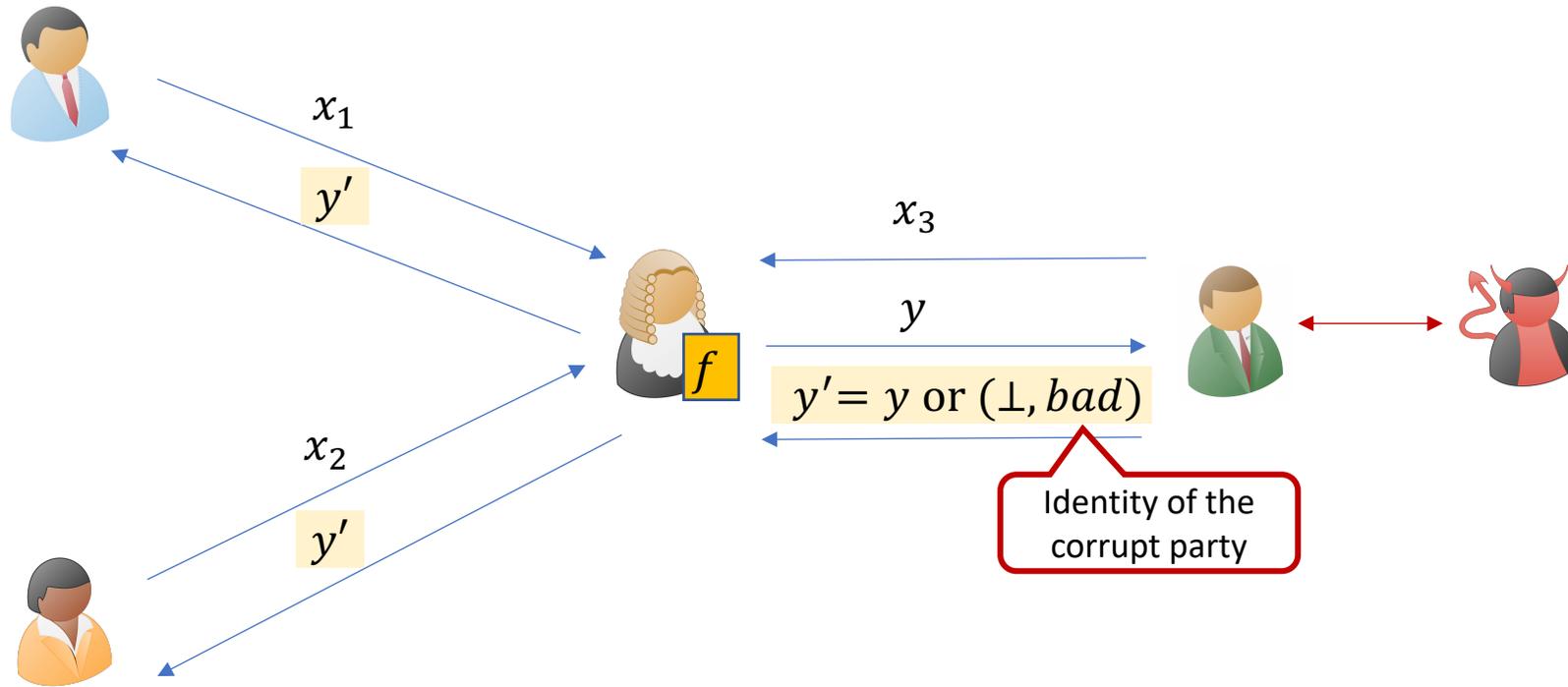
Honest Parties

Corrupt Party

# Security with Unanimous Abort



# Security with Identifiable Abort



Honest Parties

Corrupt Party

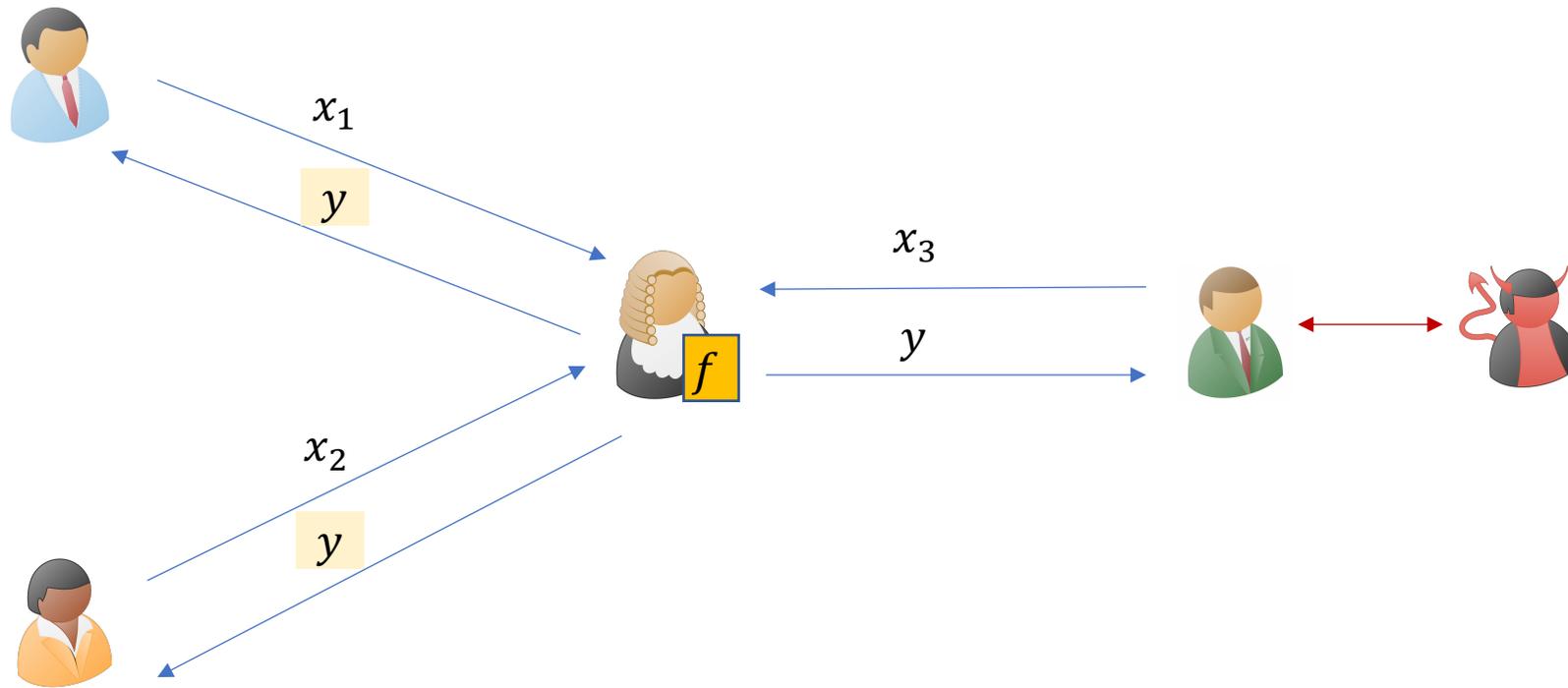
# Different Security Notions

Privacy against semi-honest adversaries

Security with (**Selective/Unanimous/Identifiable**) abort against malicious adversaries

Guaranteed output delivery against (**Malicious/Fail-stop**) adversaries

# Guaranteed Output Delivery

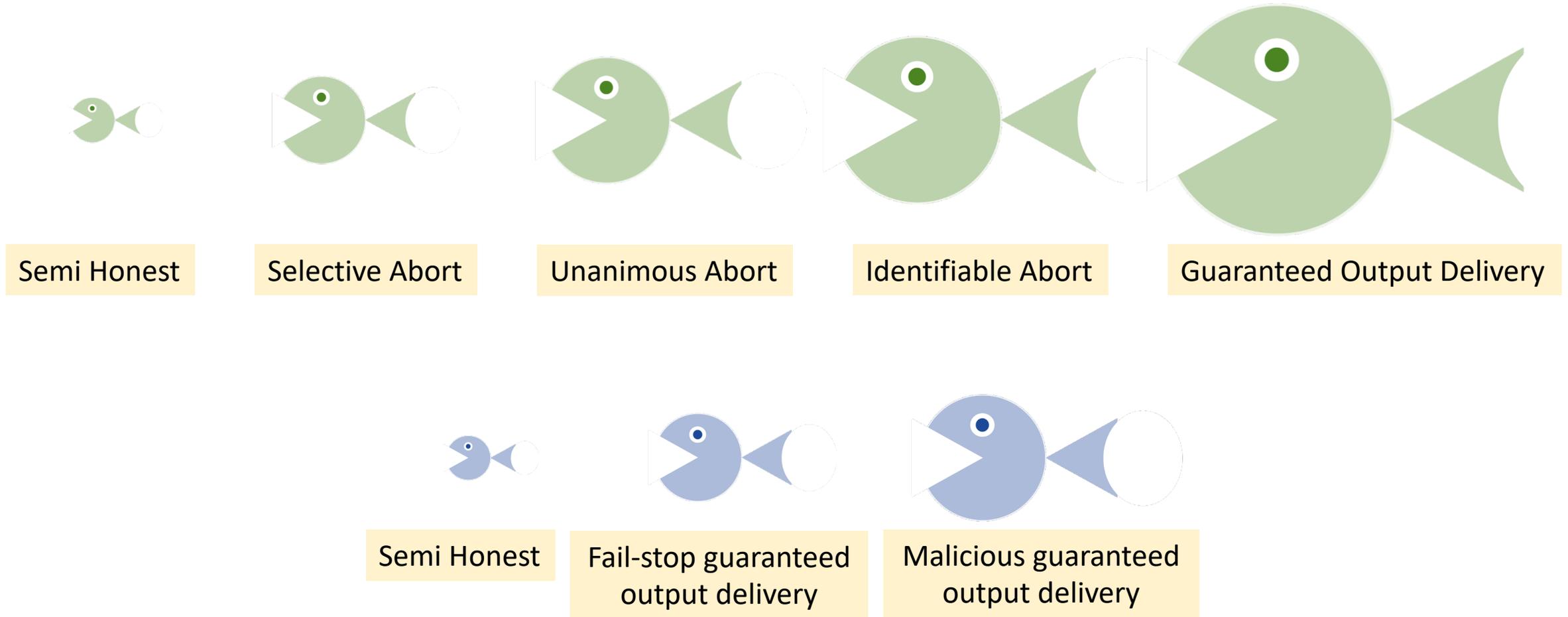


Honest Parties

Corrupt Party

Adversary is either malicious or fail-stop

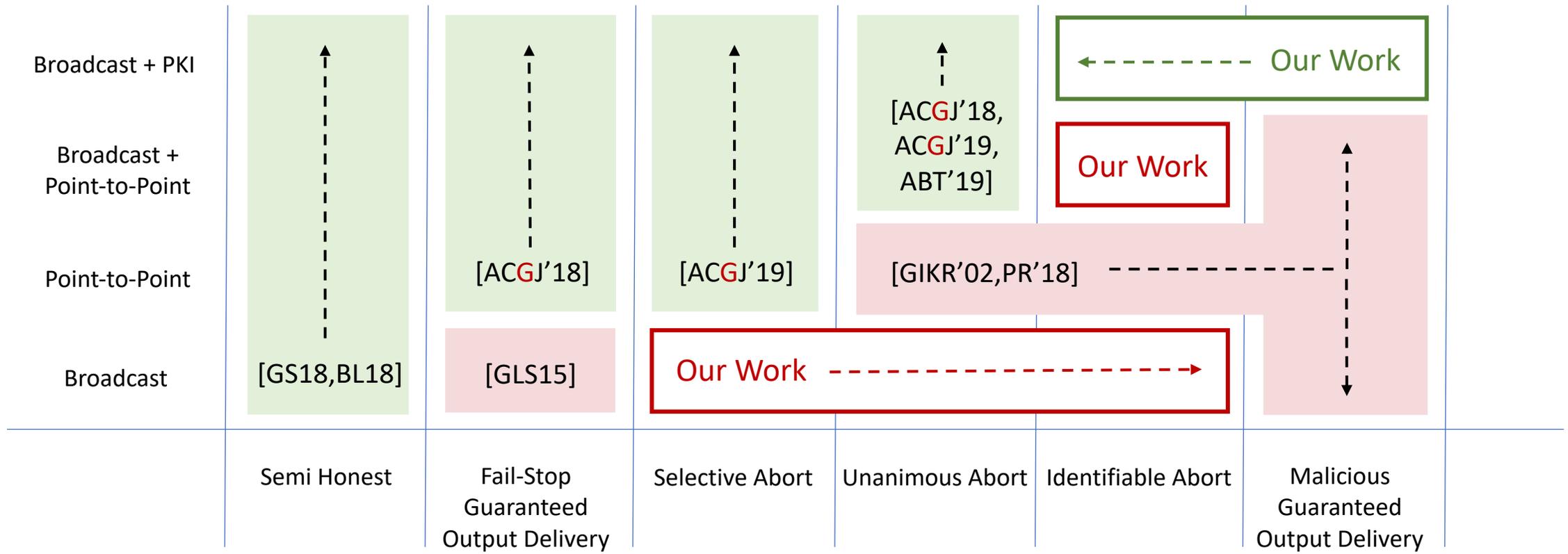
# Hierarchy of Security Notions



# Two-Round MPC

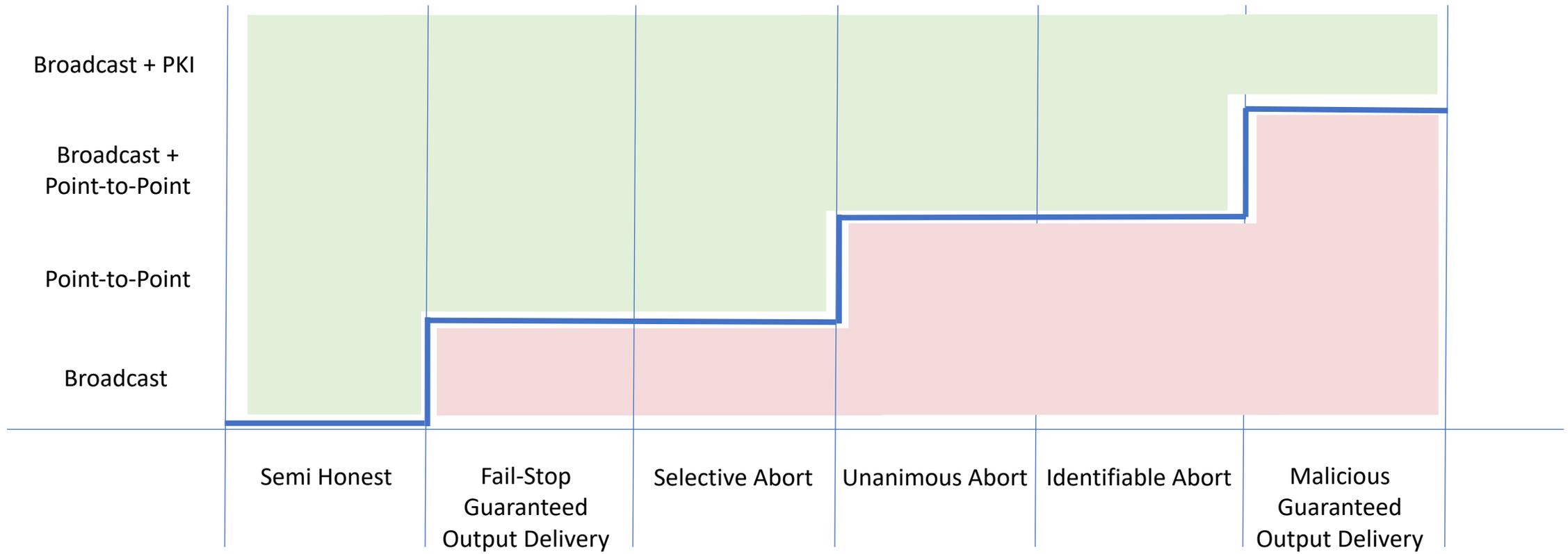
Broadcast + PKI				↑ [ACGJ'18, ACGJ'19, ABT'19]	?	?
Broadcast + Point-to-Point		↑	↑		?	↑
Point-to-Point		[ACGJ'18]	[ACGJ'19]	[GIKR'02,PR'18]	-----	↓
Broadcast	[GS18,BL18]	[GLS15]	?	?	?	
	Semi Honest	Fail-Stop Guaranteed Output Delivery	Selective Abort	Unanimous Abort	Identifiable Abort	Malicious Guaranteed Output Delivery

# Two-Round MPC (Completing the Picture)

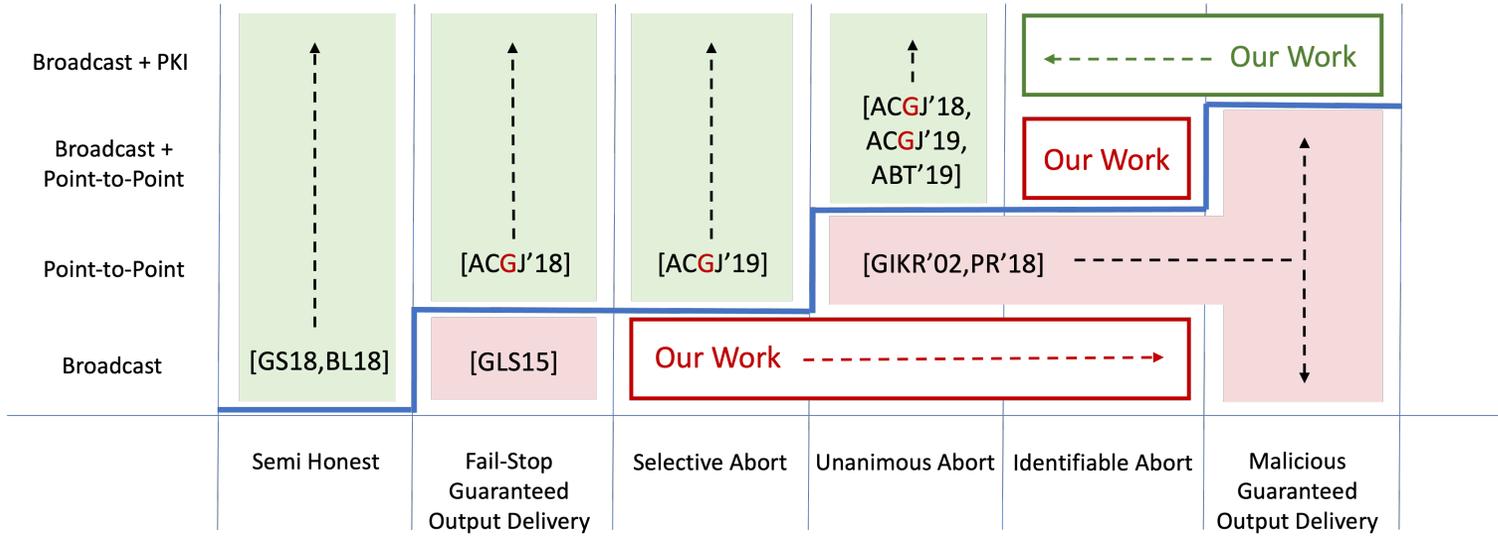


# Hierarchy of Communication Models

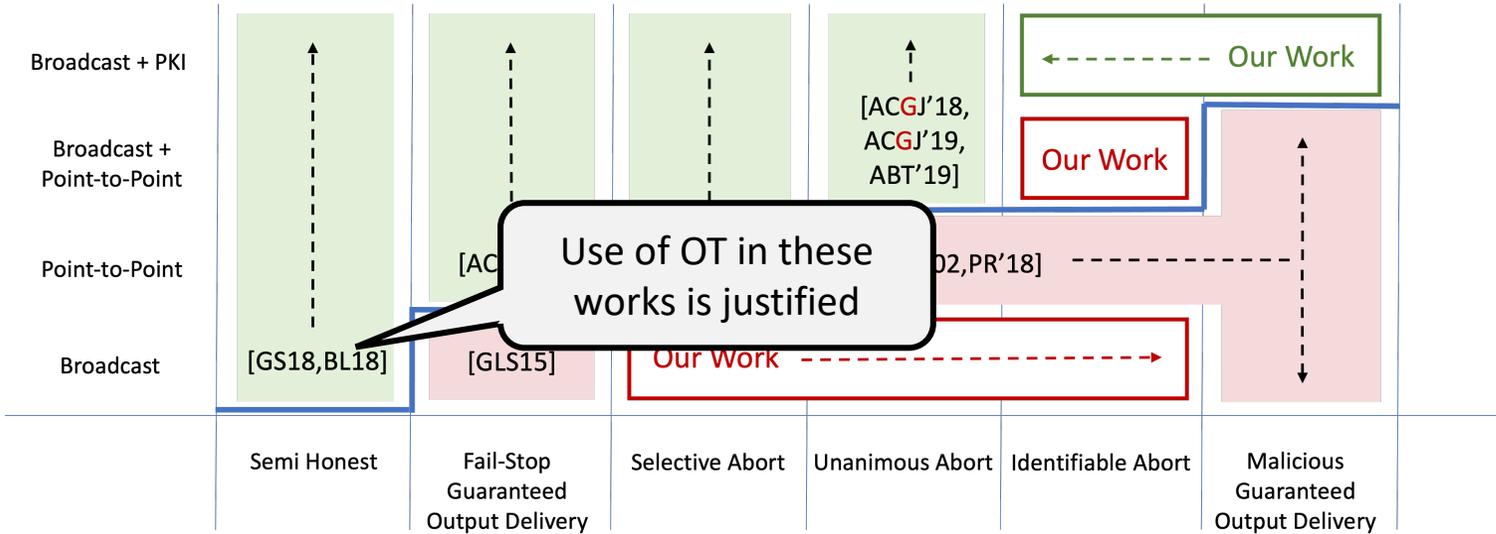
Broadcast < Point-to-Point < Broadcast + Point-to-Point < Broadcast + PKI



# Our Contributions



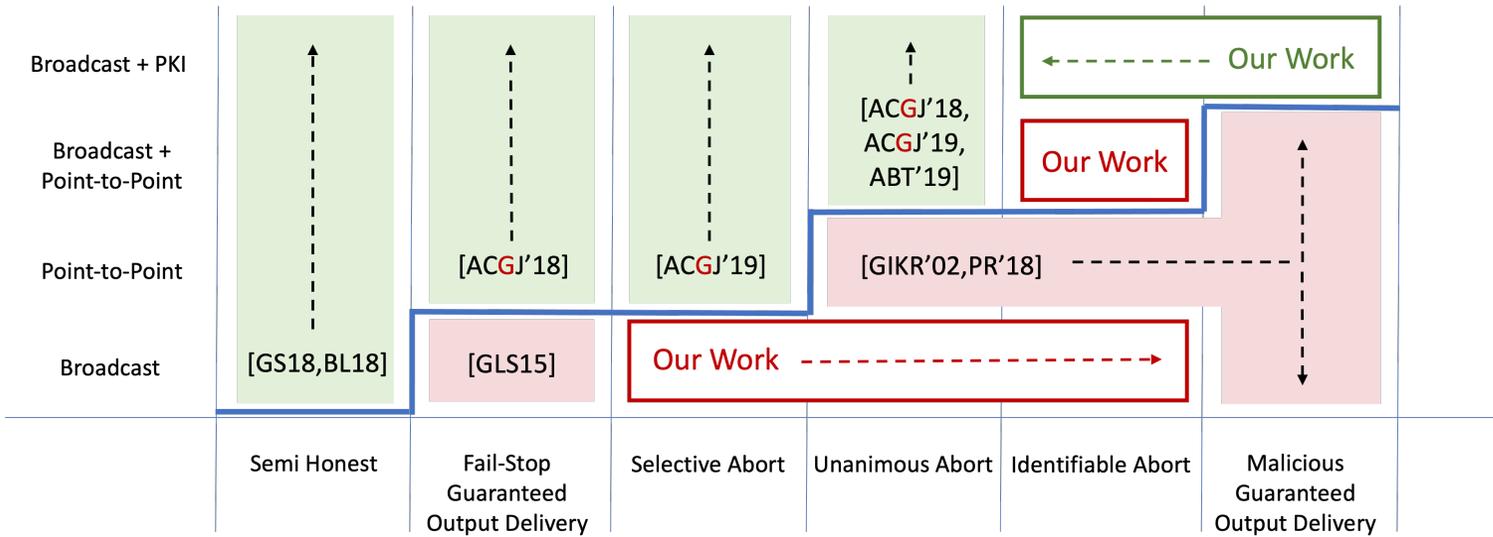
# Our Contributions



Two-round honest-majority **semi-honest/malicious** MPC over broadcast channels  
 ⇒ **semi-honest/malicious** two-message OT

This implication holds both in the plain and in the CRS model

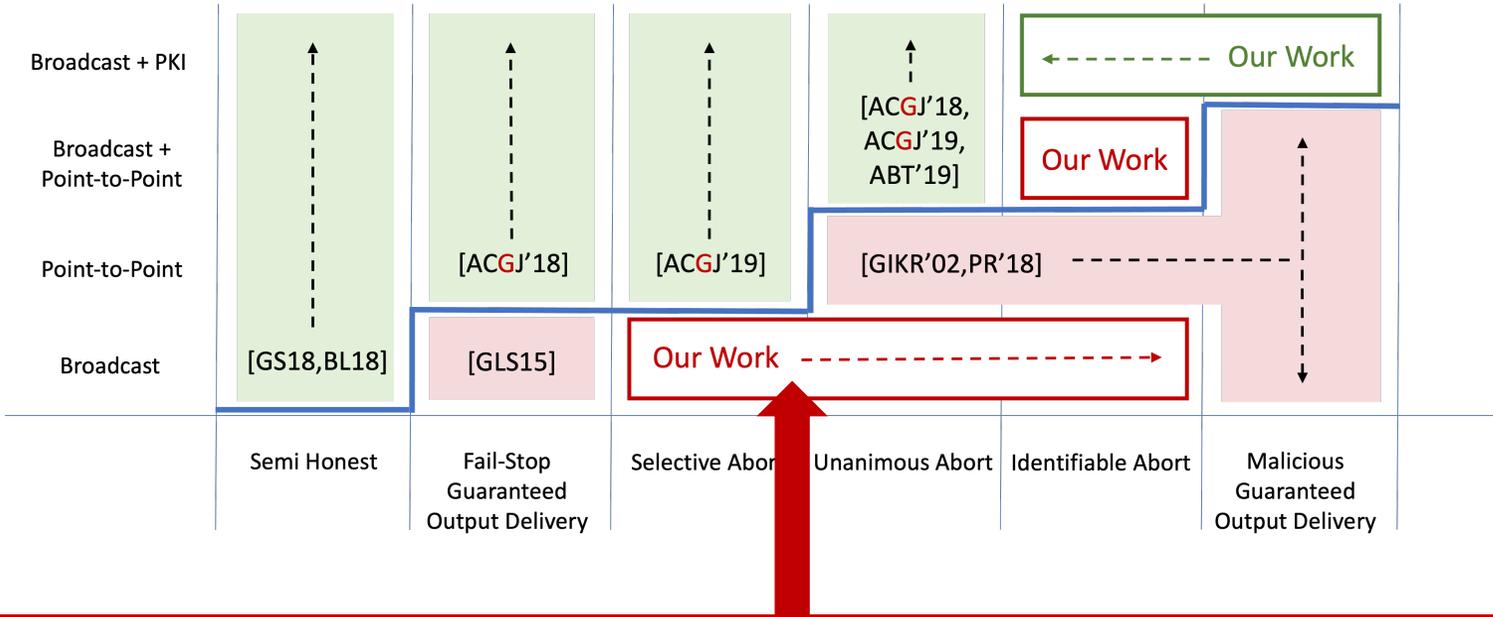
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Two-round honest-majority **semi-honest/malicious** MPC over broadcast channels  
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Two-message **malicious** OT is **impossible** in the plain model

# Our Contributions



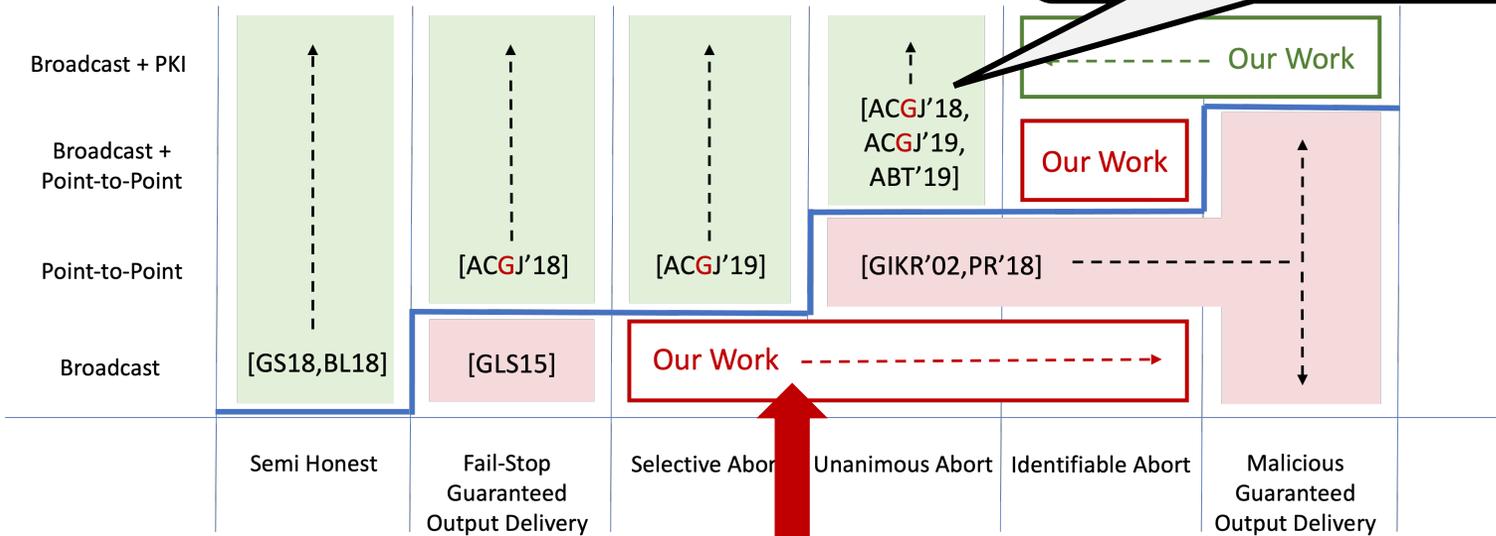
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+

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# Our Contributions

Use of P2P channels in these works was necessary



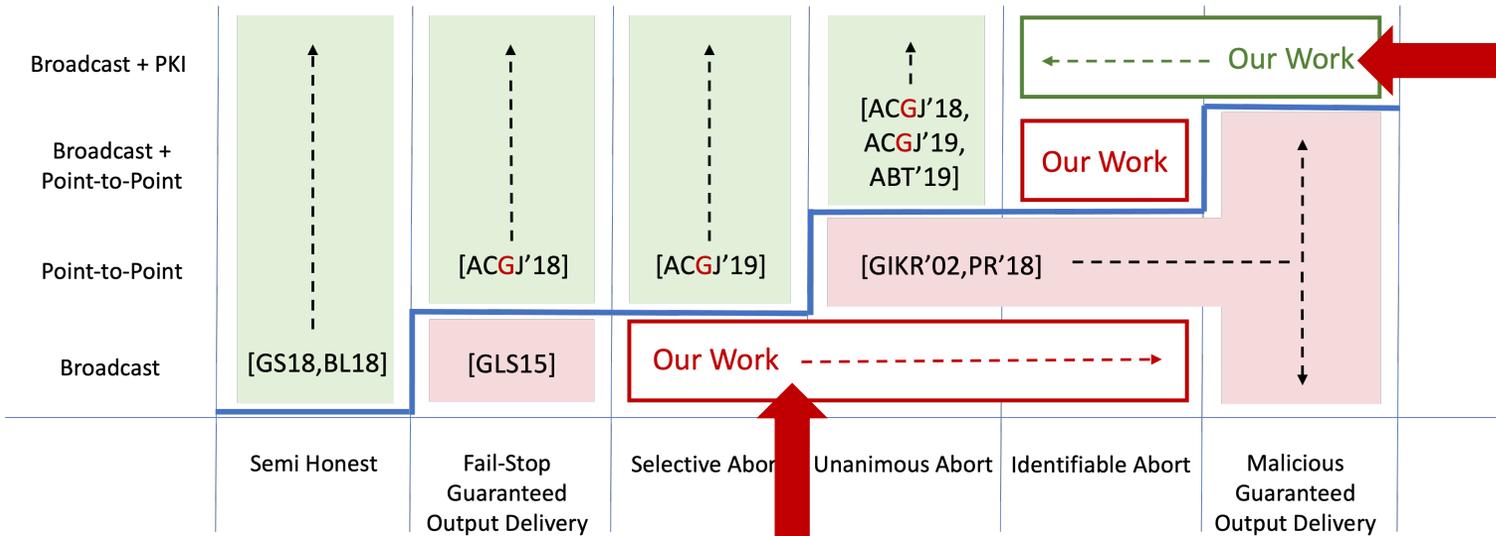
Two-round honest-majority **semi-honest/malicious** MPC over broadcast channels  
 $\Rightarrow$  **semi-honest/malicious** two-message OT

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Two-message **malicious** OT is **impossible** in the plain model

Establishes equivalence of honest majority and dishonest majority in this setting

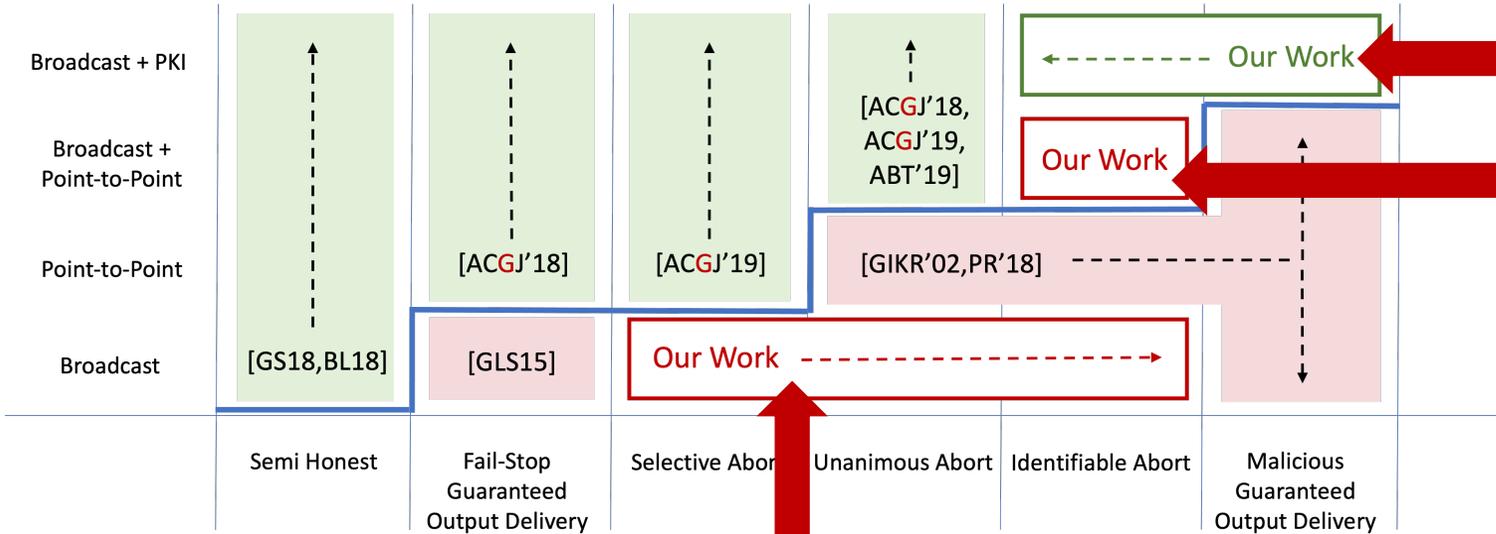
# Our Contributions



A two-round guaranteed output delivery protocol using PKE and multi-CRS NIZKs in broadcast + PKI setting for  $t < n/2$

Two-round honest-majority semi-honest/malicious MPC over broadcast channels  
 ⇒ semi-honest/malicious two-message OT  
 +  
 Two-message malicious OT is impossible in the plain model

# Our Contributions



A two-round **guaranteed output delivery** protocol using **PKE** and **multi-CRS NIZKs** in **broadcast + PKI** setting for  $t < n/2$

A two-round protocol with **identifiable abort** with  $t < n/2$  is **impossible** over **broadcast + P2P** channels in the plain model

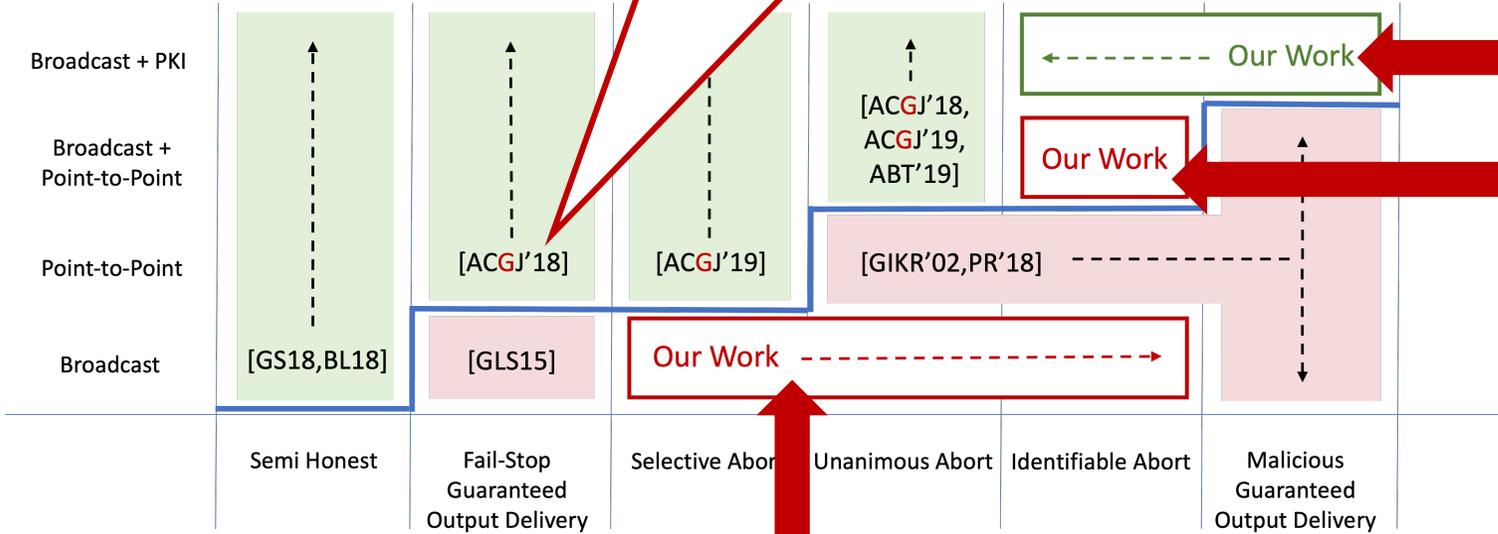
Two-round honest-majority **semi-honest/malicious** MPC over broadcast channels  
 $\Rightarrow$  **semi-honest/malicious** two-message OT

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Two-message **malicious** OT is **impossible** in the plain model

# Our Con

We also show that for  $\frac{n}{3} < t < \frac{n}{2}$ ,  
fail-stop guaranteed output  
delivery implies OT!

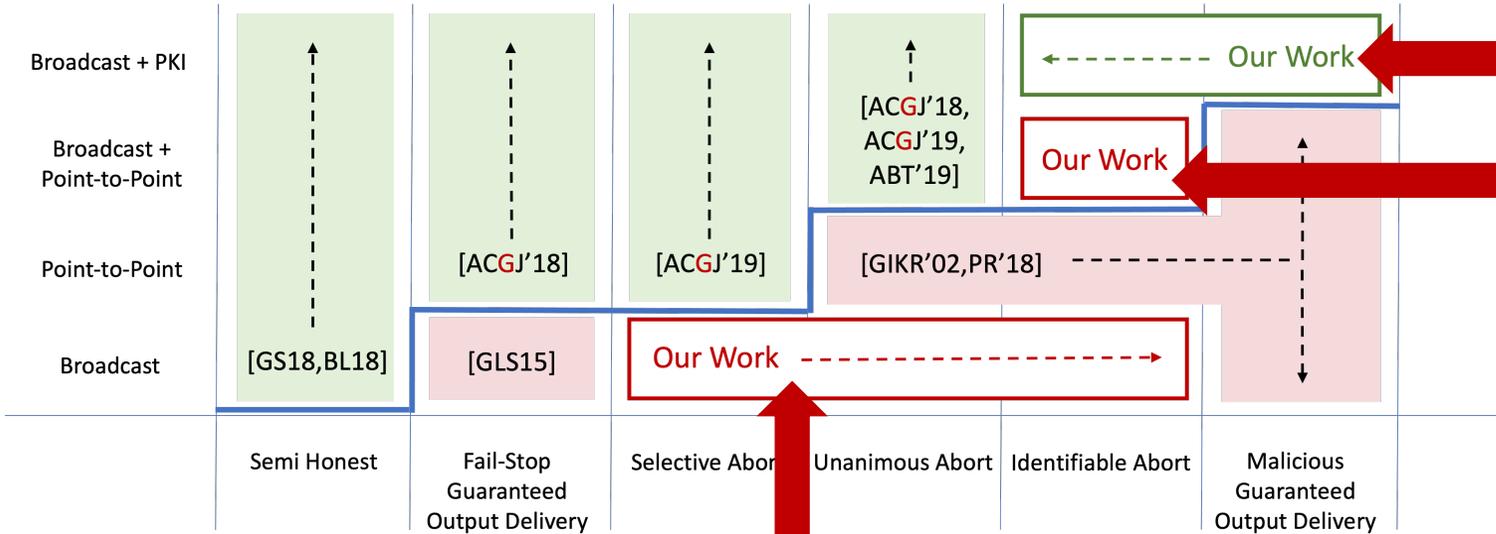


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Two-round honest-majority semi-honest/malicious MPC over broadcast channels  
 $\Rightarrow$  semi-honest/malicious two-message OT  
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 Two-message malicious OT is impossible in the plain model

# Our Contributions



A two-round **guaranteed output delivery** protocol using **PKE** and **multi-CRS NIZKs** in **broadcast + PKI** setting for  $t < n/2$

A two-round protocol with **identifiable abort** with  $t < n/2$  is **impossible** over **broadcast + P2P** channels in the plain model

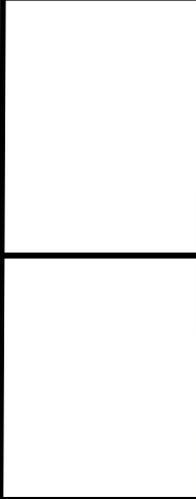
Two-round honest-majority **semi-honest/malicious** MPC over broadcast channels  
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+

Two-message **malicious** OT is **impossible** in the plain model

# Our Main Ideas

# Talk Outline

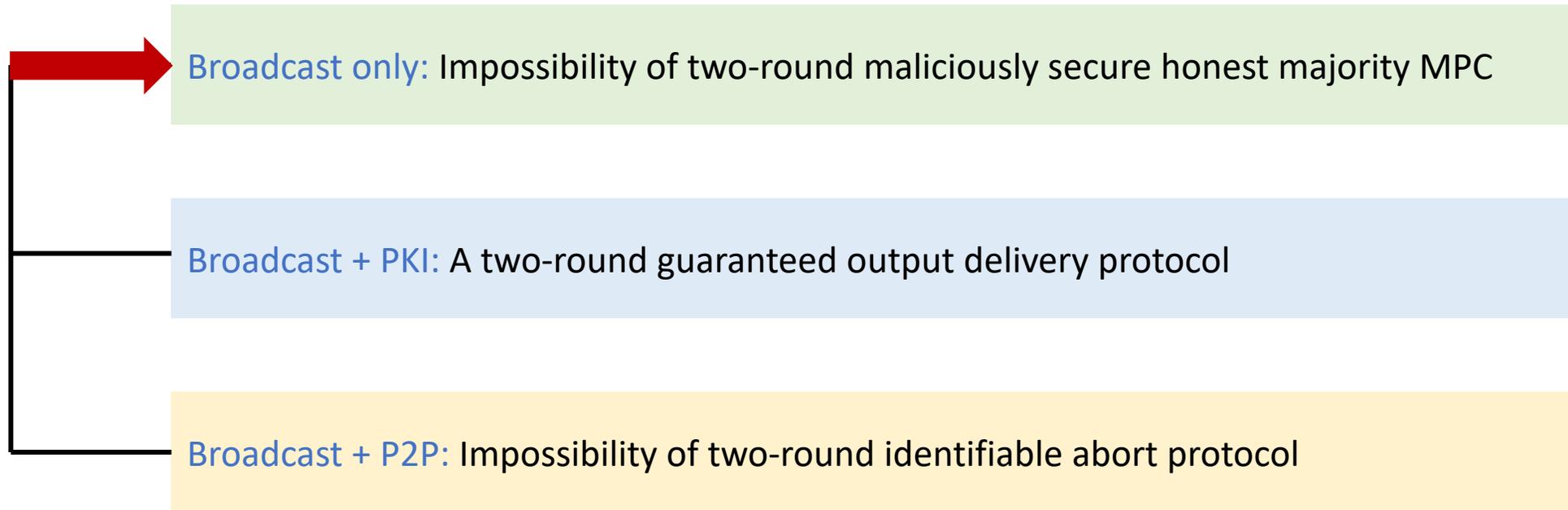


**Broadcast only:** Impossibility of two-round maliciously secure honest majority MPC

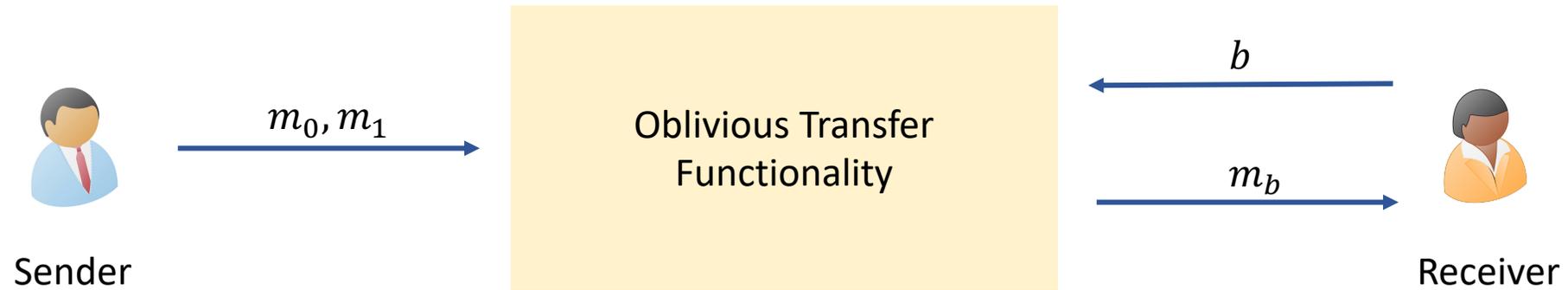
**Broadcast + PKI:** A two-round guaranteed output delivery protocol

**Broadcast + P2P:** Impossibility of two-round identifiable abort protocol

# Talk Outline



# Oblivious Transfer



# Broadcast-Only: Two-Round MPC implies OT

Two-round broadcast-only MPC

Alice

Bob

Charlie

Round 1



Round 2



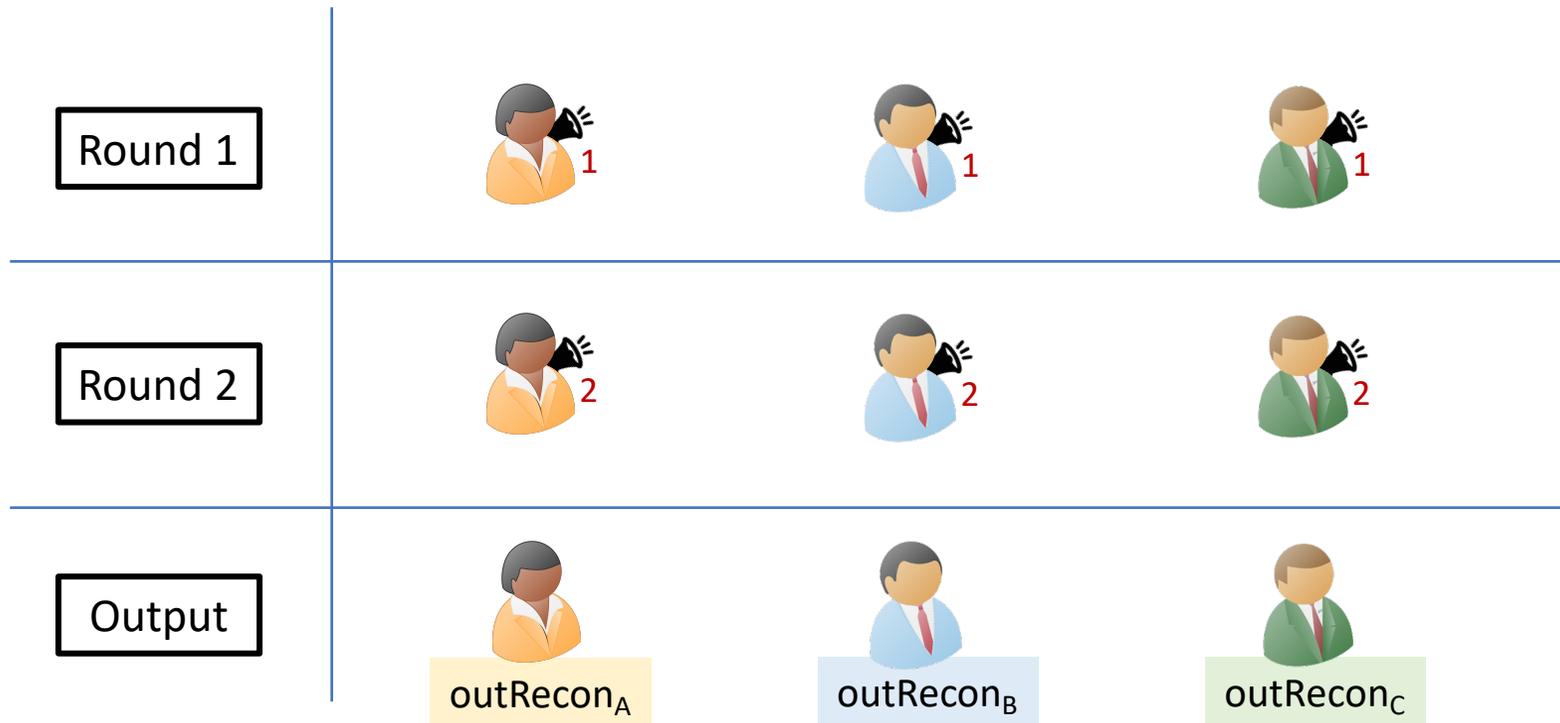
Output



# Broadcast-Only: Two-Round MPC implies OT

Two-round broadcast-only MPC for

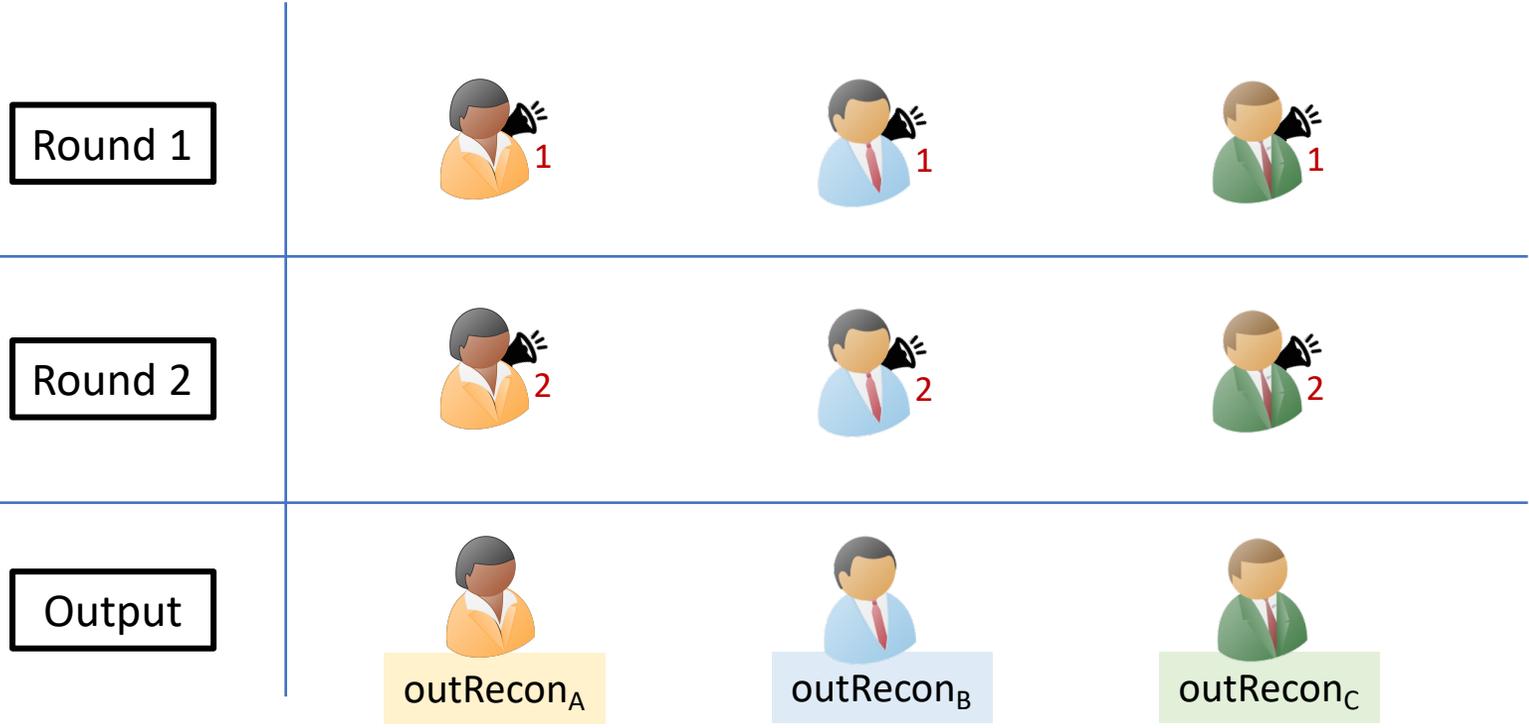
$$F\left(\begin{array}{c} \text{Person A} \\ b \end{array}, \begin{array}{c} \text{Person B} \\ m_0, m_1 \end{array}, \begin{array}{c} \text{Person C} \\ \perp \end{array}\right) = \begin{array}{c} \text{Person A} \\ m_b \end{array}, \begin{array}{c} \text{Person B} \\ \perp \end{array}, \begin{array}{c} \text{Person C} \\ \perp \end{array}$$



# Broadcast-Only: Two-Round MPC implies OT

Receiver      Sender      Helper

$$F\left(\begin{array}{c} \text{Receiver} \\ b \end{array}, \begin{array}{c} \text{Sender} \\ m_0, m_1 \end{array}, \begin{array}{c} \text{Helper} \\ \perp \end{array}\right) = \begin{array}{c} \text{Receiver} \\ m_b \end{array}, \begin{array}{c} \text{Sender} \\ \perp \end{array}, \begin{array}{c} \text{Helper} \\ \perp \end{array}$$

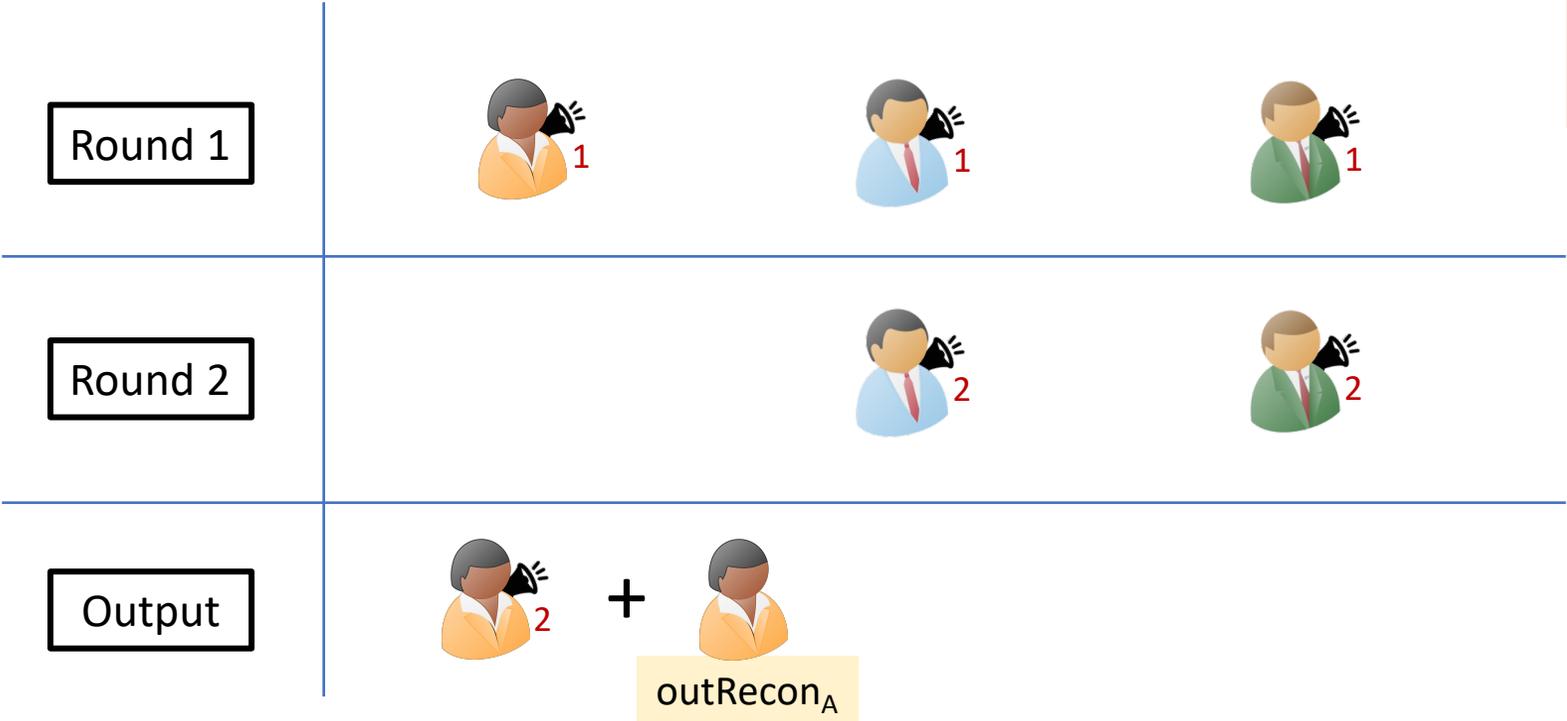


# Broadcast-Only: Two-Round MPC implies OT

Two-round broadcast-only MPC for

$$F\left(\begin{array}{c} \text{Alice} \\ b \end{array}, \begin{array}{c} \text{Bob} \\ m_0, m_1 \end{array}, \begin{array}{c} \text{Charlie} \\ \perp \end{array}\right) = \begin{array}{c} \text{Alice} \\ m_b \end{array}, \begin{array}{c} \text{Bob} \\ \perp \end{array}, \begin{array}{c} \text{Charlie} \\ \perp \end{array}$$

Since Alice is the only "output-party", it does not need to broadcast its second-round message

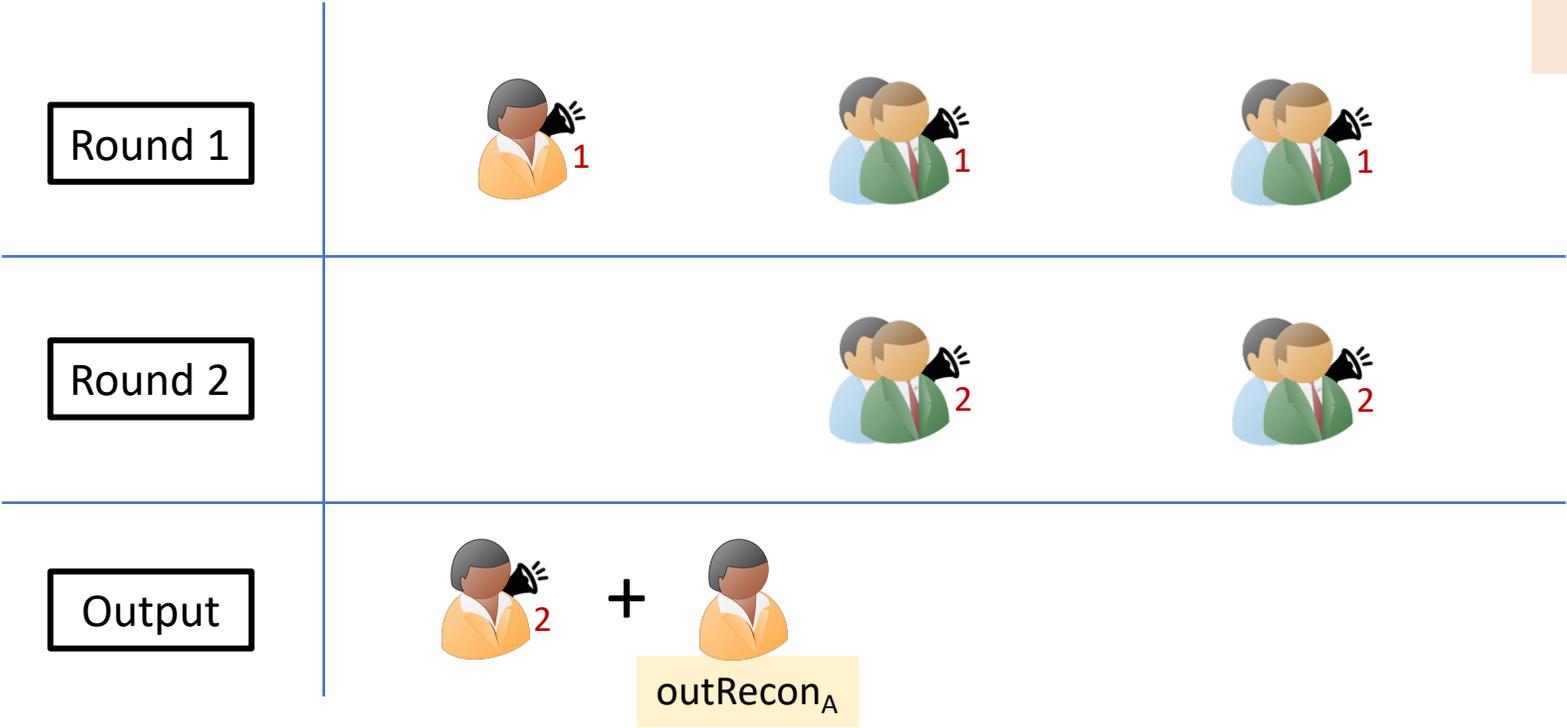


# Broadcast-Only: Two-Round MPC implies OT

Two-round broadcast-only MPC for

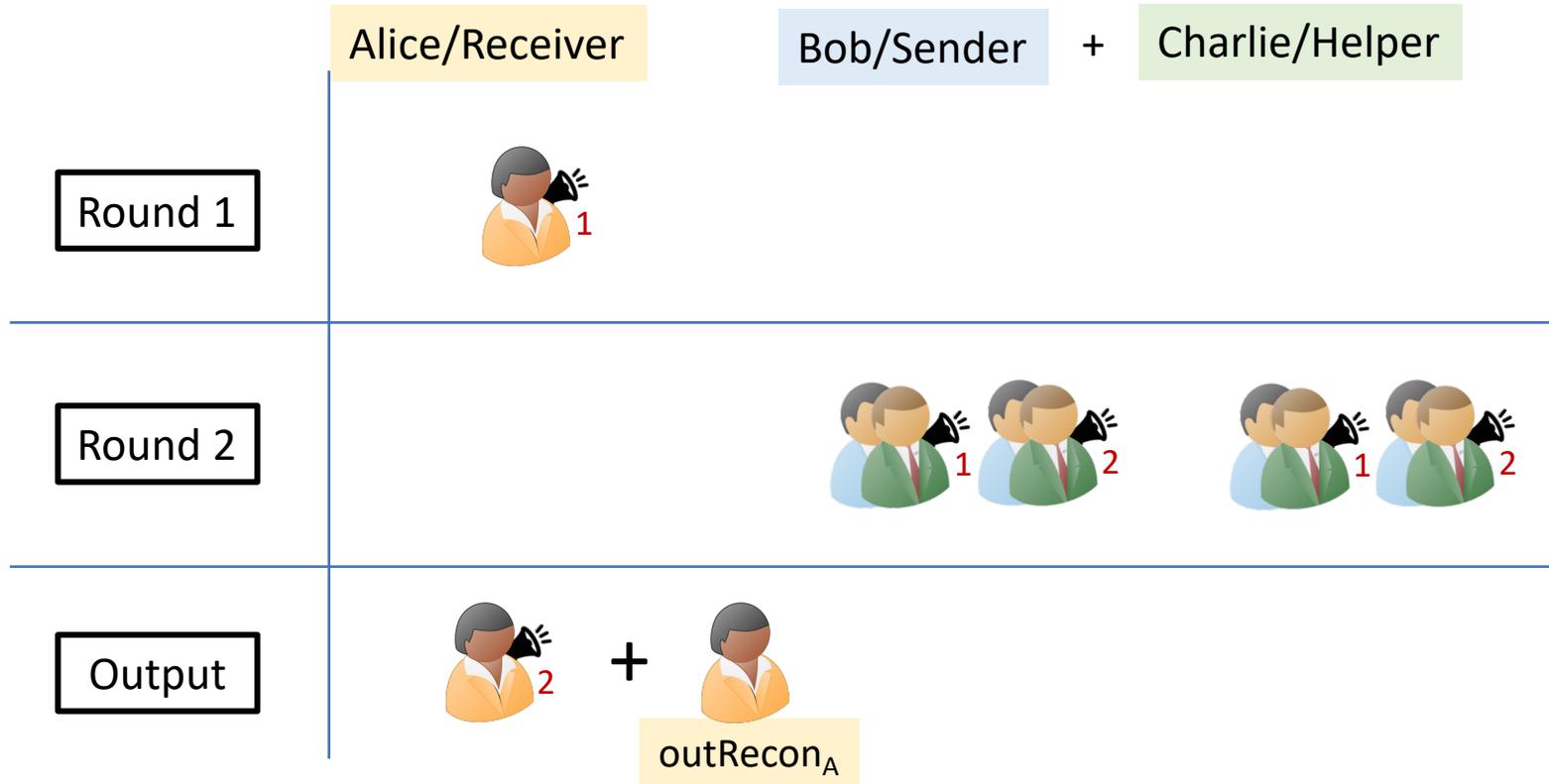
$$F\left(\begin{matrix} \text{Alice} \\ b \end{matrix}, \begin{matrix} \text{Bob, Charlie} \\ m_0, m_1 \end{matrix}\right) = \left(\begin{matrix} \text{Alice} \\ m_b \end{matrix}, \begin{matrix} \text{Bob, Charlie} \\ \perp \end{matrix}\right)$$

Modification: Bob and Charlie operate as a single party.



# Two-Message OT

$$F\left(\begin{array}{c} \text{Alice} \\ b \end{array}, \begin{array}{c} \text{Bob + Charlie} \\ m_0, m_1 \end{array}\right) = \left(\begin{array}{c} \text{Alice} \\ m_b \end{array}, \begin{array}{c} \text{Bob + Charlie} \\ \perp \end{array}\right)$$



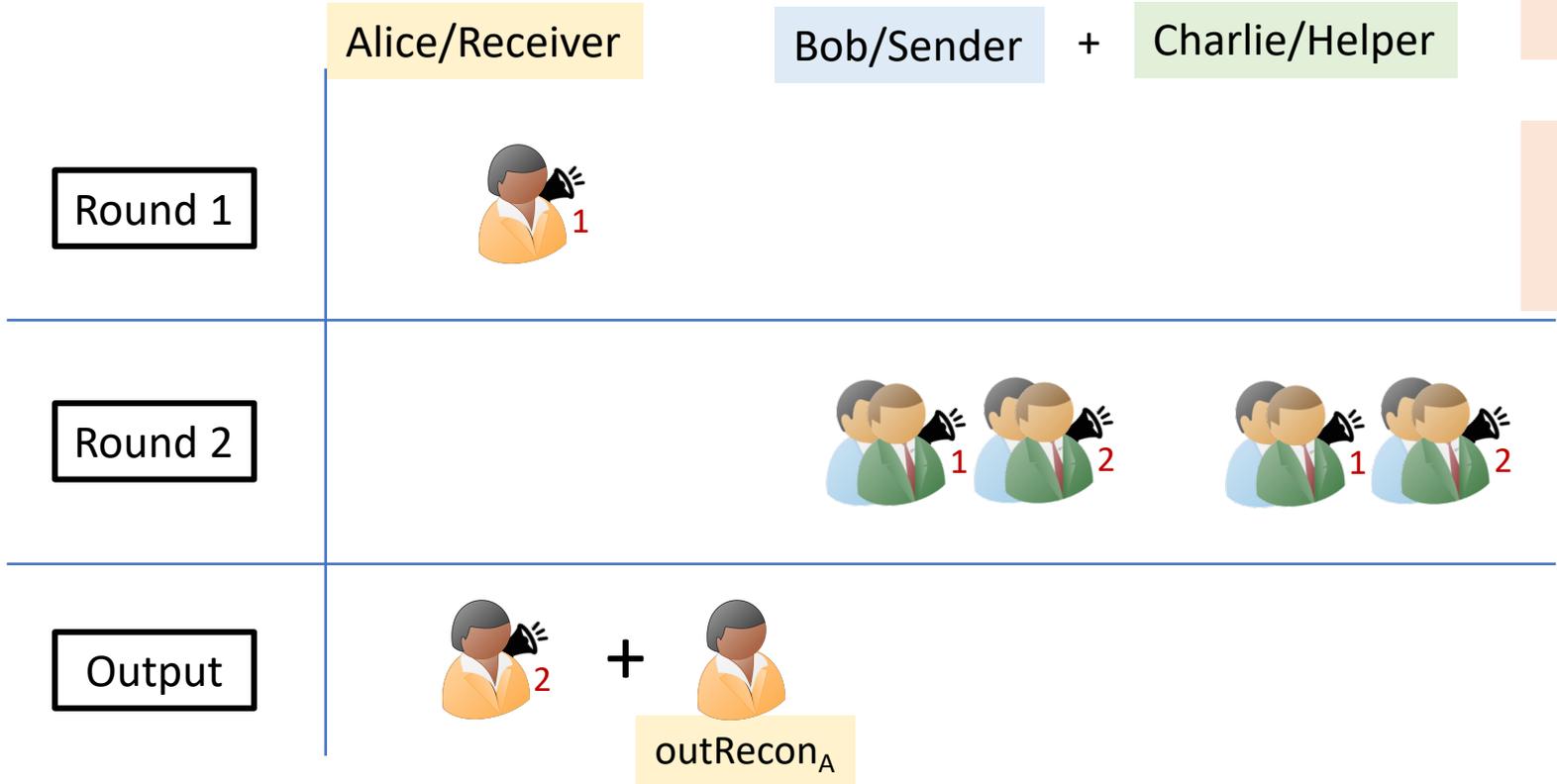
If Bob + Charlie are a single entity, they can broadcast all their messages together in the second round.

# Two-Message OT: Security against Receiver

$$F\left(\begin{array}{c} \text{Alice} \\ b \end{array}, \begin{array}{c} \text{Bob} \\ m_0, m_1 \end{array}\right) = \left(\begin{array}{c} \text{Alice} \\ m_b \end{array}, \begin{array}{c} \text{Bob} \\ \perp \end{array}\right)$$

Security against receiver follows from security of the original two-round MPC

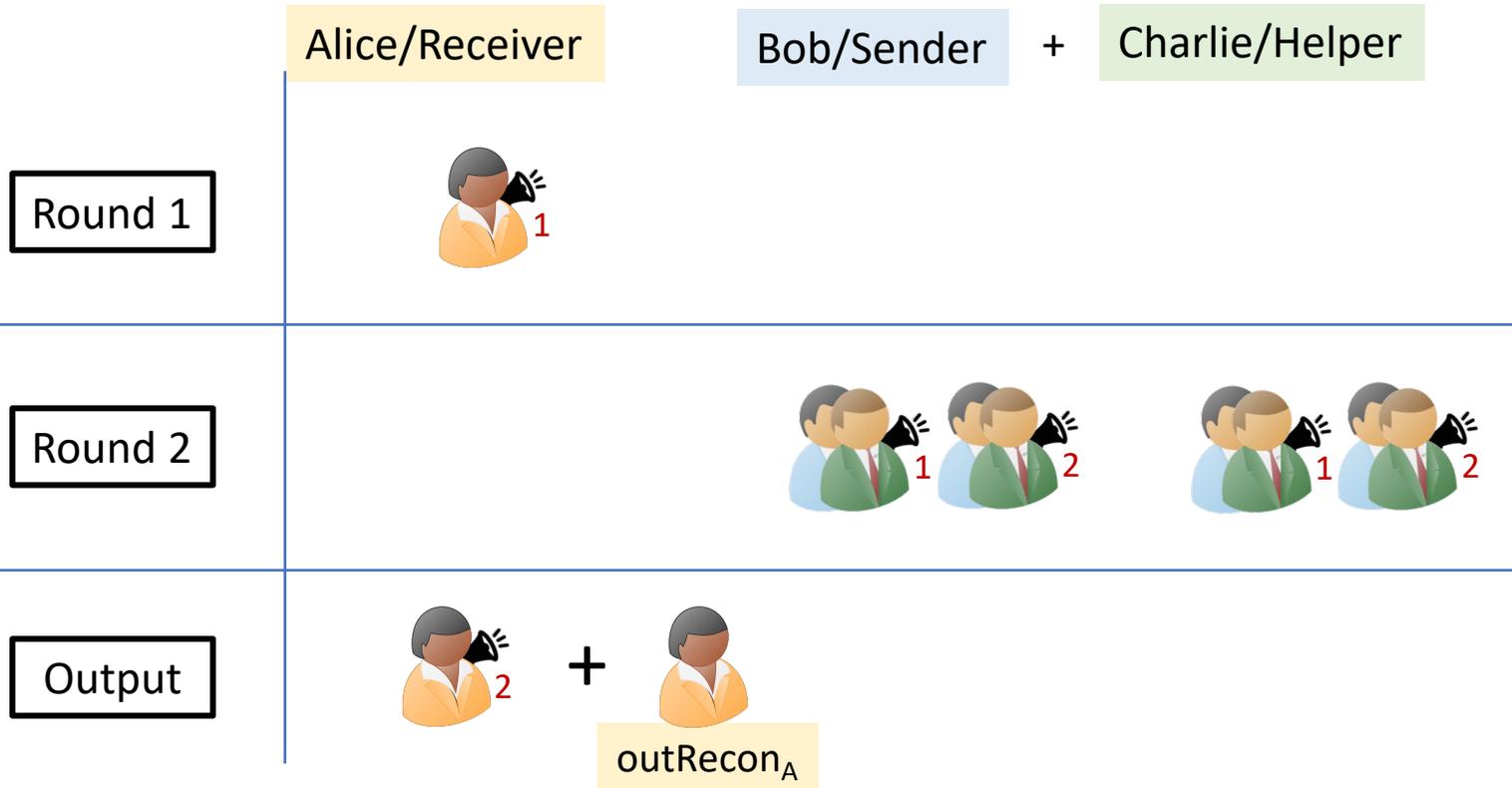
If the original MPC protocol was *semi-honest/malicious*, we get security against *semi-honest/malicious* receiver



# Two-Message OT: Security against **Sender**

$$F\left(\begin{array}{c} \text{Alice} \\ b \end{array}, \begin{array}{c} \text{Bob} \\ m_0, m_1 \end{array}\right) = \left(\begin{array}{c} \text{Alice} \\ m_b \end{array}, \begin{array}{c} \text{Bob} \\ \perp \end{array}\right)$$

Charlie did not have an input in the original function



If the adversary only corrupts Bob in the original protocol, it can obtain the same view as in this transformed 2-party protocol, by internally simulating Charlie.

We get security against **semi-honest sender**

# Two-Message OT

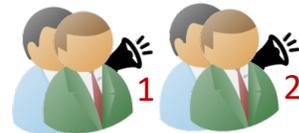
$$F\left(\begin{array}{c} \text{Alice} \\ b \end{array}, \begin{array}{c} \text{Bob} \\ m_0, m_1 \end{array}\right) = \left(\begin{array}{c} \text{Alice} \\ m_b \end{array}, \begin{array}{c} \text{Bob} \\ \perp \end{array}\right)$$

Alice/Receiver      Bob/Sender + Charlie/Helper

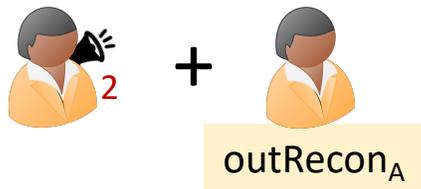
Round 1



Round 2



Output

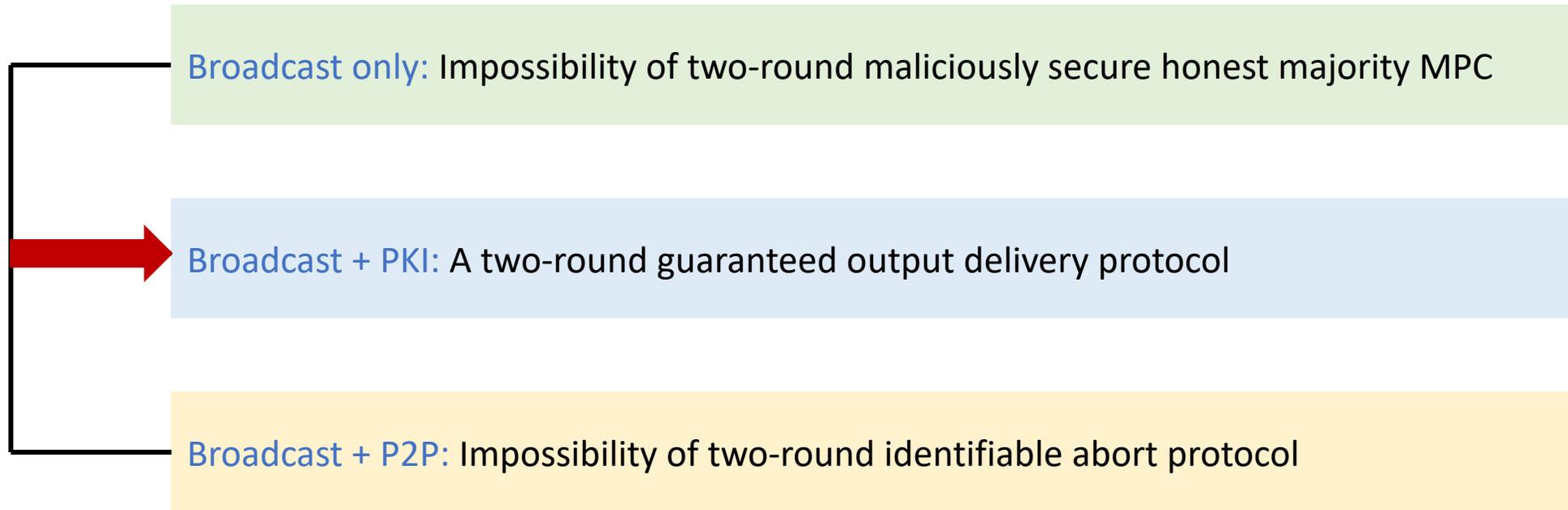


A maliciously secure broadcast-only two-round MPC  
⇒ Two-message malicious receiver OT

We show that a two-message malicious receiver OT is impossible

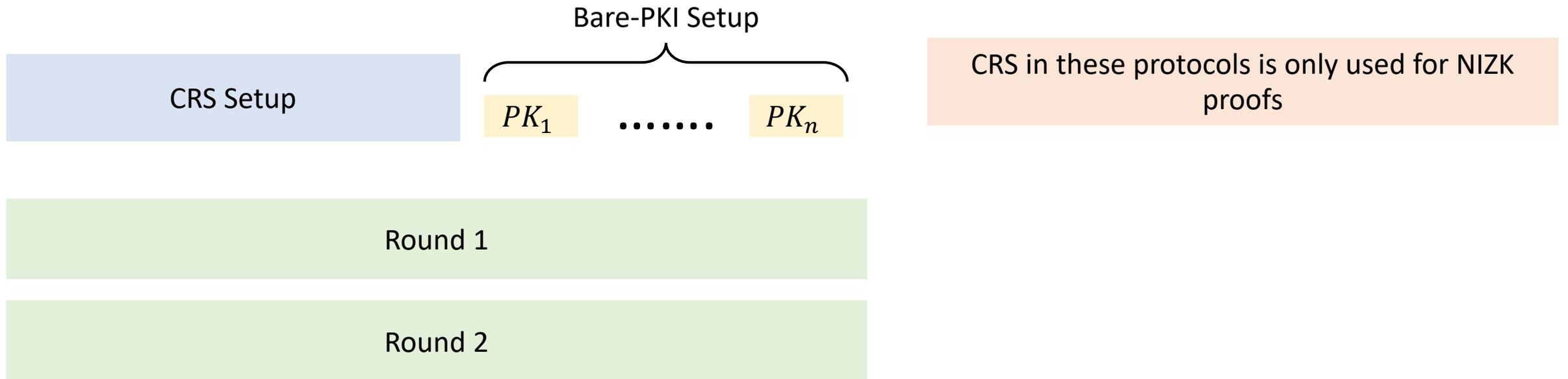
Hence, a maliciously secure broadcast-only two-round MPC is **impossible!**

# Talk Outline



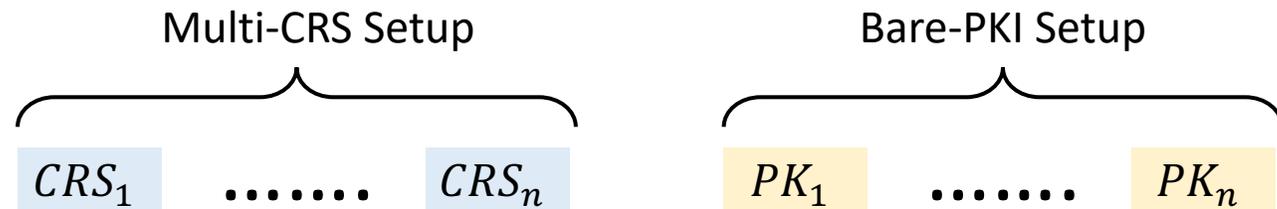
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Existing guaranteed output delivery protocols (e.g. [GLS'18]) in the broadcast + PKI setting, rely on a trusted CRS setup



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Round 1

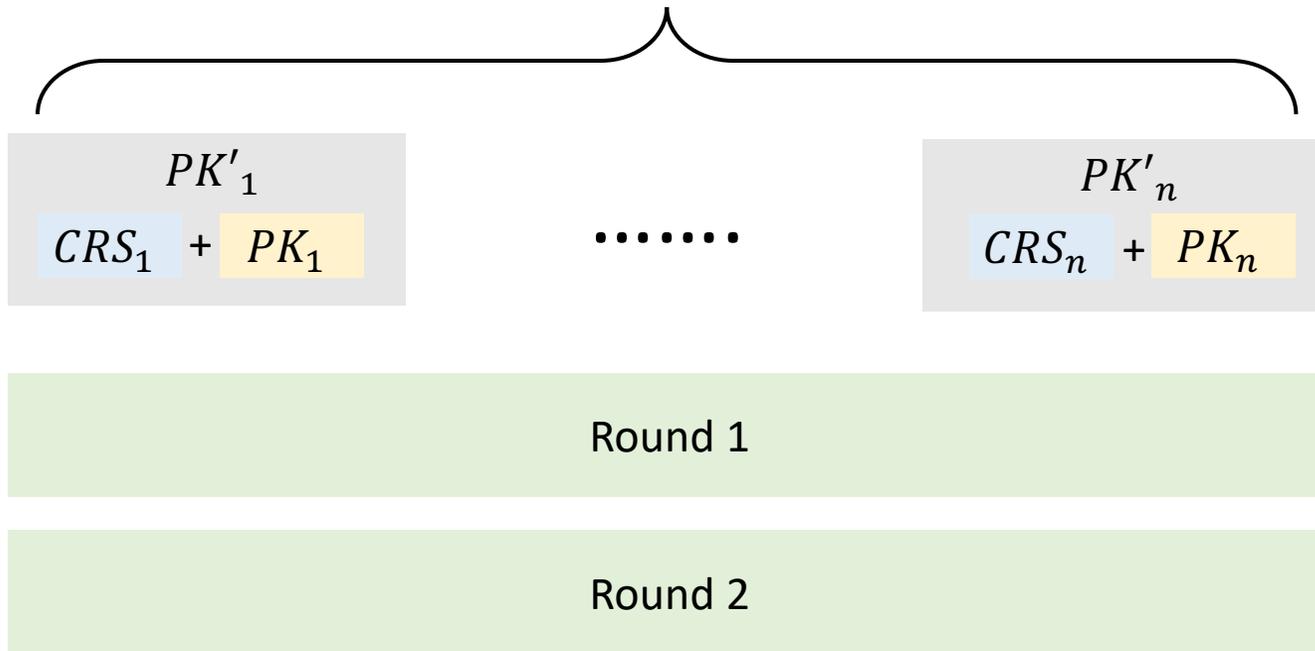
Round 2

CRS in these protocols is only used for NIZK proofs

NIZKs in the honest majority setting can be replaced with multi-CRS NIZKs [GO'07]

# Broadcast + PKI: Guaranteed Output Delivery

Existing guaranteed output delivery protocols (e.g. [GLS'18]) in the broadcast + PKI setting, rely on a trusted CRS setup



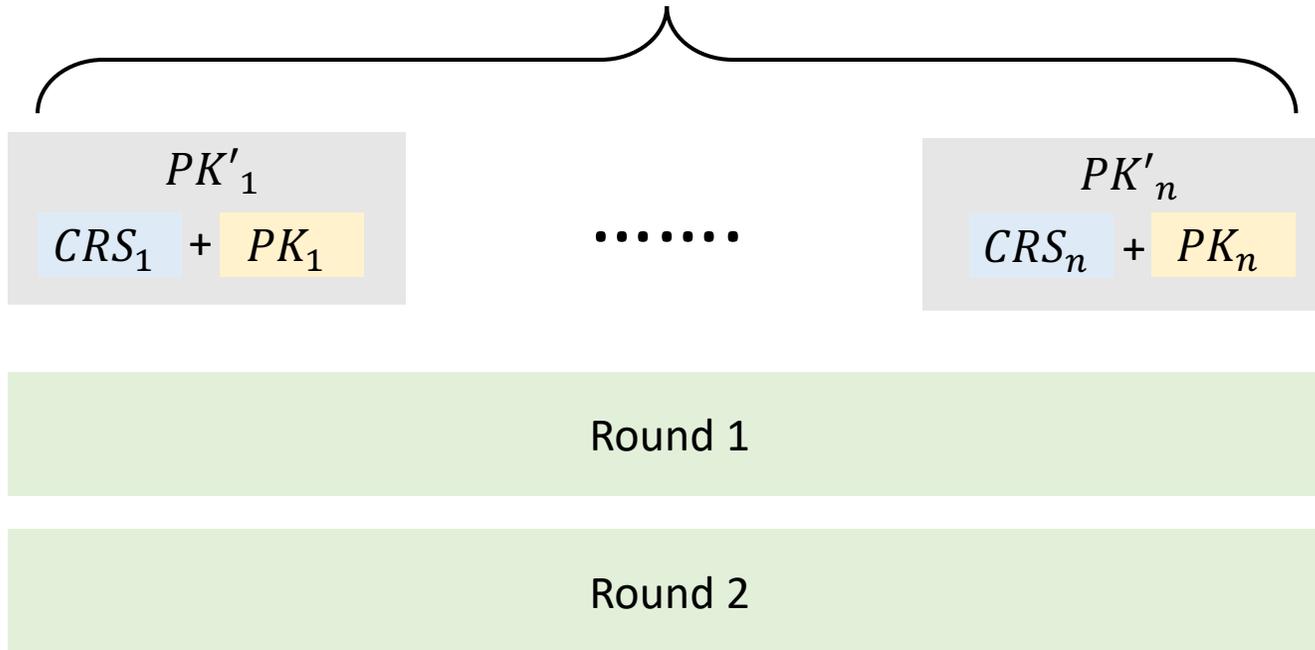
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NIZKs in the honest majority setting can be replaced with multi-CRS NIZKs [GO'07]

Multi-CRS can be embedded inside the bare-PKI setup

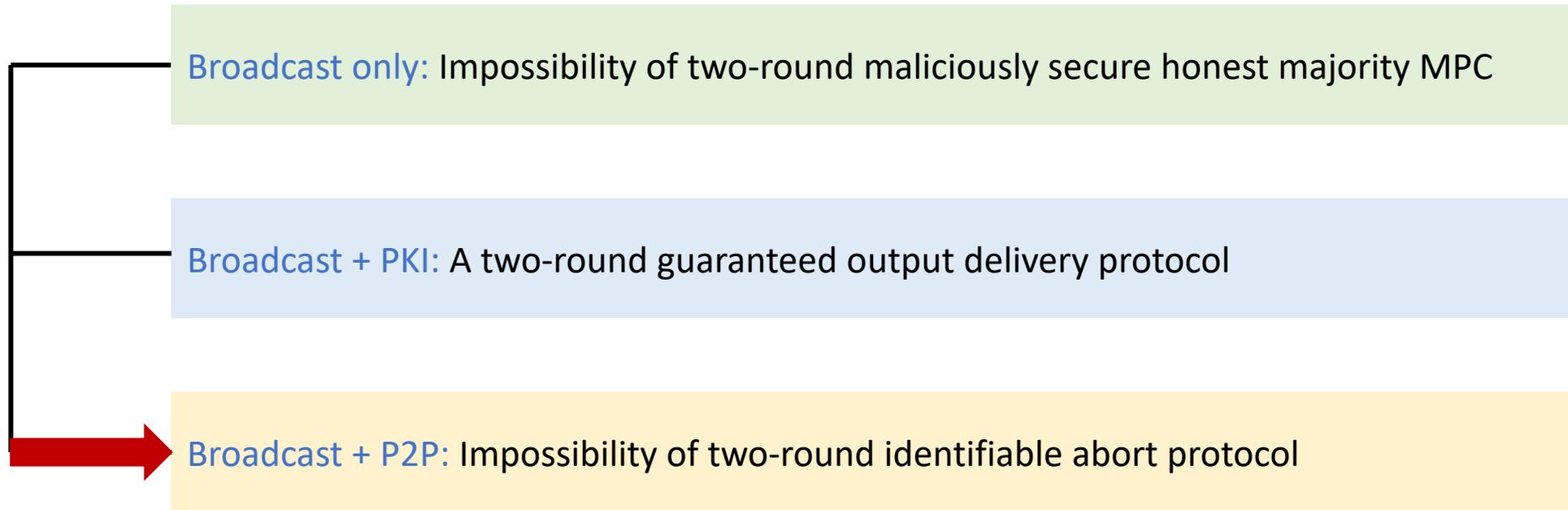
# Broadcast + PKI: Guaranteed Output Delivery

Bare-PKI Setup



This gives us a two-round guaranteed output delivery protocol without CRS!

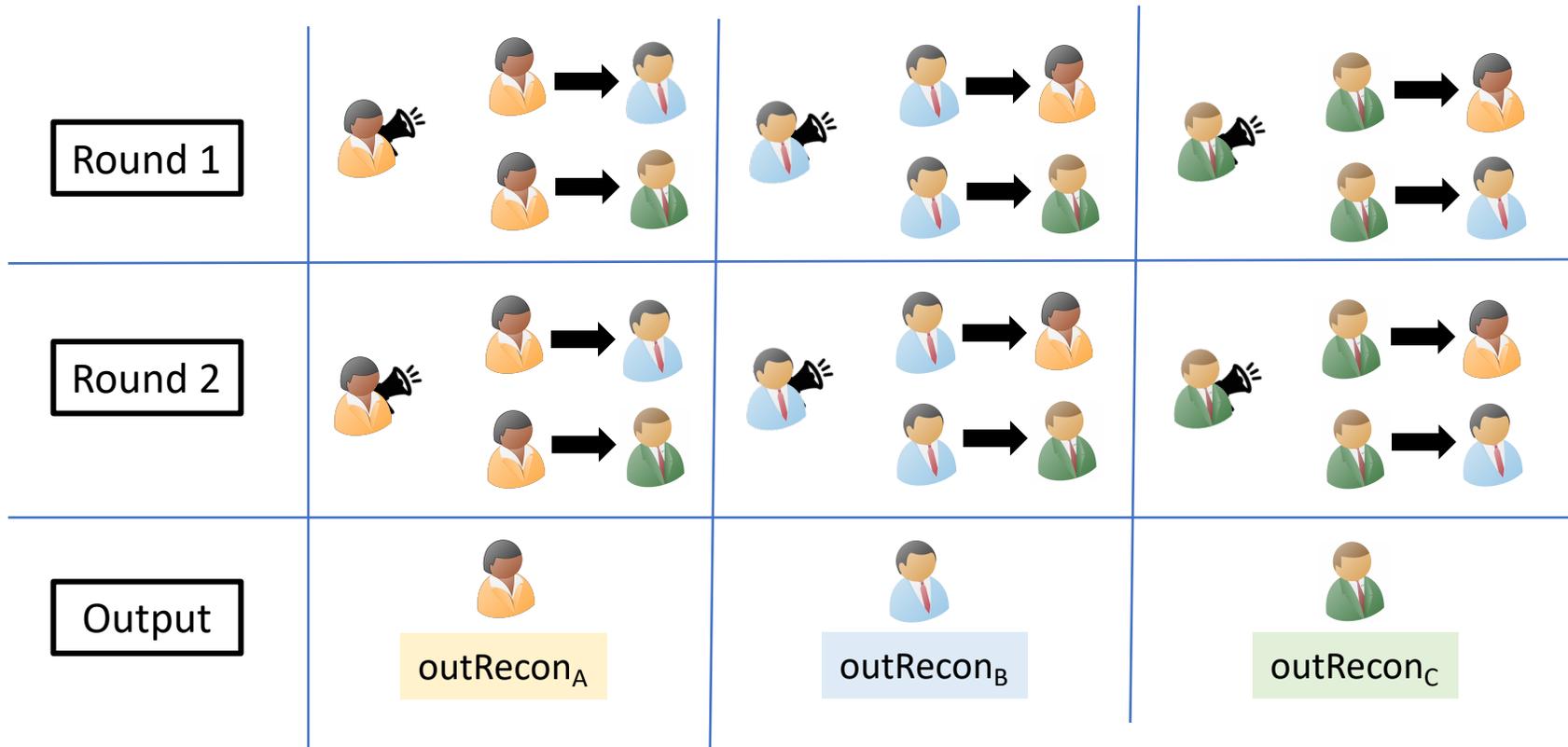
# Talk Outline



# Broadcast + P2P: Identifiable Abort is Impossible

Assume FSOC,  $\exists$  a two-round identifiable abort protocol for

$$F\left(\begin{array}{c} \text{A} \\ b \end{array}, \begin{array}{c} \text{B} \\ m_0, m_1 \end{array}, \begin{array}{c} \text{C} \\ \perp \end{array}\right) = \left(\begin{array}{c} \text{A} \\ \perp \end{array}, \begin{array}{c} \text{B} \\ \perp \end{array}, \begin{array}{c} \text{C} \\ m_b \end{array}\right)$$

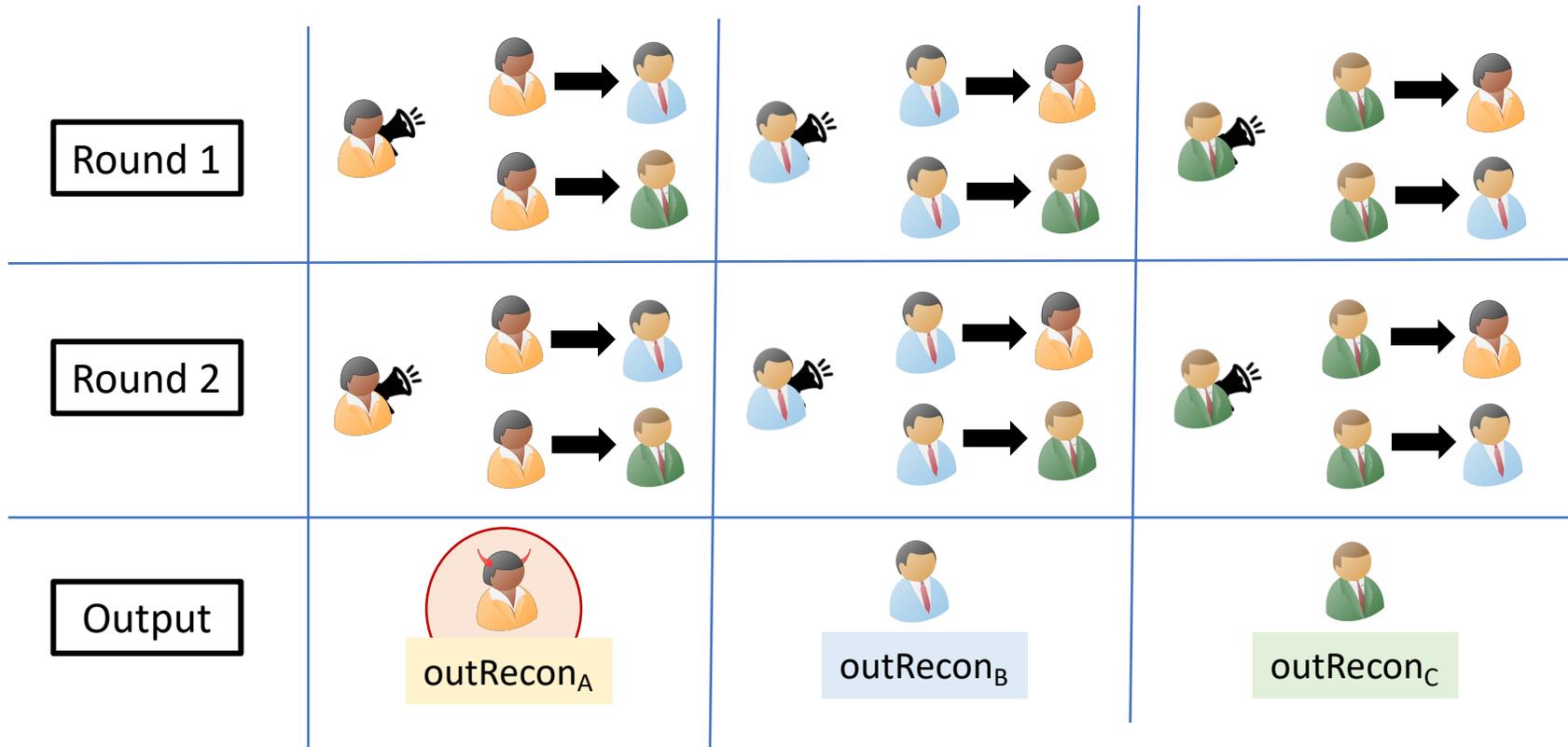


# Broadcast + P2P: Identifiable Abort is Impossible

Assume FSOC,  $\exists$  a two-round identifiable abort protocol for

$$F\left(\begin{array}{c} \text{Alice} \\ b \end{array}, \begin{array}{c} \text{Bob} \\ m_0, m_1 \end{array}, \begin{array}{c} \text{Charlie} \\ \perp \end{array}\right) = \left(\begin{array}{c} \text{Alice} \\ \perp \end{array}, \begin{array}{c} \text{Bob} \\ \perp \end{array}, \begin{array}{c} \text{Charlie} \\ m_b \end{array}\right)$$

Adversary corrupts Alice



# Broadcast + P2P: Identifiable Abort is Impossible

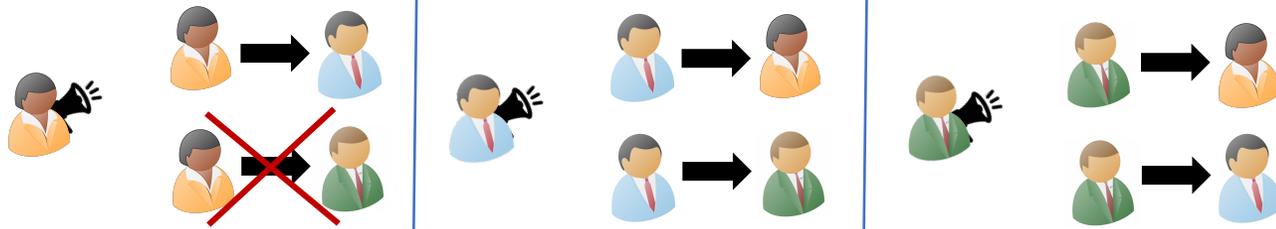
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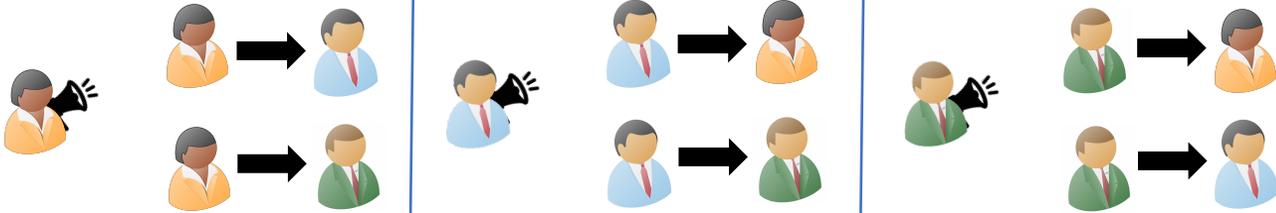
Adversary corrupts Alice

Alice doesn't send private message to Charlie

Round 1



Round 2



Output



# Broadcast + P2P: Identifiable Abort is Impossible

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$$F\left(\begin{array}{c} \text{Alice} \\ b \end{array}, \begin{array}{c} \text{Bob} \\ m_0, m_1 \end{array}, \begin{array}{c} \text{Charlie} \\ \perp \end{array}\right) = \left(\begin{array}{c} \text{Alice} \\ \perp \end{array}, \begin{array}{c} \text{Bob} \\ \perp \end{array}, \begin{array}{c} \text{Charlie} \\ m_b \end{array}\right)$$

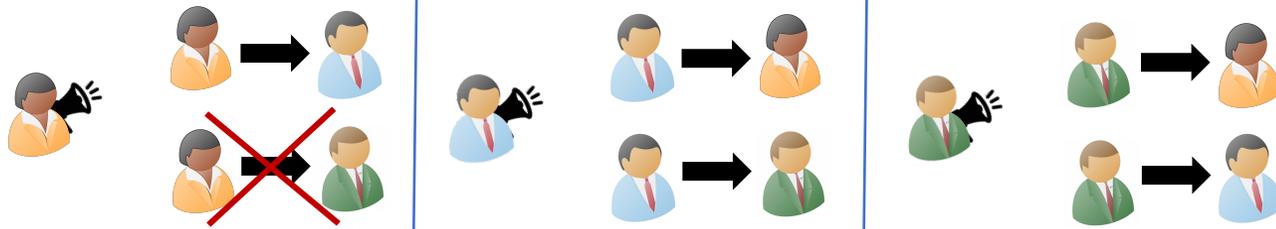
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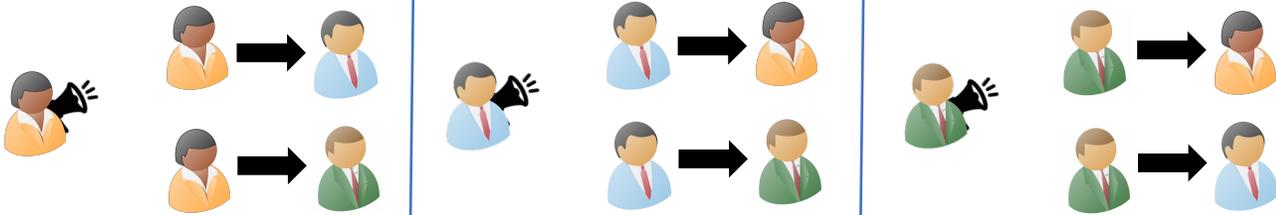
Honest parties should :

1. Either abort and identify the corrupt party
2. Or do not abort

Round 1



Round 2



Output



# Broadcast + P2P: Identifiable Abort is Impossible

Assume FSOC,  $\exists$  a two-round identifiable abort protocol for

$$F\left(\begin{array}{c} \text{Person A} \\ b \end{array}, \begin{array}{c} \text{Person B} \\ m_0, m_1 \end{array}, \begin{array}{c} \text{Person C} \\ \perp \end{array}\right) = \left(\begin{array}{c} \text{Person A} \\ \perp \end{array}, \begin{array}{c} \text{Person B} \\ \perp \end{array}, \begin{array}{c} \text{Person C} \\ m_b \end{array}\right)$$

Round 1			
Round 2			
Output	<p>outRecon<sub>A</sub></p>	<p>outRecon<sub>B</sub></p>	<p>outRecon<sub>C</sub></p>

Case 1: Lets assume the honest parties abort

If outputs  $\perp$ , then all honest parties should identify as corrupt.

But has no reason to believe why would be corrupt.

# Broadcast + P2P: Identifiable Abort is Impossible

Assume FSOC,  $\exists$  a two-round identifiable abort protocol for

$$F\left(\begin{array}{c} \text{Person A} \\ b \end{array}, \begin{array}{c} \text{Person B} \\ m_0, m_1 \end{array}, \begin{array}{c} \text{Person C} \\ \perp \end{array}\right) = \left(\begin{array}{c} \text{Person A} \\ \perp \end{array}, \begin{array}{c} \text{Person B} \\ \perp \end{array}, \begin{array}{c} \text{Person C} \\ m_b \end{array}\right)$$

Round 1			
Round 2			
Output	<p>outRecon<sub>A</sub></p>	<p>outRecon<sub>B</sub></p>	<p>outRecon<sub>C</sub></p>

~~Case 1:~~ Lets assume the honest parties abort

If outputs  $\perp$ , then all honest parties should identify as corrupt.

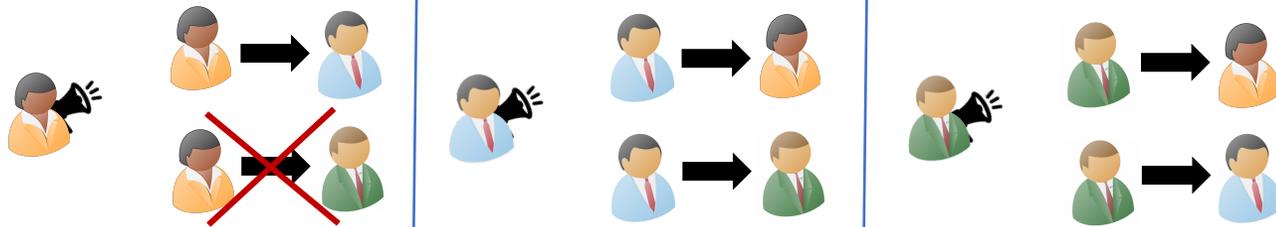
But has no reason to believe why would be corrupt.

# Broadcast + P2P: Identifiable Abort is Impossible

$$F\left(\begin{array}{c} \text{Person A} \\ b \end{array}, \begin{array}{c} \text{Person B} \\ m_0, m_1 \end{array}, \begin{array}{c} \text{Person C} \\ \perp \end{array}\right) = \left(\begin{array}{c} \text{Person A} \\ \perp \end{array}, \begin{array}{c} \text{Person B} \\ \perp \end{array}, \begin{array}{c} \text{Person C} \\ m_b \end{array}\right)$$

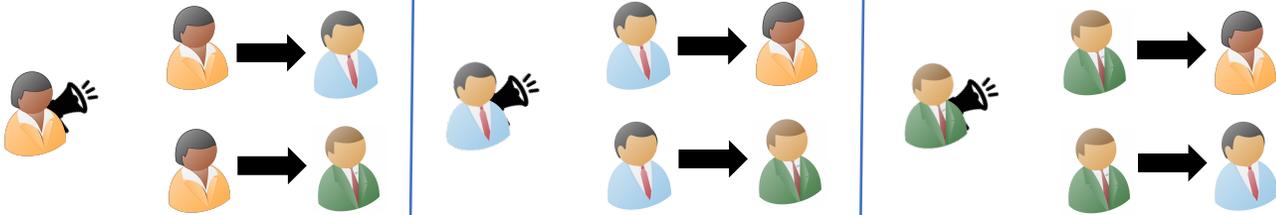
Case 2: Lets assume the honest parties **do not** abort

Round 1



1. The simulator extracts  $b$  as 's input.

Round 2



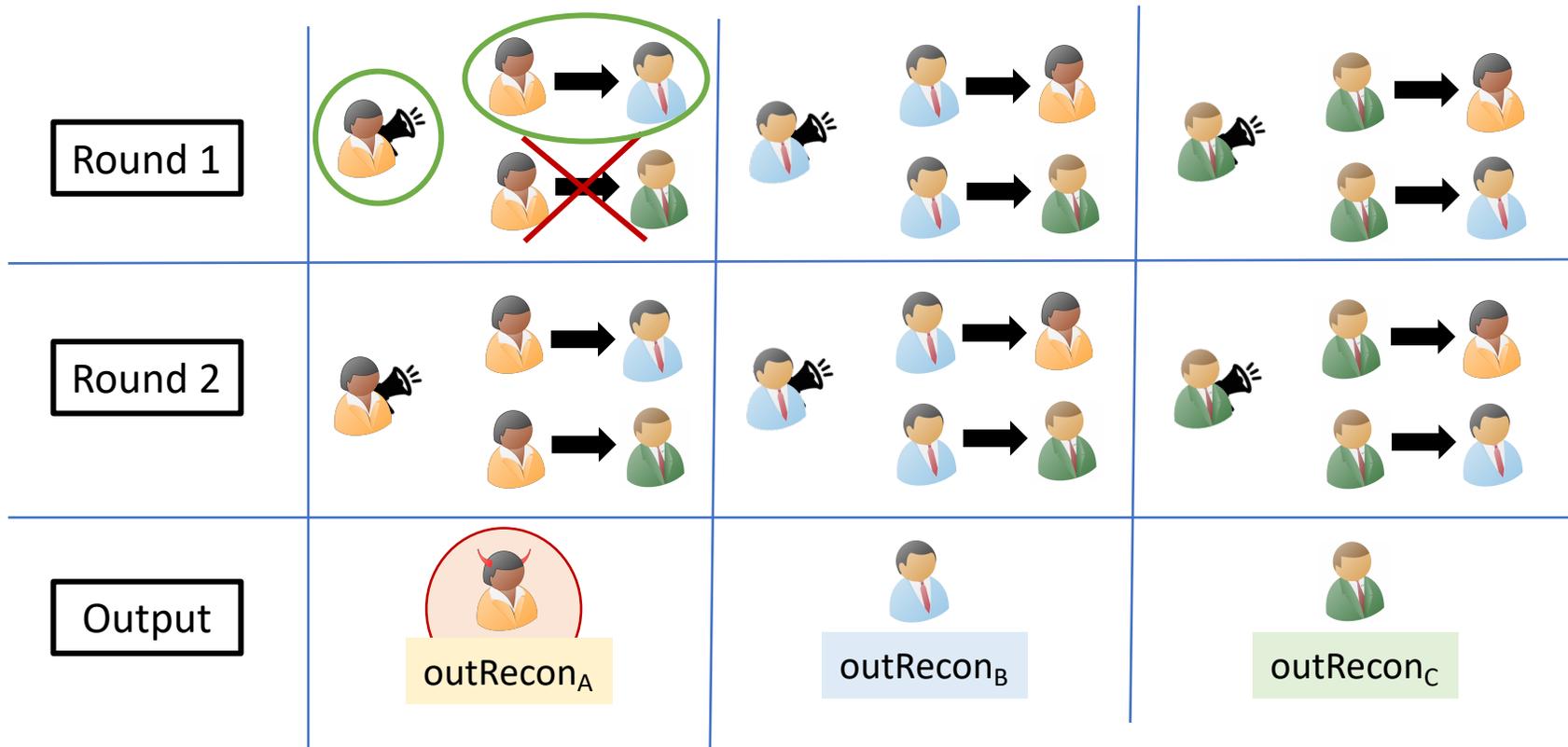
2. The simulator extracts  $1 - b$  as 's input.

Output



# Broadcast + P2P: Identifiable Abort is Impossible

$$F\left(\begin{matrix} \text{Person A} \\ b \end{matrix}, \begin{matrix} \text{Person B} \\ m_0, m_1 \end{matrix}, \begin{matrix} \text{Person C} \\ \perp \end{matrix}\right) = \left(\begin{matrix} \text{Person A} \\ \perp \end{matrix}, \begin{matrix} \text{Person B} \\ \perp \end{matrix}, \begin{matrix} \text{Person C} \\ m_b \end{matrix}\right)$$



Case 2: Lets assume the honest parties **do not** abort

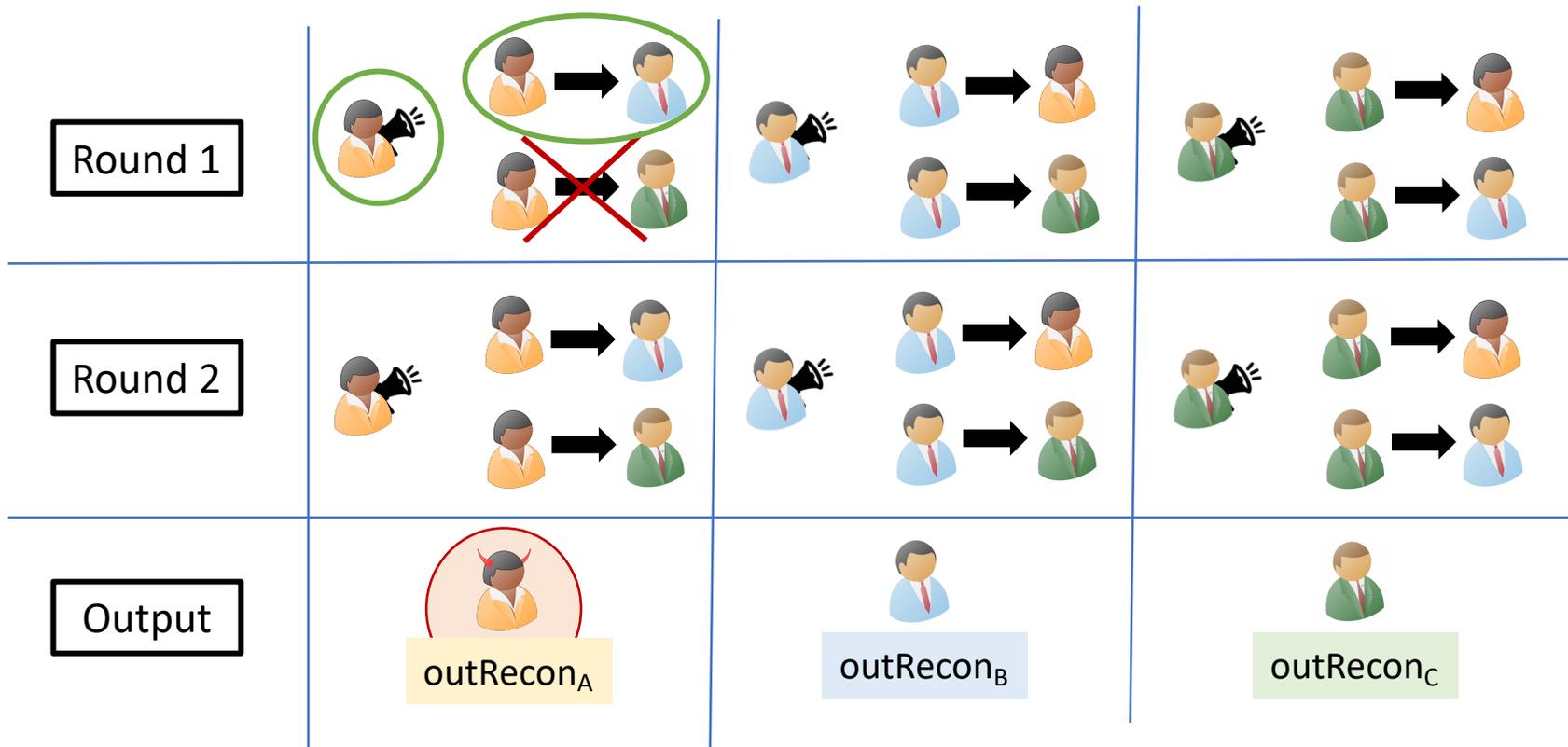
1. The simulator extracts  $b$  as Person A's input.

A corrupt Person B can use the same simulator algorithm to violate Person A's privacy

2. The simulator extracts  $1 - b$  as Person A's input.

# Broadcast + P2P: Identifiable Abort is Impossible

$$F\left(\begin{matrix} \text{Person A} \\ b \end{matrix}, \begin{matrix} \text{Person B} \\ m_0, m_1 \end{matrix}, \begin{matrix} \text{Person C} \\ \perp \end{matrix}\right) = \left(\begin{matrix} \text{Person A} \\ \perp \end{matrix}, \begin{matrix} \text{Person B} \\ \perp \end{matrix}, \begin{matrix} \text{Person C} \\ m_b \end{matrix}\right)$$



Case 2: Lets assume the honest parties **do not** abort

1. ~~The simulator extracts  $b$  as  's input.~~

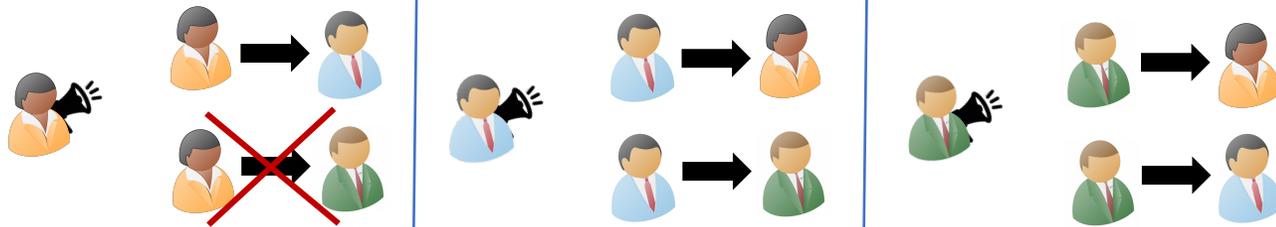
A corrupt  can use the same simulator algorithm to violate  's privacy

2. The simulator extracts  $1 - b$  as  's input.

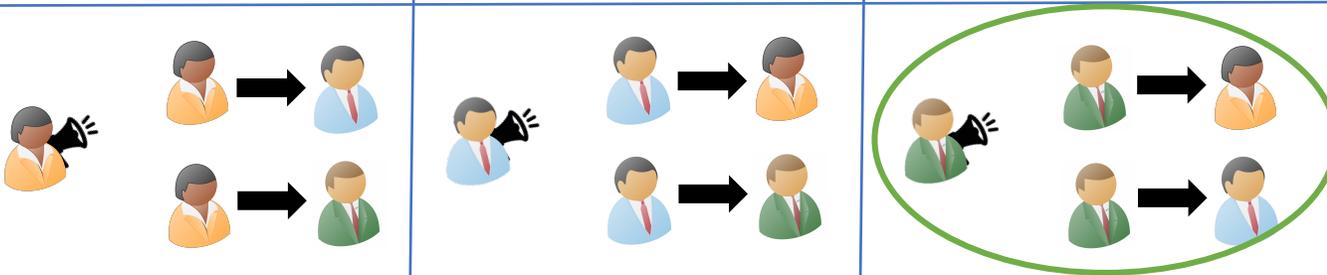
# Broadcast + P2P: Identifiable Abort is Impossible

$$F\left(\begin{matrix} \text{Person A} \\ b \end{matrix}, \begin{matrix} \text{Person B} \\ m_0, m_1 \end{matrix}, \begin{matrix} \text{Person C} \\ \perp \end{matrix}\right) = \left(\begin{matrix} \text{Person A} \\ \perp \end{matrix}, \begin{matrix} \text{Person B} \\ \perp \end{matrix}, \begin{matrix} \text{Person C} \\ m_b \end{matrix}\right)$$

Round 1



Round 2



Output



Case 2: Lets assume the honest parties **do not** abort

1. ~~The simulator extracts  $b$  as Person A's input.~~

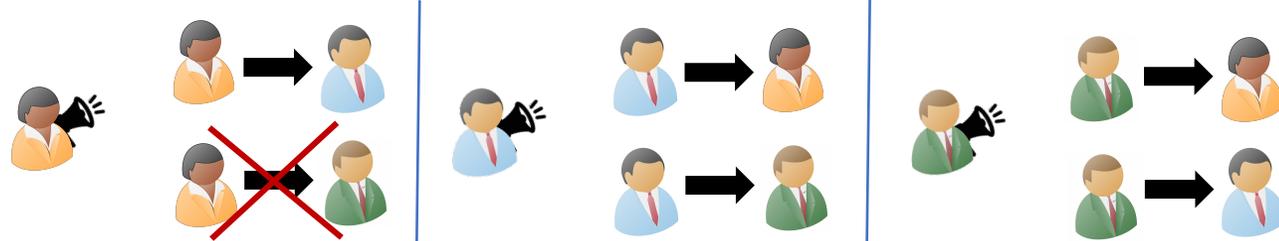
2. The simulator extracts  $1 - b$  as Person A's input.

A corrupt Person C can launch a residual function attack to violate Person A's privacy

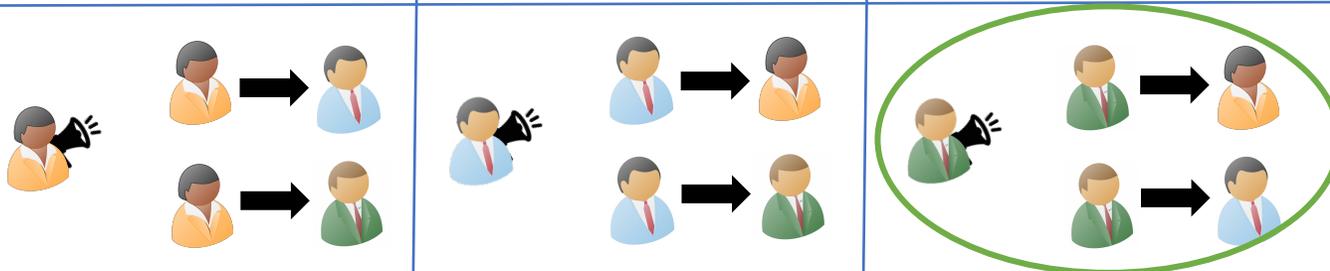
# Broadcast + P2P: Identifiable Abort is Impossible

$$F\left(\begin{matrix} \text{Person A} \\ b \end{matrix}, \begin{matrix} \text{Person B} \\ m_0, m_1 \end{matrix}, \begin{matrix} \text{Person C} \\ \perp \end{matrix}\right) = \left(\begin{matrix} \text{Person A} \\ \perp \end{matrix}, \begin{matrix} \text{Person B} \\ \perp \end{matrix}, \begin{matrix} \text{Person C} \\ m_b \end{matrix}\right)$$

Round 1



Round 2



Output



Case 2: Lets assume the honest parties **do not** abort

~~1. The simulator extracts  $b$  as 's input.~~

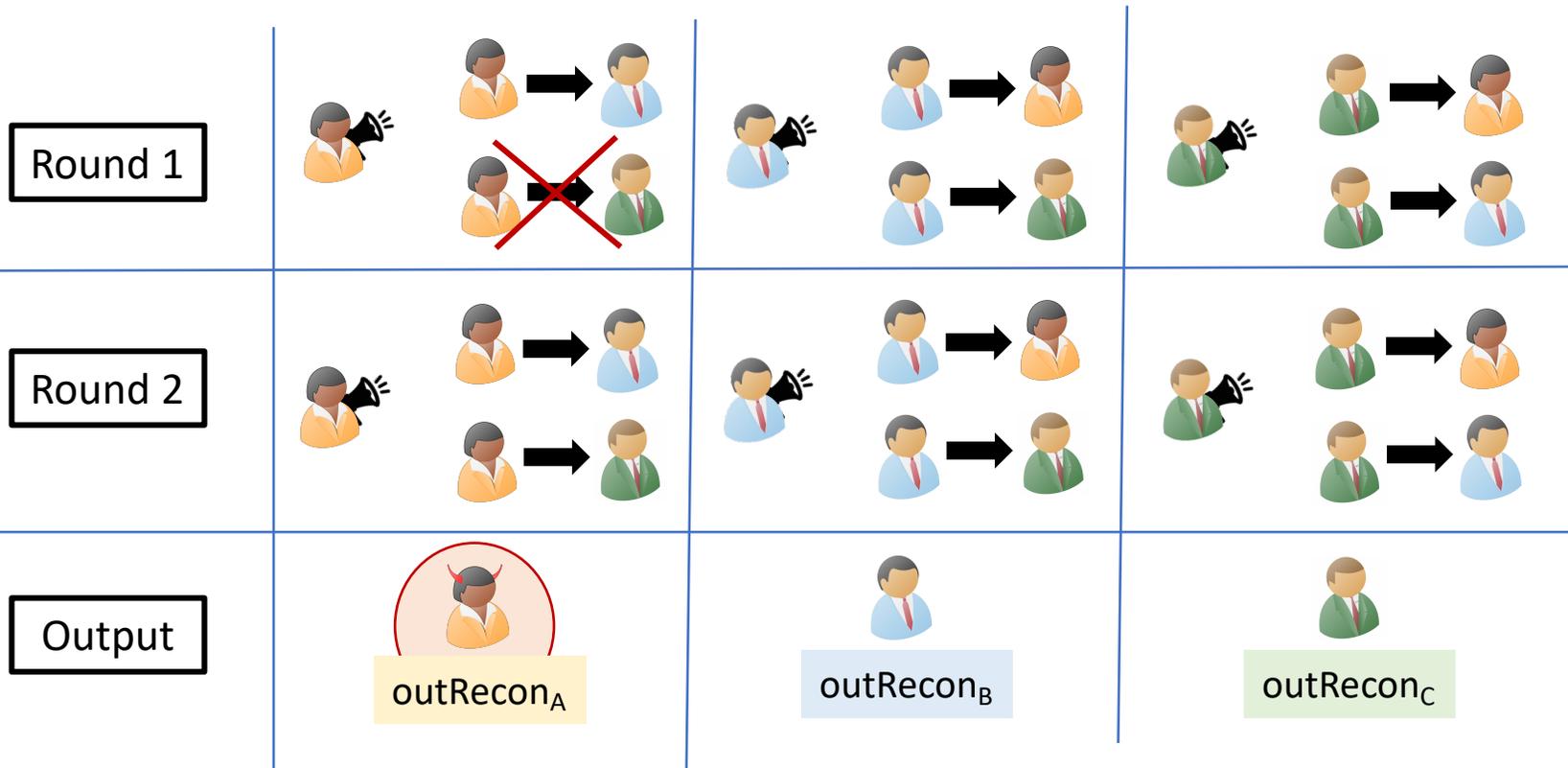
~~2. The simulator extracts  $1 - b$  as 's input.~~

A corrupt Person C can launch a residual function attack to violate Person A's privacy

# Broadcast + P2P: Identifiable Abort is Impossible

Assume FSOC,  $\exists$  a two-round identifiable abort protocol for

$$F\left(\begin{array}{c} \text{Alice} \\ b \end{array}, \begin{array}{c} \text{Bob} \\ m_0, m_1 \end{array}, \begin{array}{c} \text{Charlie} \\ \perp \end{array}\right) = \left(\begin{array}{c} \text{Alice} \\ \perp \end{array}, \begin{array}{c} \text{Bob} \\ \perp \end{array}, \begin{array}{c} \text{Charlie} \\ m_b \end{array}\right)$$



Adversary corrupts Alice

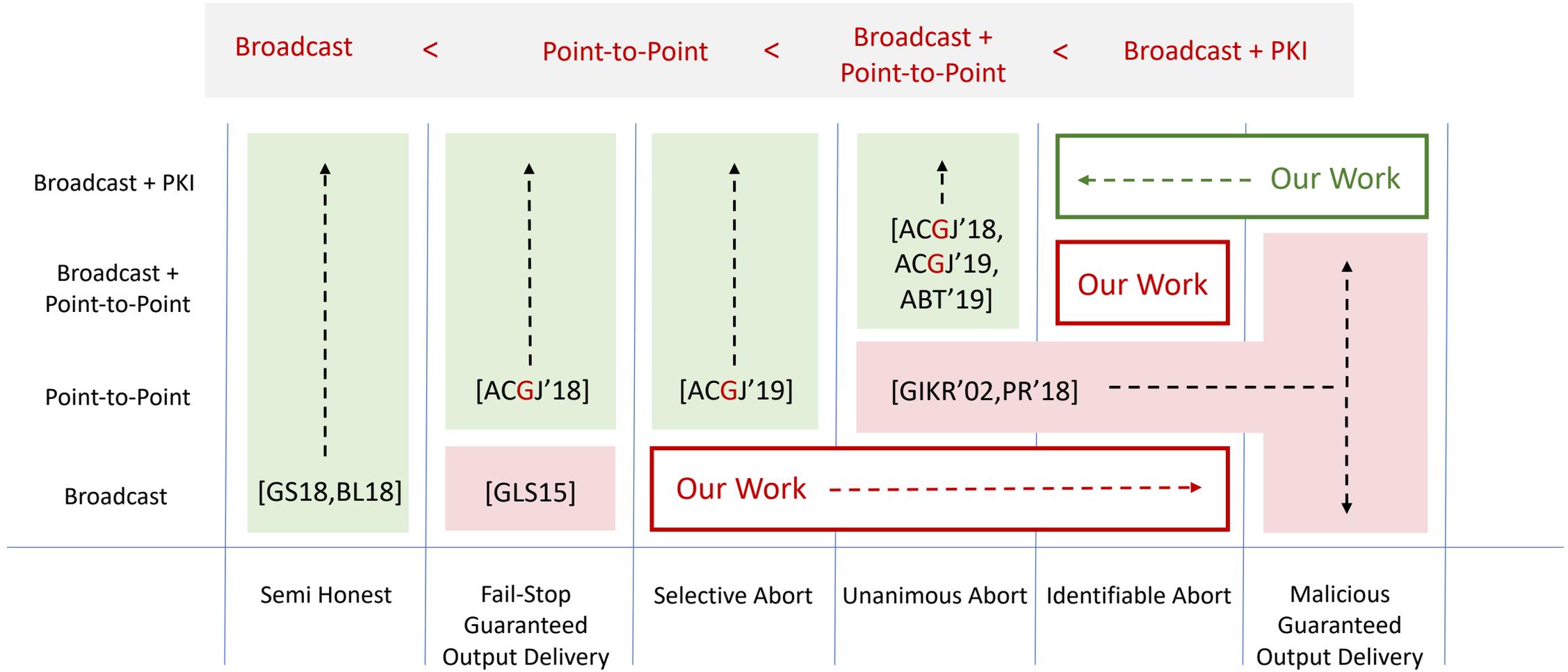
Alice doesn't send private message to Charlie

Honest parties should :

1. Either abort and identify the corrupt party
2. Or do not abort

Neither of these cases are true!  
No such identifiable abort protocol exists!

# Conclusion: Two-Round MPC



<https://eprint.iacr.org/2021/690>

Thank You!