#### **Shared Components Topic Models**

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Topic Model =

Distributions over topics (docs)

Distributions over words (topics)

#### Contrast of LDA Extensions

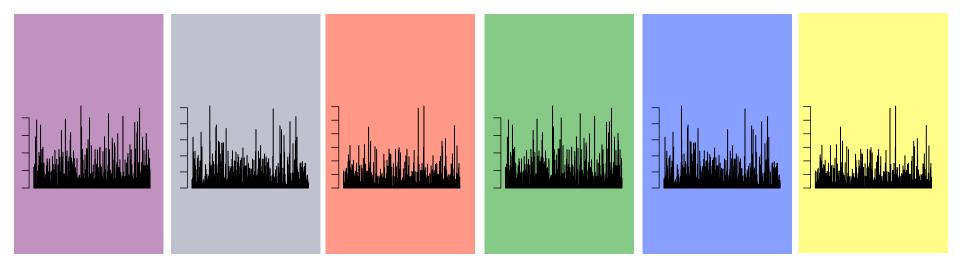
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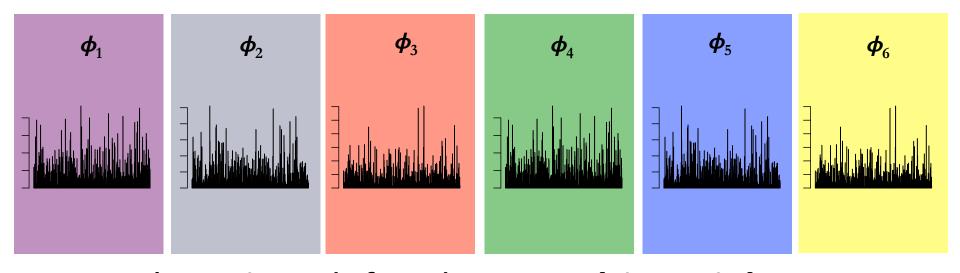
Distributions over words (topics)

Most extensions to LDA

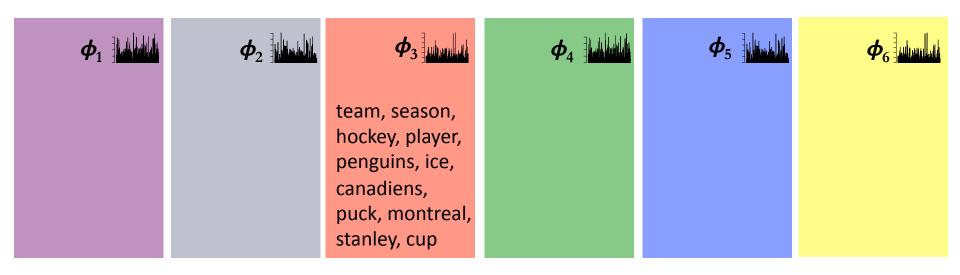
Our Model



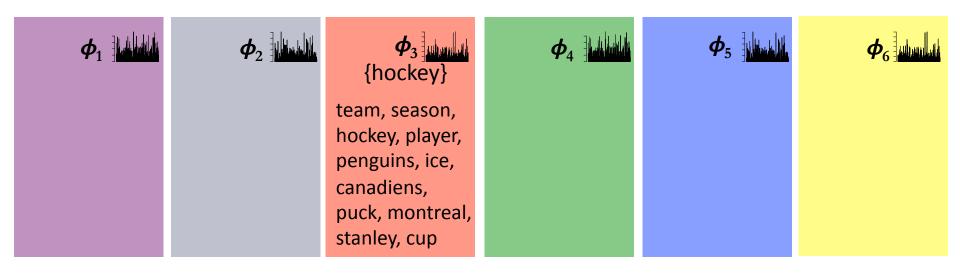
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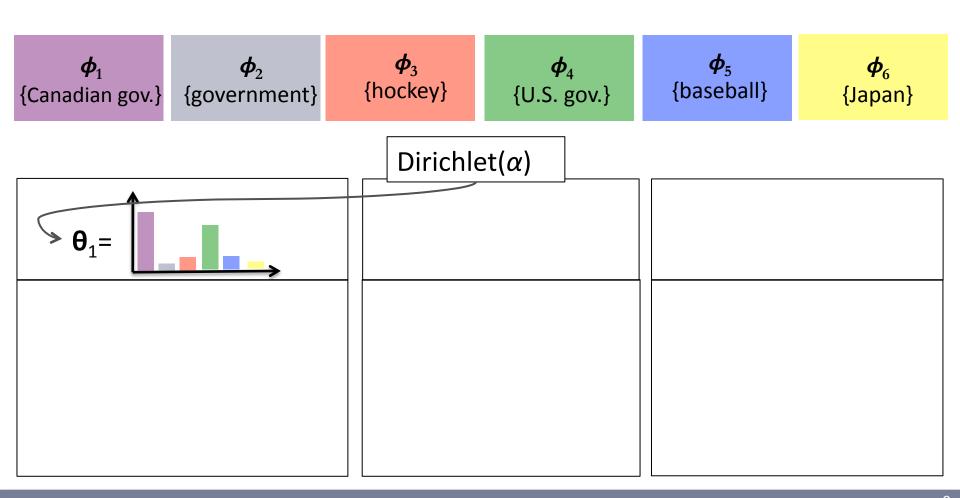
• A topic is visualized as its high probability words.

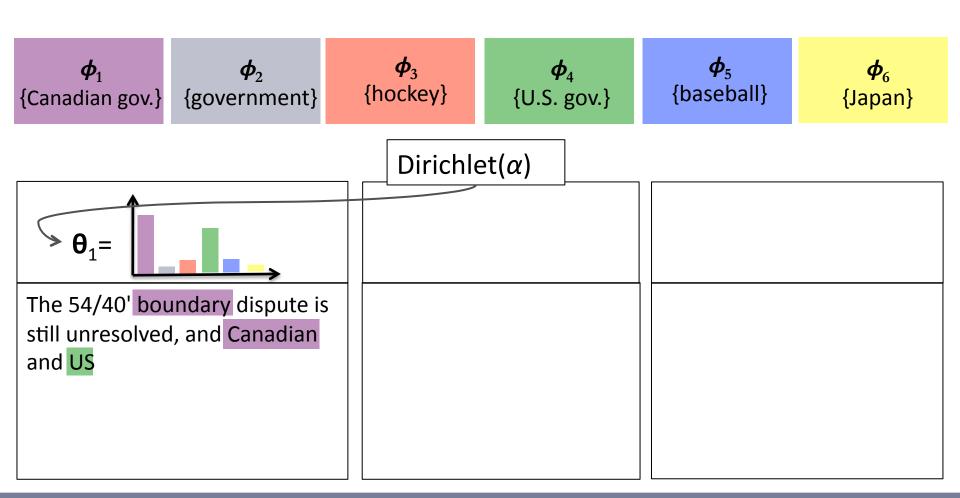


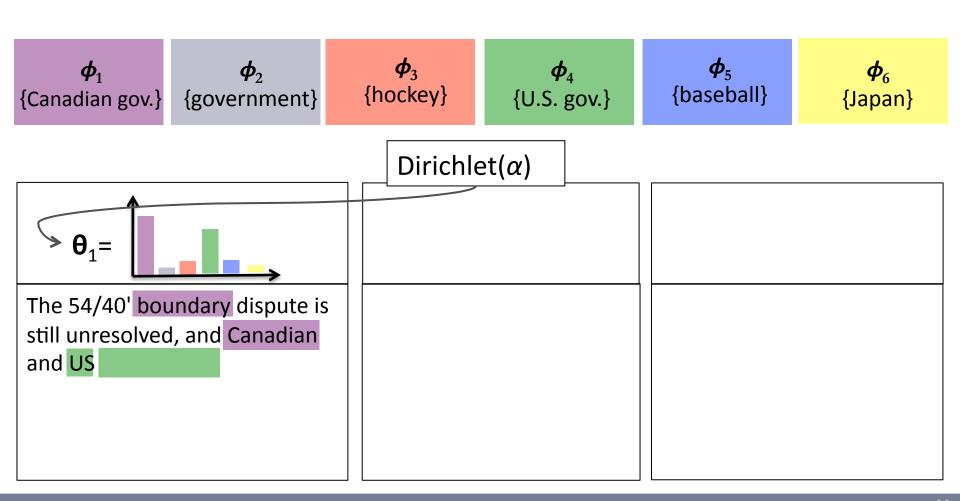
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- A pedigogical label is used to identify the topic.

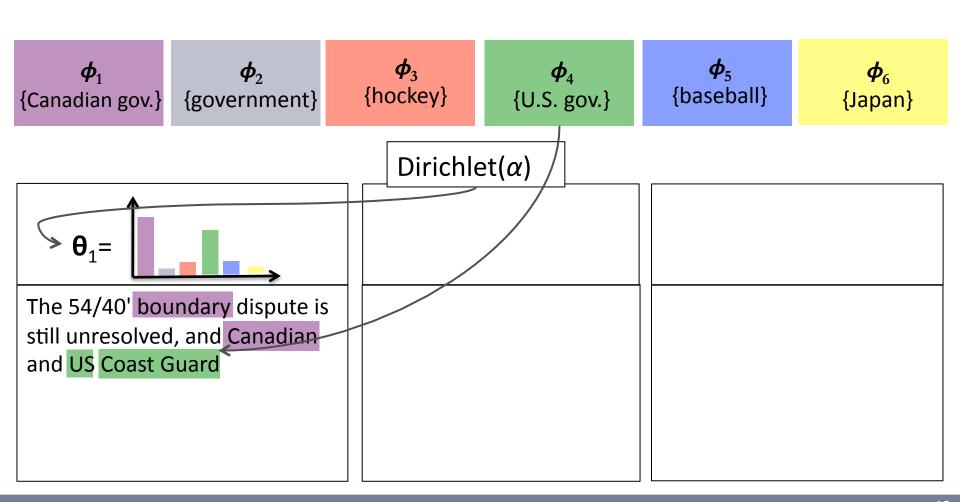


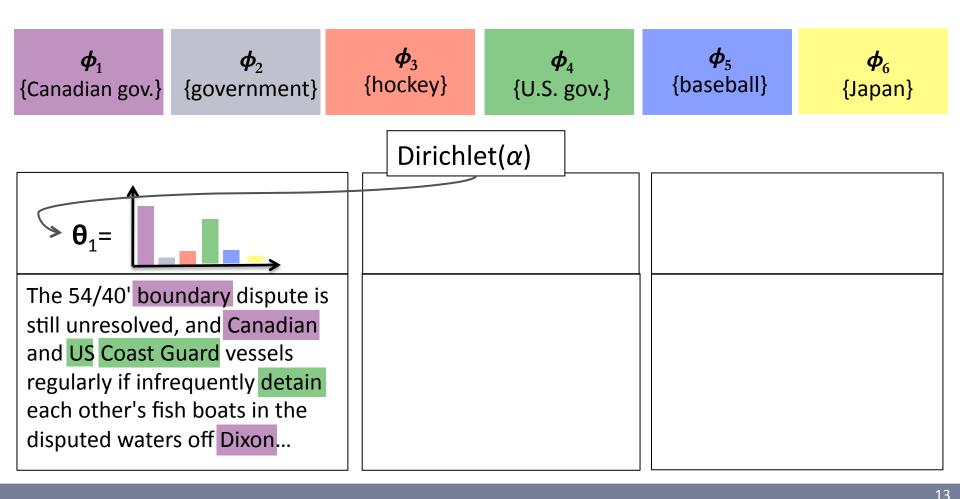
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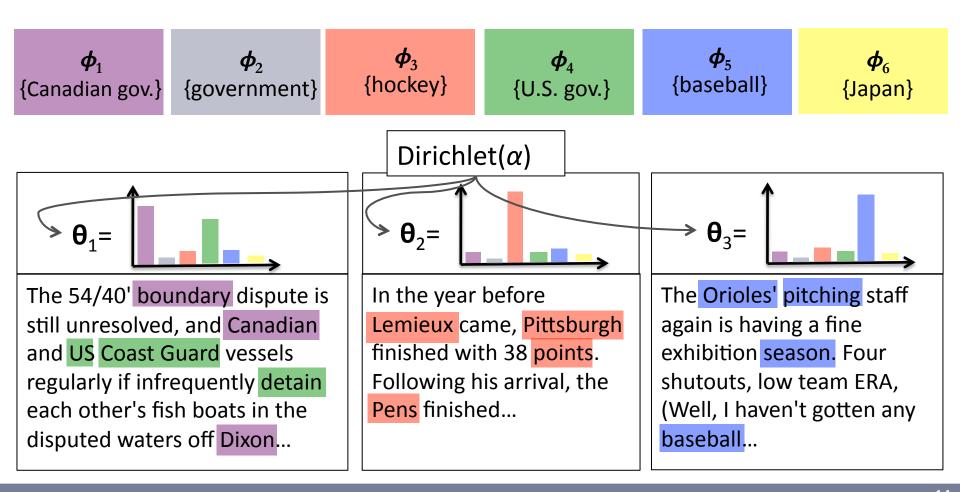


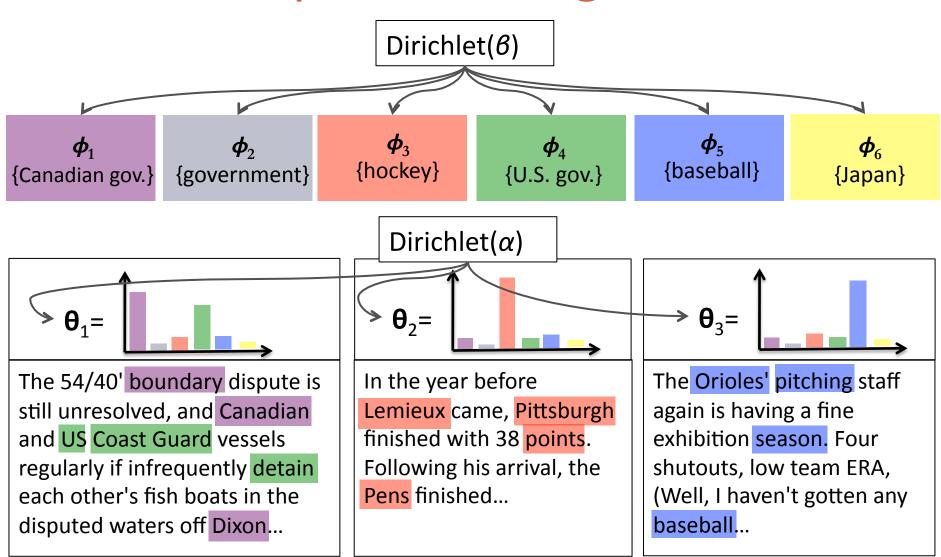


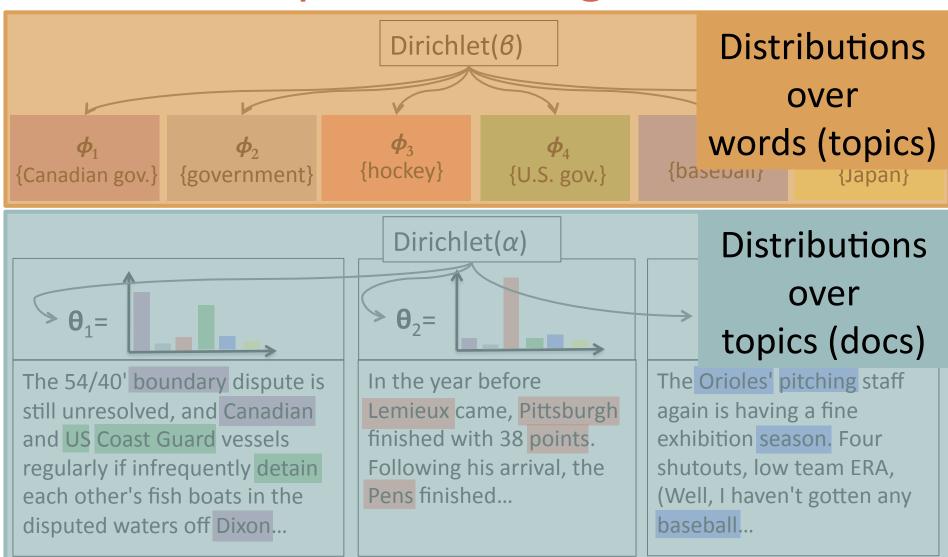


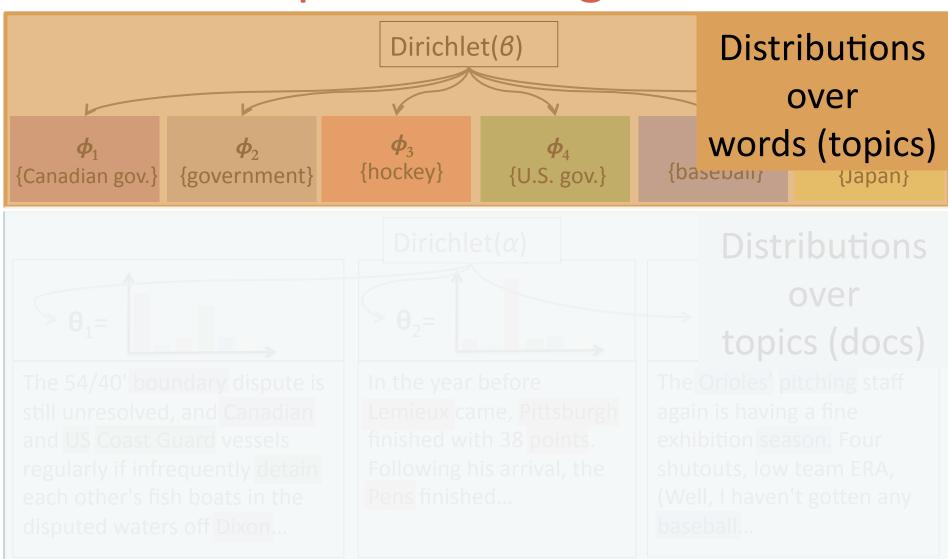












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We're not the first to notice this...

#### Our Model

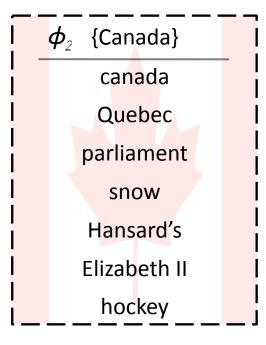
#### Shared Components Topic Model (SCTM):

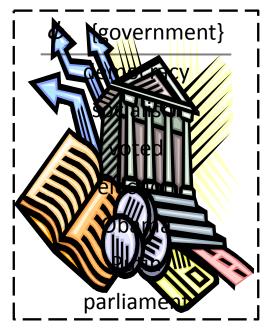
- Generate a pool of "components" (proto-topics)
- Assemble each topic from some of the components
  - Multiply and renormalize ("product of experts")
- Documents are mixtures of topics (just like LDA)
- 1. So the wordlists of two topics are not generated independently!
- 2. Fewer parameters

Components are distributions over words.

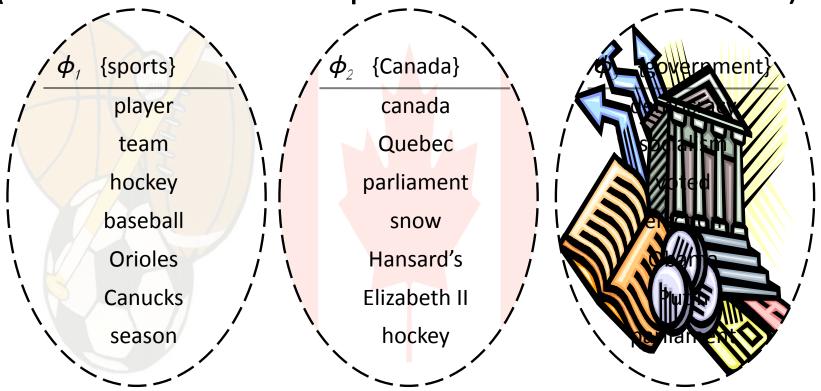
How to combine components into topics?

player
team
hockey
baseball
Orioles
Canucks
season

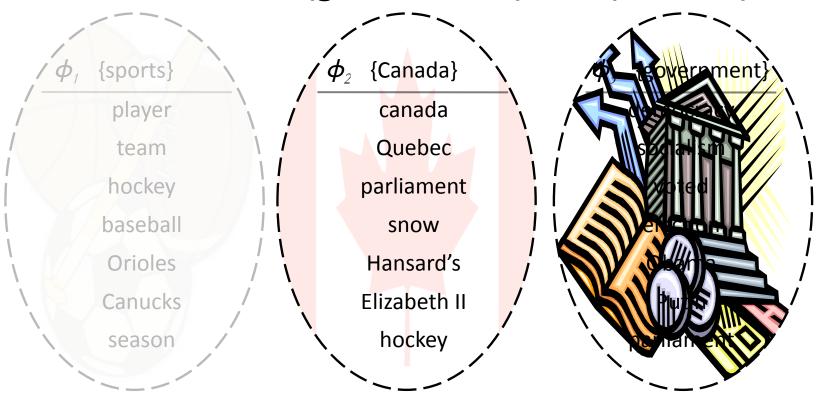




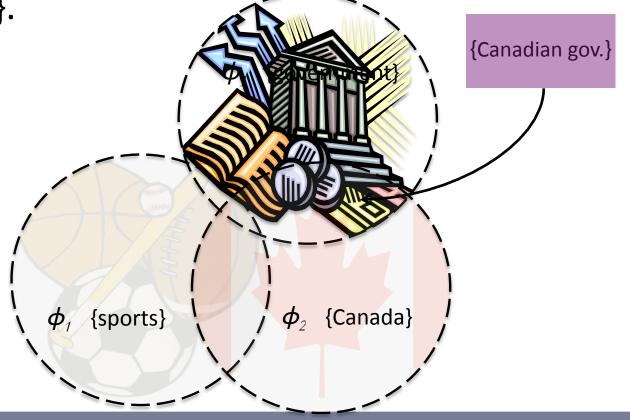
We can imagine a component as a set of words (i.e. all the non-zero probabilities are identical):



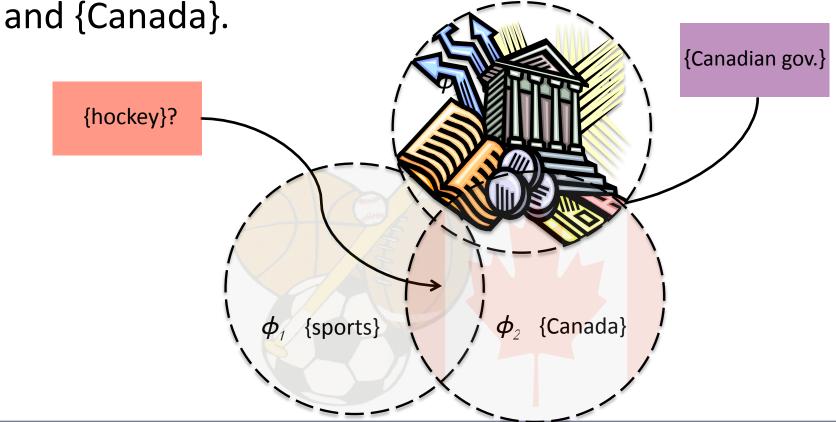
To create a {Canadian government} topic we could take the **union** of {government} and {Canada}.

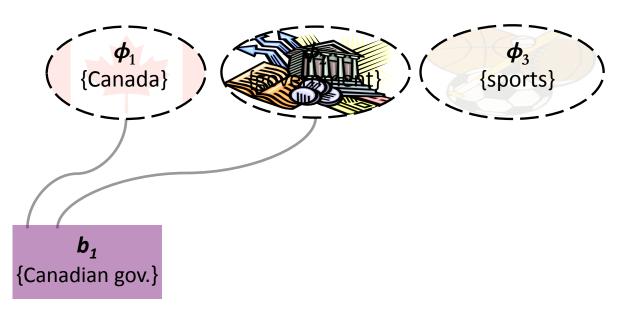


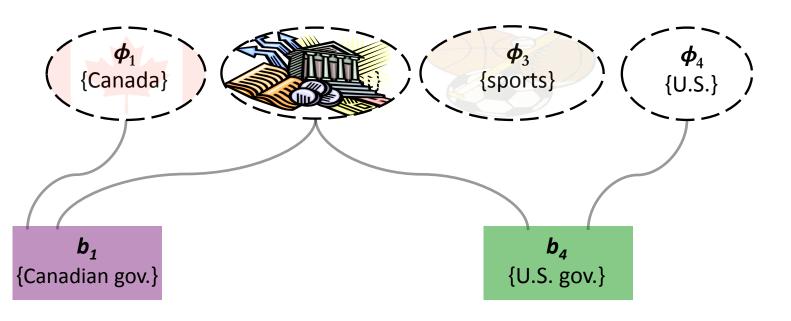
Better yet, to create a {Canadian government} topic we could take the **intersection** of {government} and {Canada}.

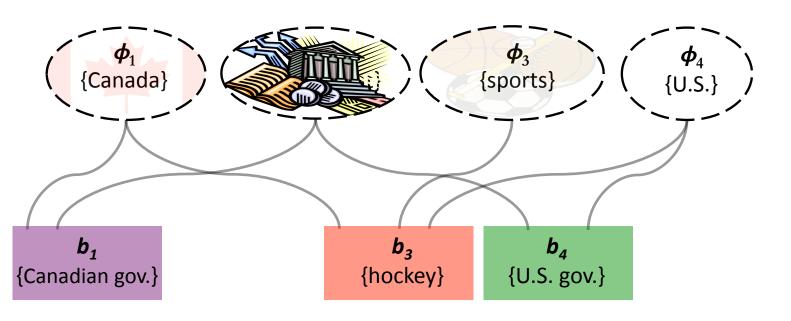


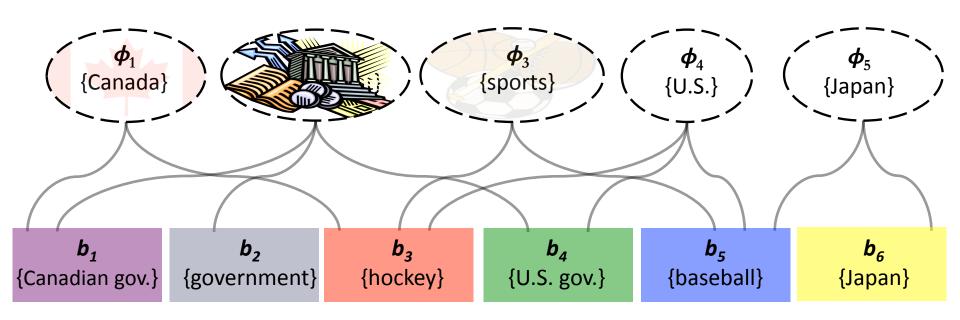
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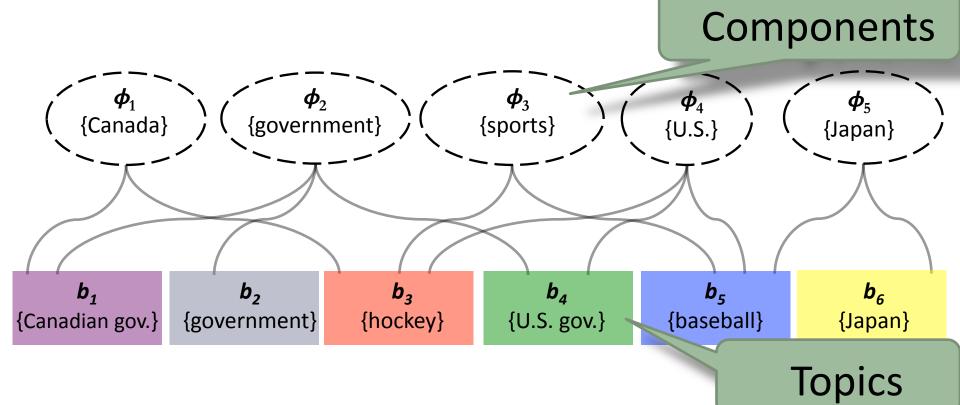






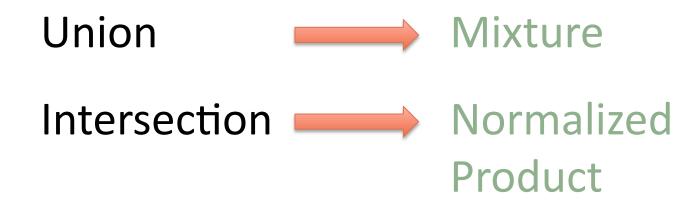






#### Soft Intersection and Union

- We don't want topics to be sets of words, we want probability distributions over words
- In probability space...



### **Product of Experts**

#### Product of Experts (PoE) model (Hinton, 2002)

- Another name for a normalized product
- For a subset of components, define the model as:

$$p(x|\boldsymbol{\phi}_1,\dots,\boldsymbol{\phi}_C) = \frac{\prod_{c\in\mathcal{C}}\phi_{cx}}{\sum_{v=1}^{V}\prod_{c\in\mathcal{C}}\phi_{cv}}$$

Intersection Normalized
Product (PoE)

#### Our Model

#### Shared Components Topic Model (SCTM):

- Generate a pool of "components" (proto-topics)
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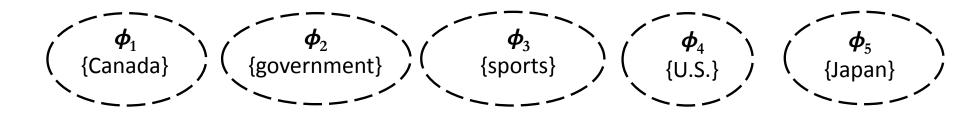
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#### Learning the Structure of Topics

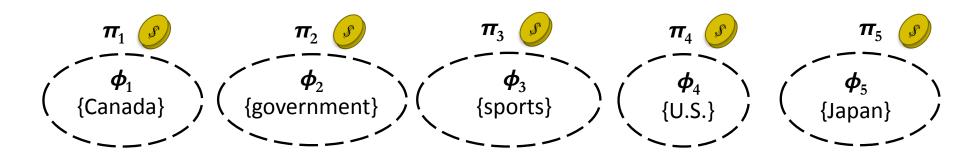
How do we decide **which subset** of components combine to form a single topic?

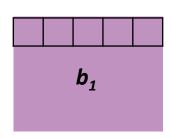


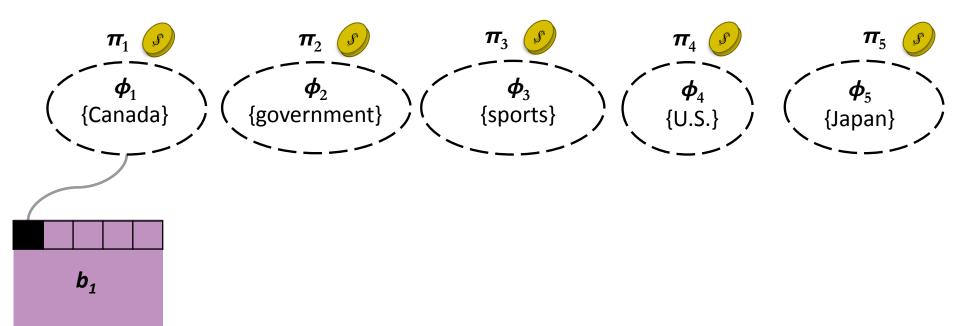
 $b_1$ 

#### Learning the Structure of Topics

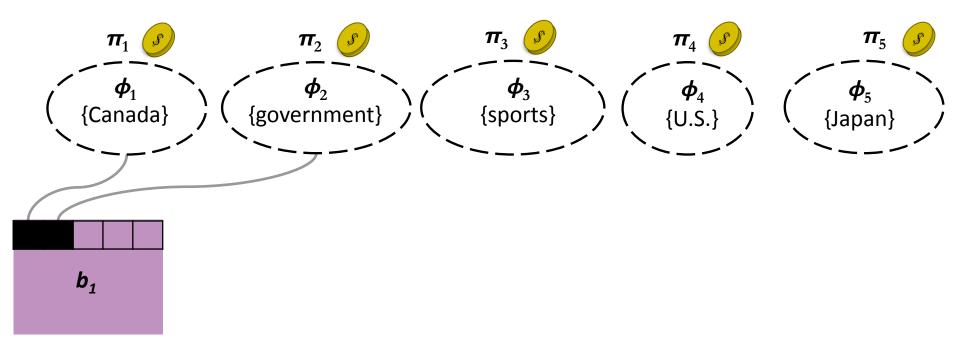
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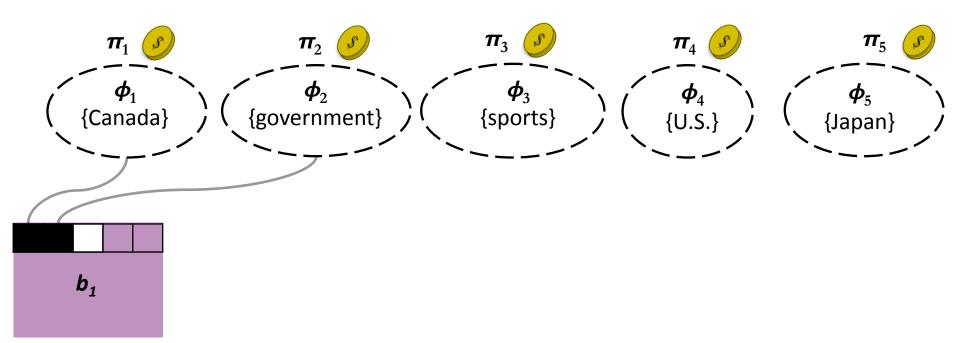




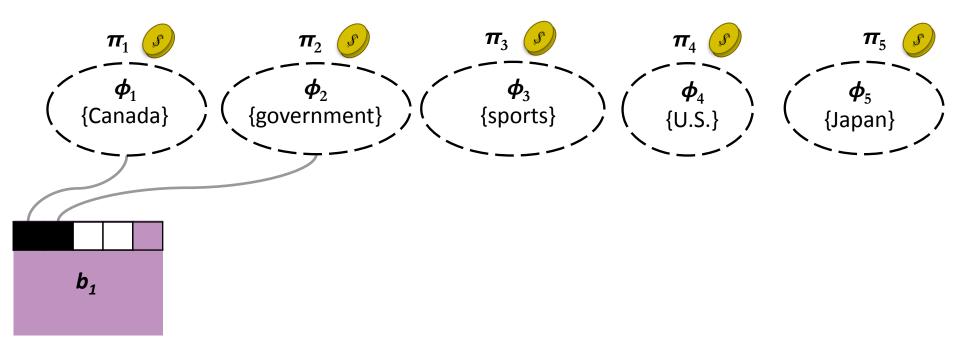
$$\boldsymbol{b_{1c}} \sim \text{Bernoulli}(\boldsymbol{\pi}_{\text{c}})$$



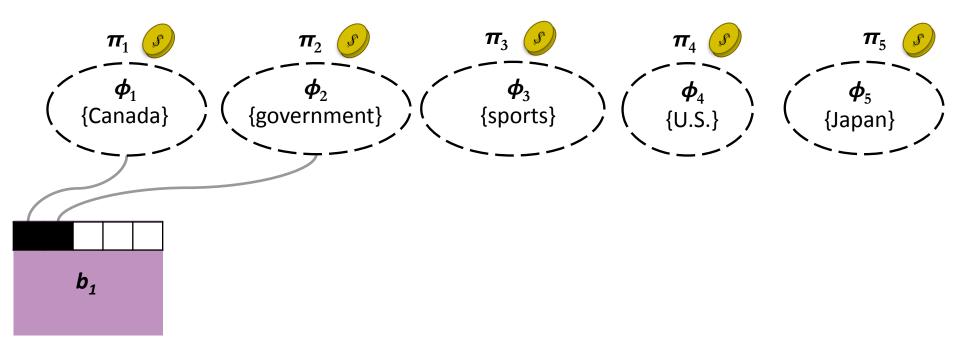
$$m{b}_{1c} \sim \text{Bernoulli}(m{\pi}_{ ext{c}})$$



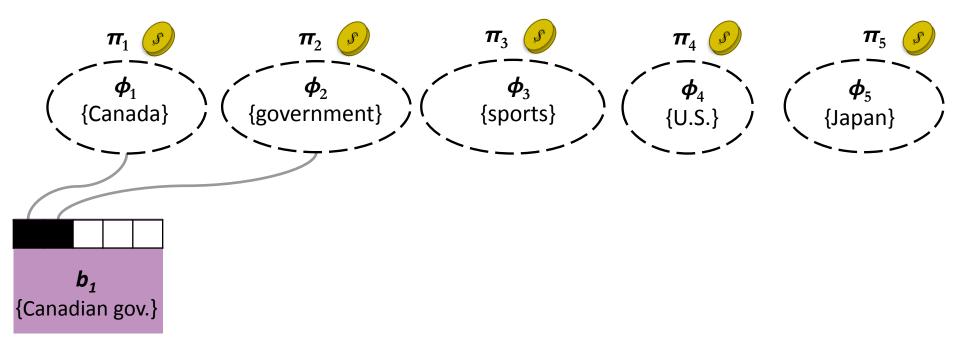
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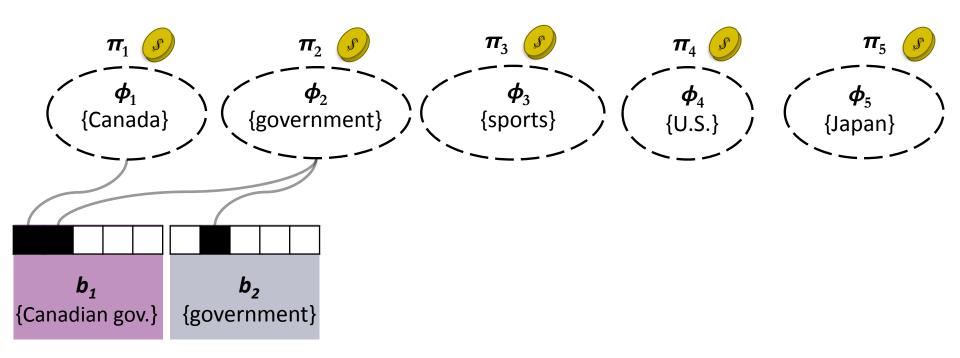
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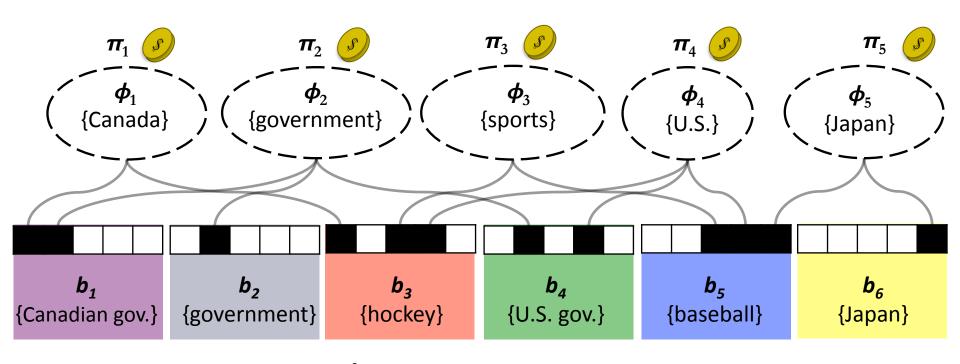


$$m{b}_{1c} \sim \text{Bernoulli}(m{\pi}_{ ext{c}})$$



$$\boldsymbol{b_{kc}} \sim \text{Bernoulli}(\boldsymbol{\pi}_{c})$$

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 $b_{kc} \sim \text{Bernoulli}(\boldsymbol{\pi}_c)$ 

How do we decide which subset of components combine to form a single topic? Beta( $\gamma/C$ , 1)  $\pi_{3}$  $\pi_{\scriptscriptstyle \mathsf{E}}$ {government} {sports} {Canada} {Japan}  $b_1$ b,  $b_3$  $b_5$  $b_4$  $b_6$ {baseball} {Canadian gov.} {hockey} {U.S. gov.} {Japan} {government}

$$m{b}_{kc} \sim \mathrm{Bernoulli}(m{\pi}_{\mathrm{c}})$$

How do we decide **which subset** of components combine to form a single topic?

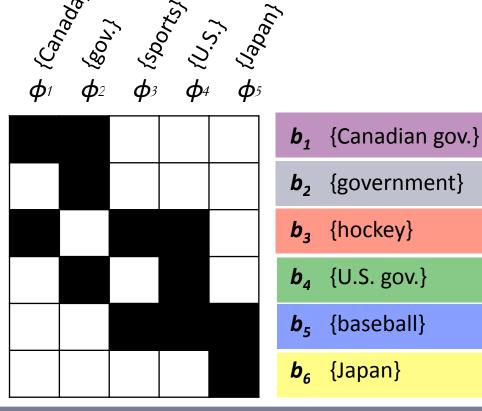
#### Beta-Bernoulli model

- The finite version of the Indian Buffet Process (Griffiths & Ghahramani, 2006)
- Prior over K x C binary matrices

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#### Beta-Bernoulli model

- The finite version of the Indian Buffet Process (Griffiths & Ghahramani, 2006)
- Prior over K x C binary matrices
- We can stack the binary vectors to form a matrix

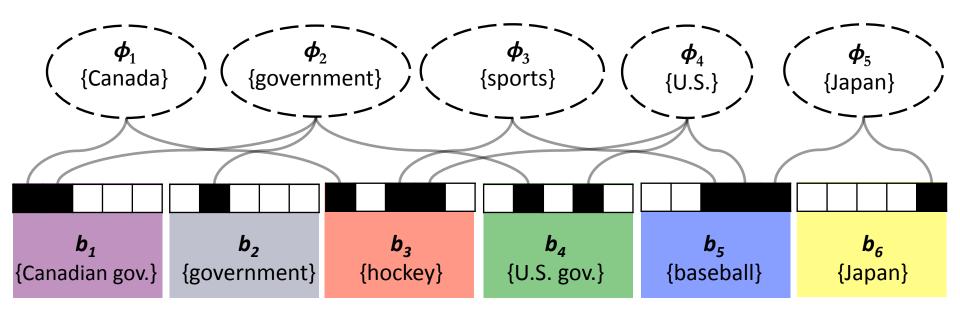


### Our Model

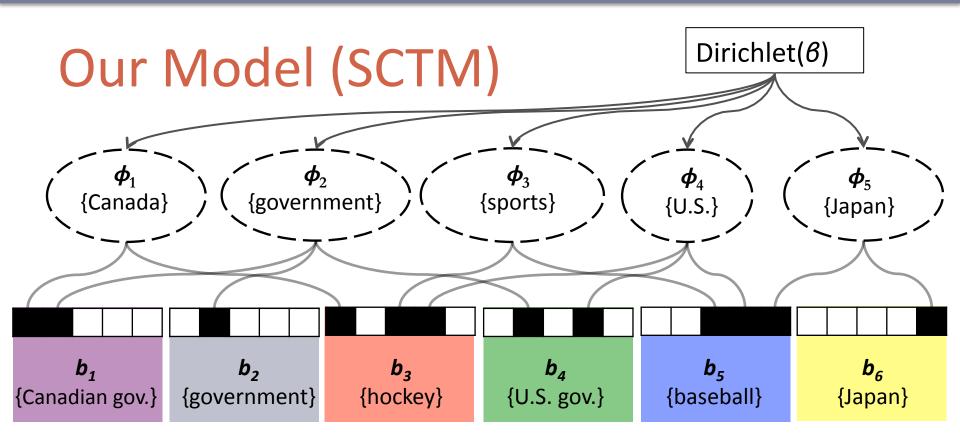
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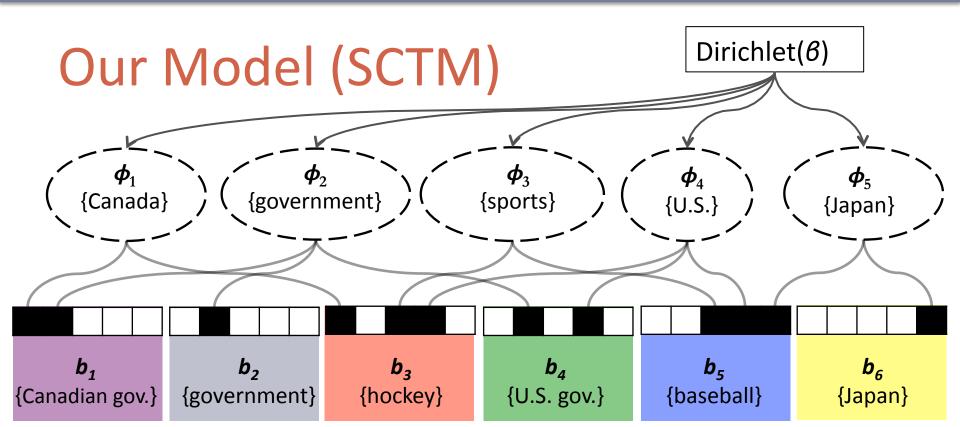
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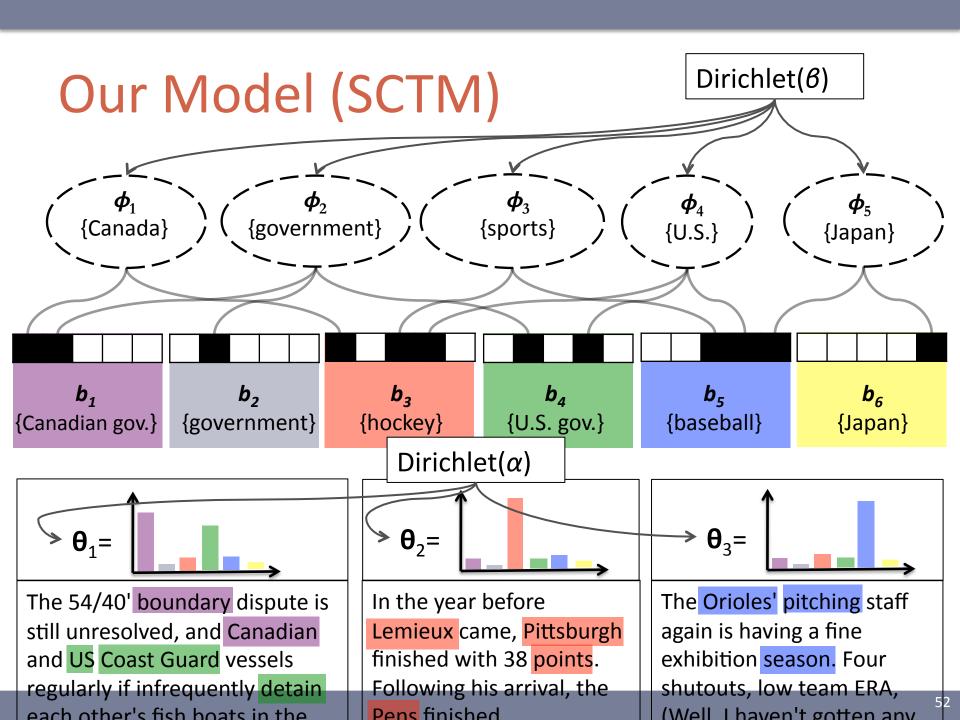


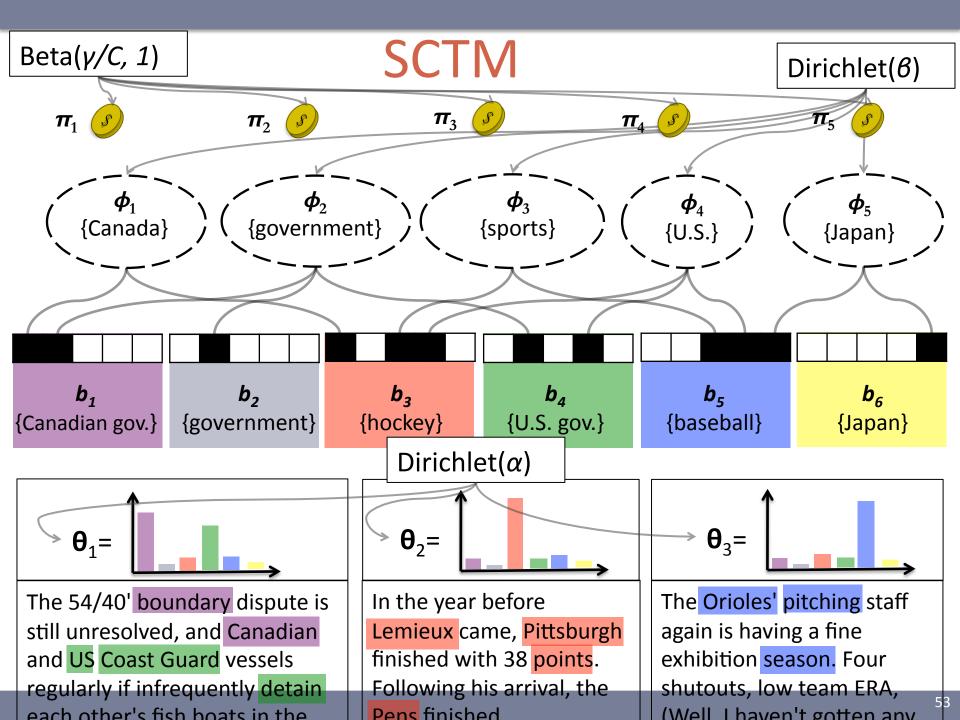
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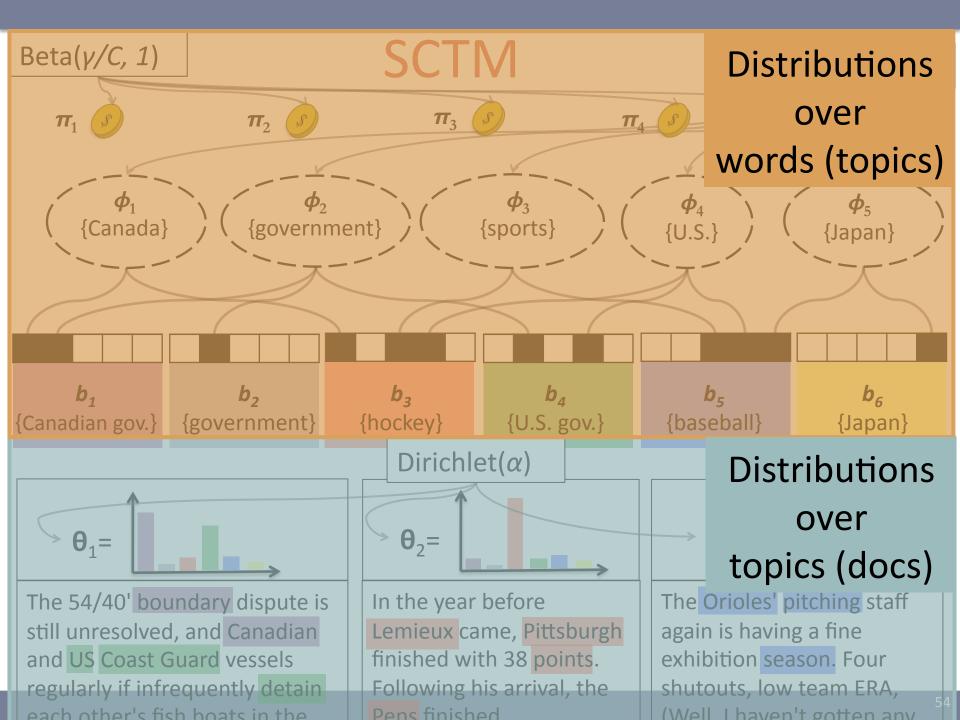


How do we **generate** the components?









Topic Model =

Distributions over topics (docs)

+



- (Rosen-Zvi et al., 2004)
- (Teh et al., 2004)
- (Blei & Lafferty, 2006)
- (Li & McCallum, 2006)
- (Mimno et al., 2007)
- (Boyd-Graber & Blei, 2009)
- (Williamson et al, 2010)
- (Paul & Girju, 2010)
- (Paisley et al, 2011)
- (Kim & Sudderth, 2011)

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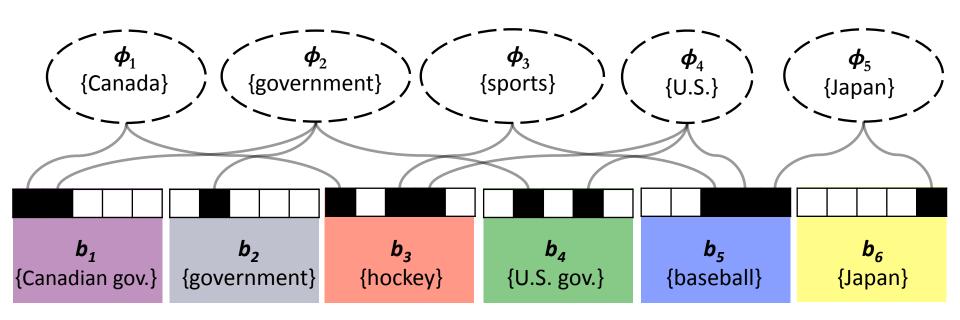


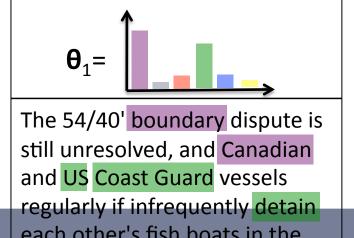
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- HDP mixture model
- Correlated Topic Models (CTM)
- Pachinko Allocation Model (PAM)
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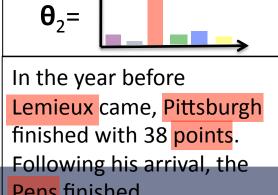
### **Correlated Topics**

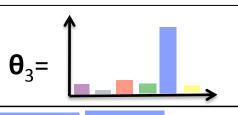
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- **Key difference from SCTM**: correlation is limited to topics that *appear together in the same document* 
  - Example: {hockey} and {baseball} topics share many words in common, but never appear in the same document
- The spirit of learning relationships between topics is very similar!

## Our Model (SCTM)







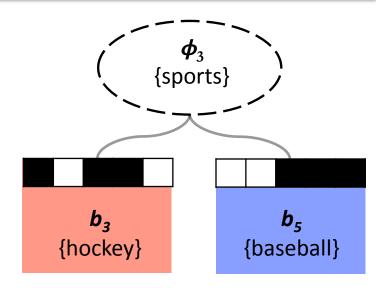


58

The Orioles' pitching staff again is having a fine exhibition season. Four shutouts, low team ERA,

## **Correlated Topics**

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- (Wallach et al., 2009)
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- (Wang & Blei, 2009)
- (Eisenstein et al., 2011)

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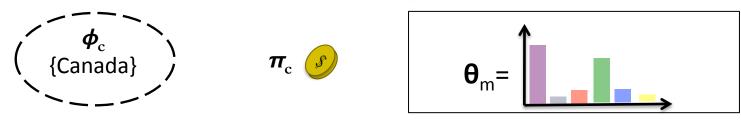
# Comparison of a few Topic Models

|   | Dependently<br>Generated<br>Topics | Fewer<br>Parameters | Description   |
|---|------------------------------------|---------------------|---|
| LDA<br>(Blei et al., 2003)                        |                                    |                     |   |
| Asymmetric Dirichlet Prior (Wallach et al., 2009) |                                    |                     | All topics drawn from language specific base distribution |
| Spherical Topic Model (Reisinger et al., 2010)    |                                    |                     |   |
| SparseTM (Wang & Blei, 2009)                      |                                    |                     | Each topic is sparse                                      |
| SAGE<br>(Eisenstein et al., 2011)                 |                                    |                     |   |
|   |                                    |                     |   |

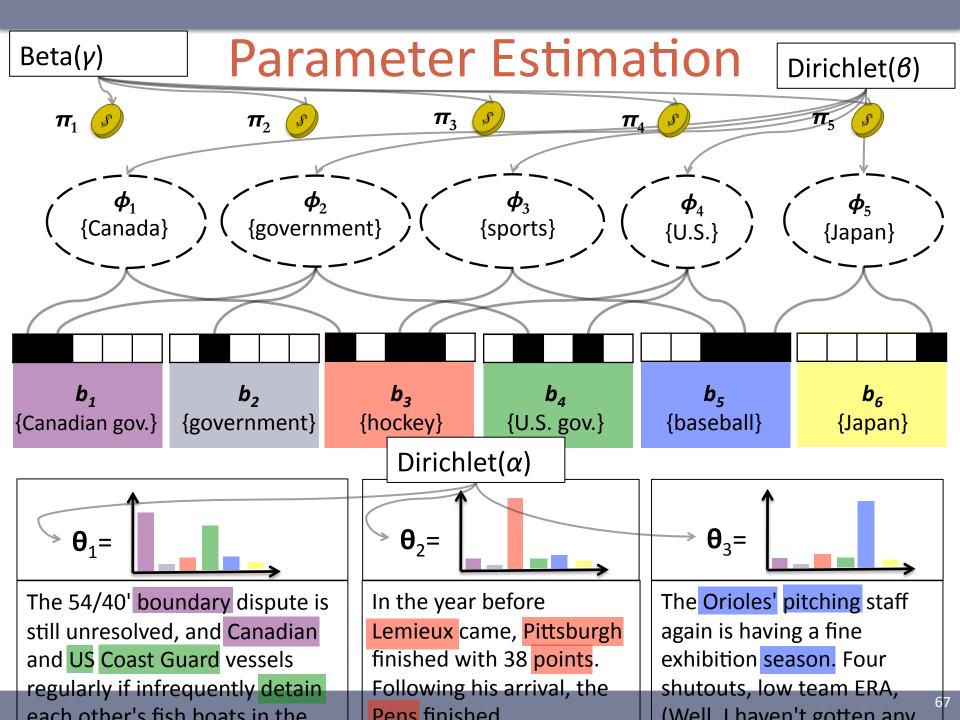
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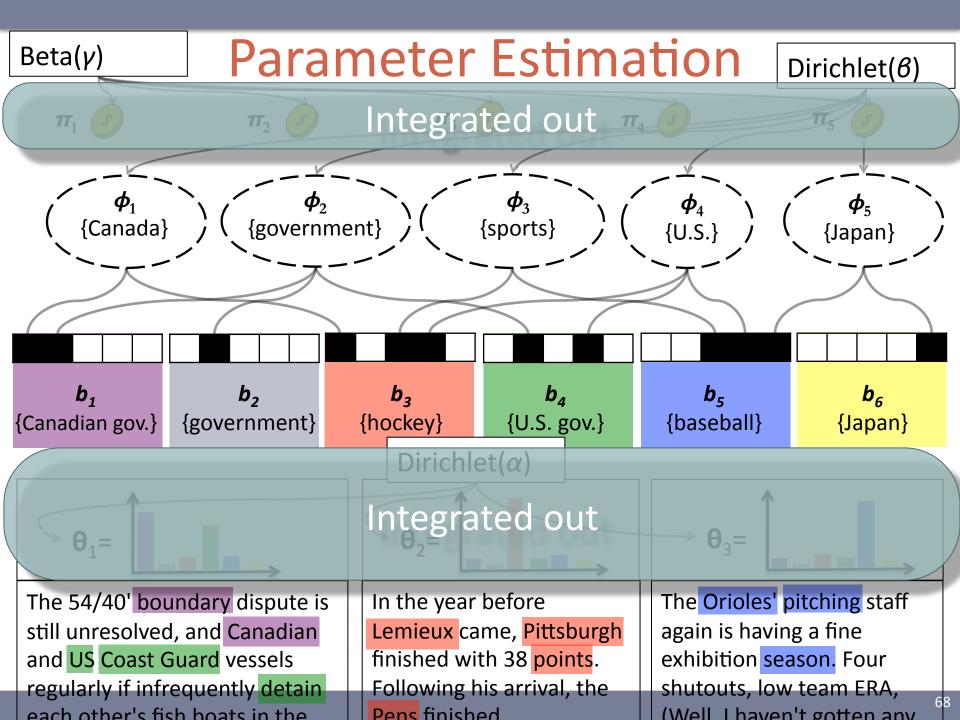
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| SparseTM (Wang & Blei, 2009)                      |                                    |                     | Each topic is sparse                               |
| SAGE (Eisenstein et al., 2011)                    |                                    |                     |  |
| SCTM<br>(This paper)                              |                                    |                     | Topics are products of a shared pool of components |

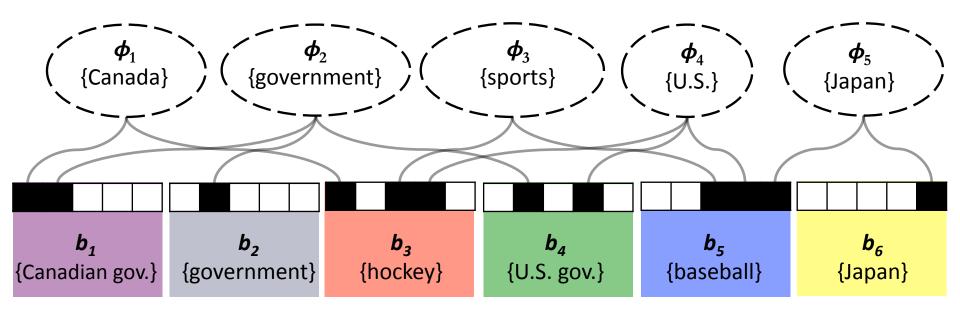
Goal: infer values for model parameters



 Monte Carlo EM (MCEM) algorithm, where the M-step minimizes a Contrastive Divergence (CD) objective







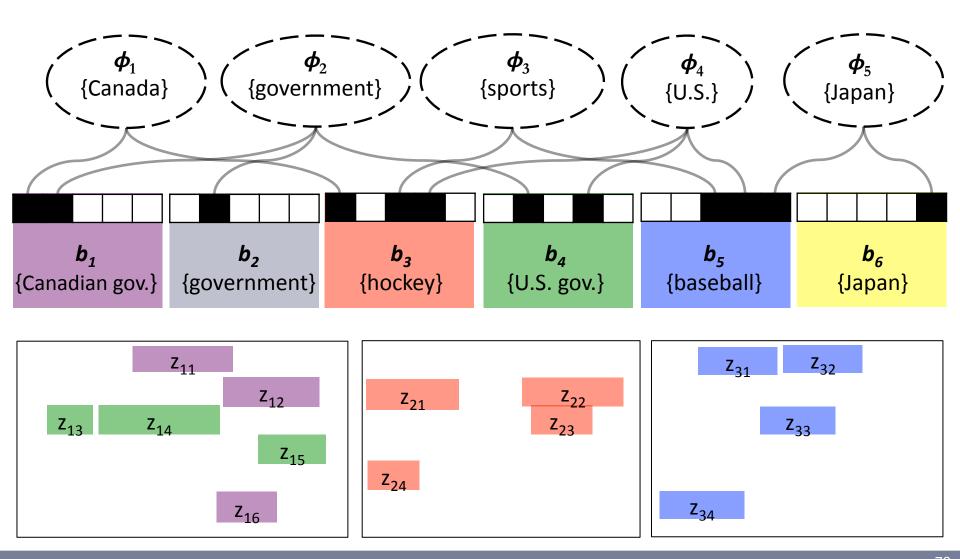
The 54/40' boundary dispute is still unresolved, and Canadian and US Coast Guard vessels regularly if infrequently detain each other's fish boats in the disputed waters off Dixon...

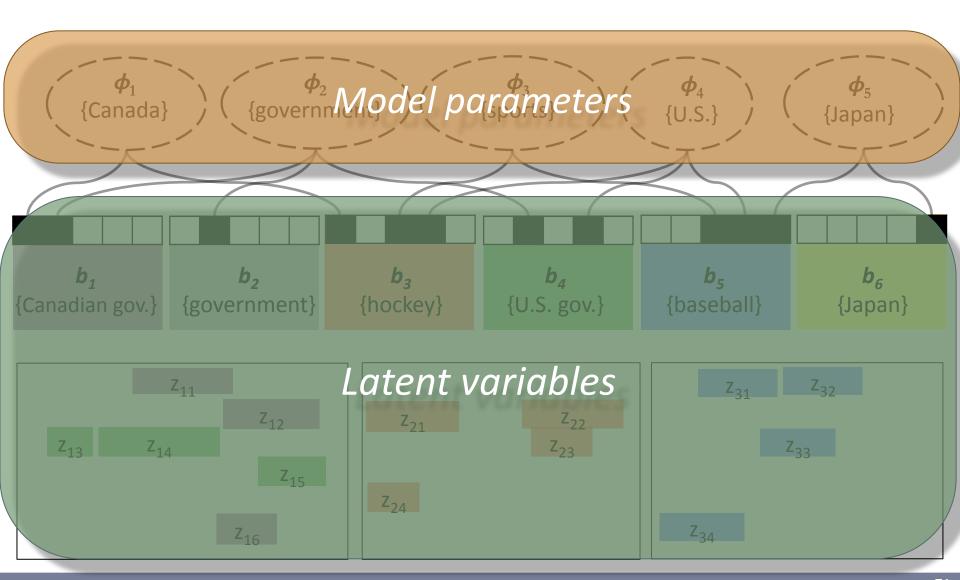
In the year before

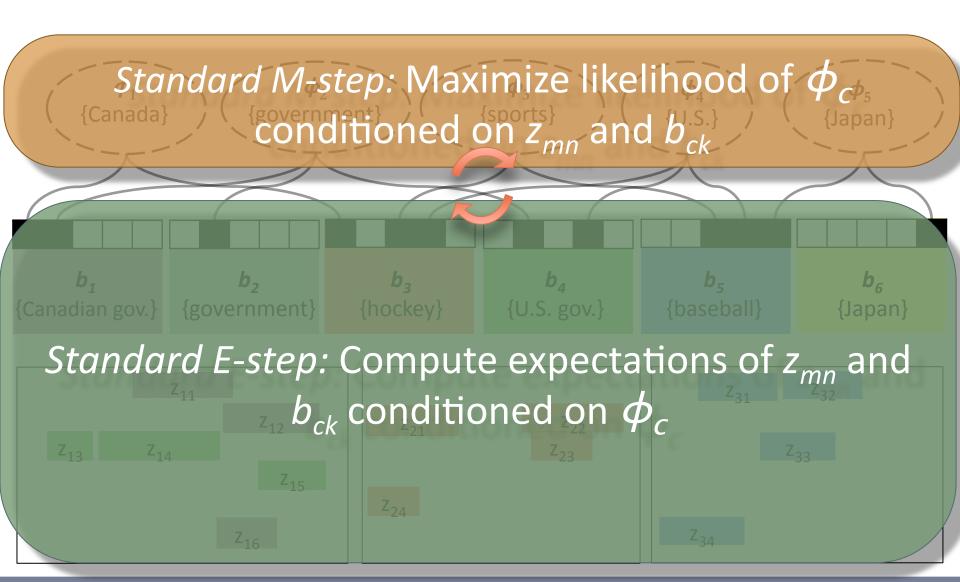
Lemieux came, Pittsburgh
finished with 38 points.

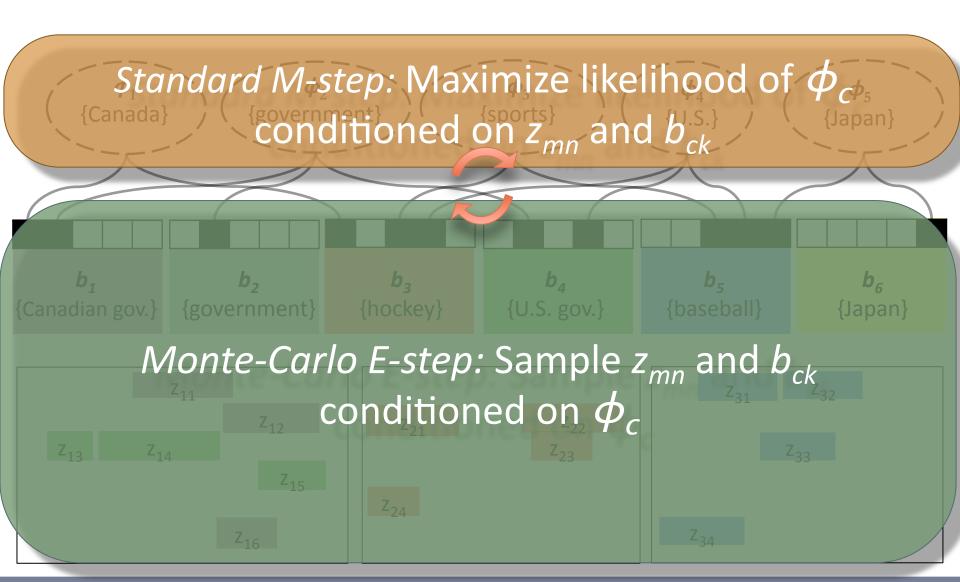
Following his arrival, the
Pens finished...

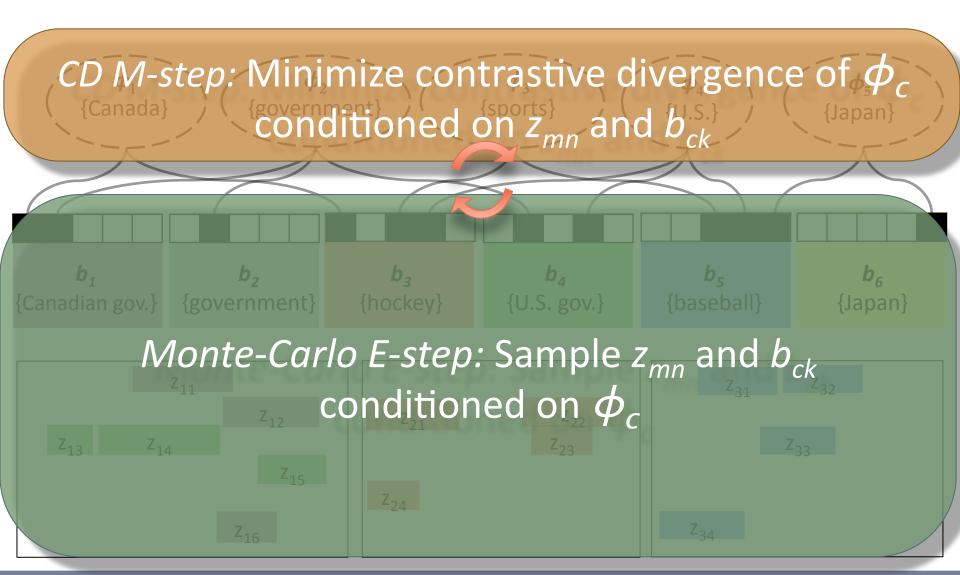
The Orioles' pitching staff again is having a fine exhibition season. Four shutouts, low team ERA, (Well, I haven't gotten any baseball...











#### CD M-step:

$$\begin{array}{l} \mbox{ for } c=1 \mbox{ to } C \mbox{ do} \\ \mbox{ for } v=1 \mbox{ to } V \mbox{ do} \\ \mbox{ Single gradient step over } \xi \end{array}$$

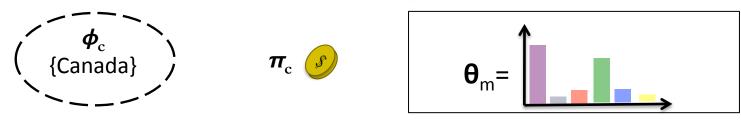
We follow Hinton (2002)

$$\phi_{cv}^{(t+1)} = \phi_{cv}^{(t)} - \eta \cdot \frac{d\operatorname{CD}(\{Z, B\})}{d\phi_{cv}}$$

#### Monte-Carlo E-step:

$$\begin{aligned} & \textbf{for } i = 1 \text{ to } N \textbf{ do} \\ & \text{Sample } z_i \\ & \textbf{for } k = 1 \text{ to } K \textbf{ do} \\ & \textbf{for } c = 1 \text{ to } C \textbf{ do} \\ & \text{Sample } b_{kc} \end{aligned}$$

Goal: infer values for model parameters



 Monte Carlo EM (MCEM) algorithm, where the M-step minimizes a Contrastive Divergence (CD) objective

#### Experiments:

- Can SCTM combine a fixed number of components (multinomials) into topics to achieve lower perplexity?
- Does SCTM achieve lower perplexity than LDA with a more compact model?

#### Analysis:

- What are the learned topics like?
- What are the learned components like?
- What topic-structure is learned?

#### Experimental Setup:

#### – Datasets:

- 1,000 random articles from 20 Newsgroups
- 1,617 NIPS abstracts

#### - Evaluation:

left-to-right average perplexity on held-out data

#### -Models:

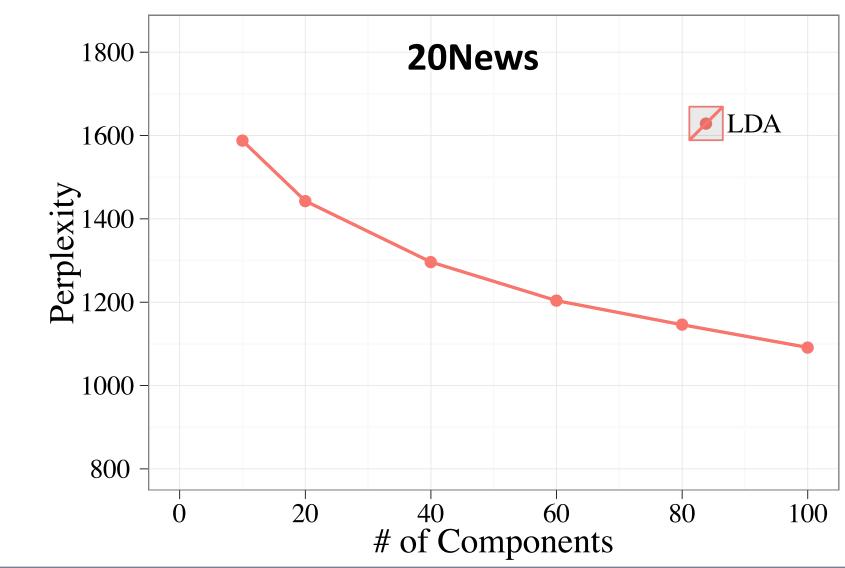
- LDA trained with a collapsed Gibbs sampler
  - In LDA, components and topics are in a one-to-one relationship (i.e. a special case of the SCTM where each topic is comprised of only its corresponding component)
- SCTM with parameter estimation as described

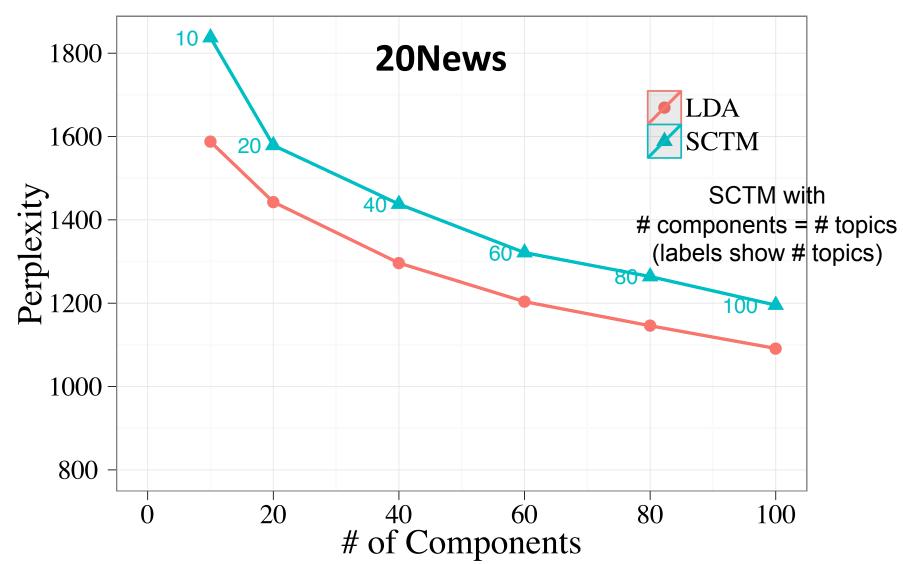
#### Experiments:

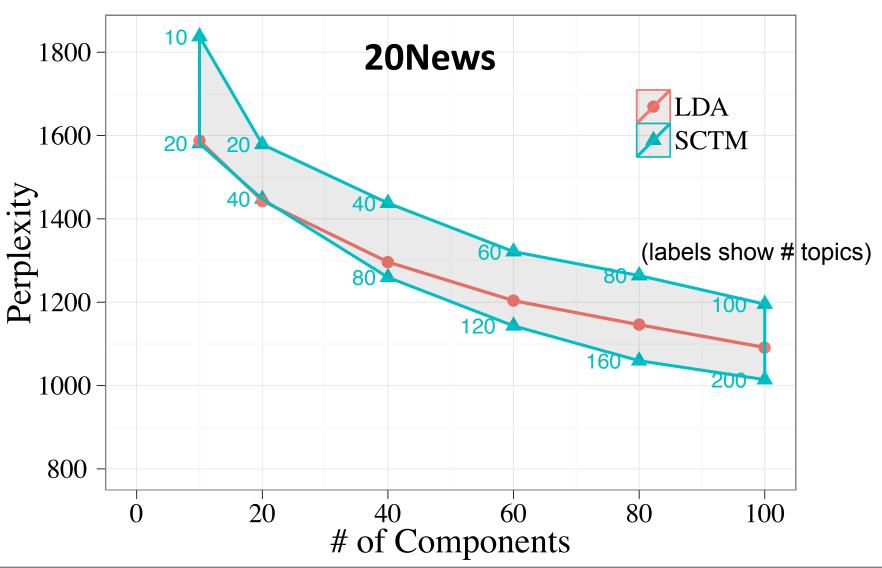
- Can SCTM combine a fixed number of components (multinomials) into topics to achieve lower perplexity?
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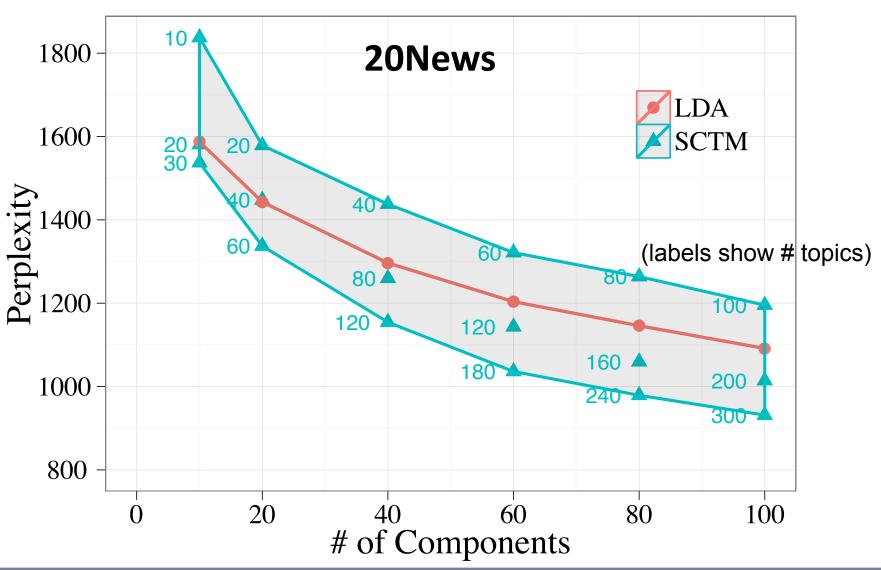
#### Analysis:

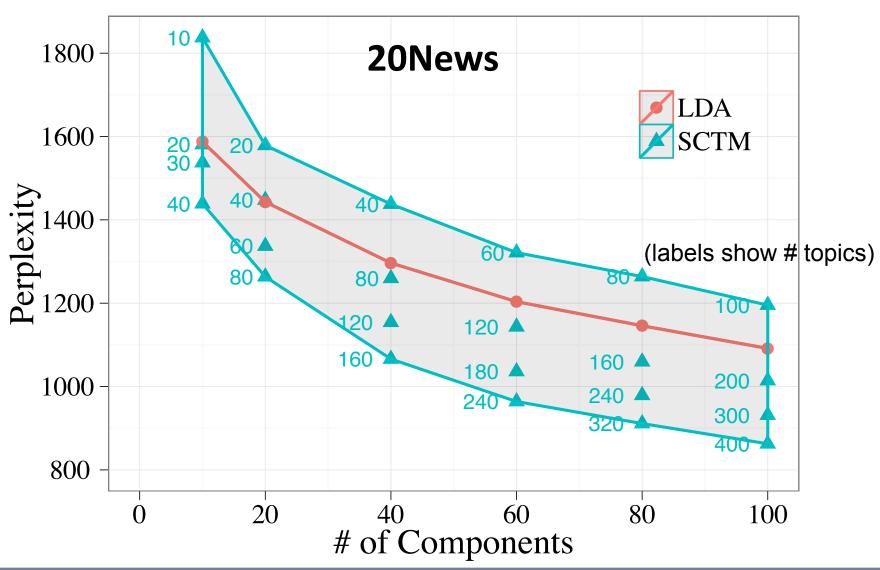
- What are the learned topics like?
- What are the learned components like?
- What topic-structure is learned?

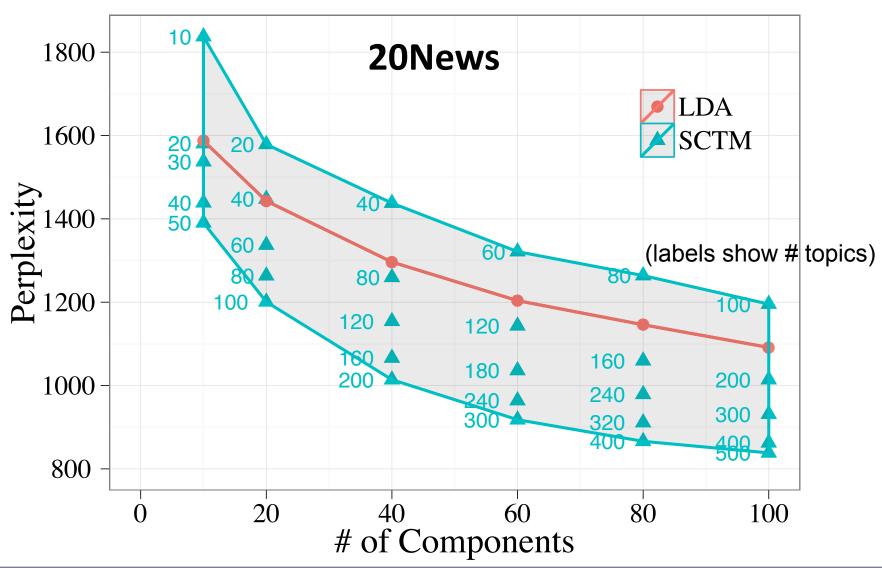


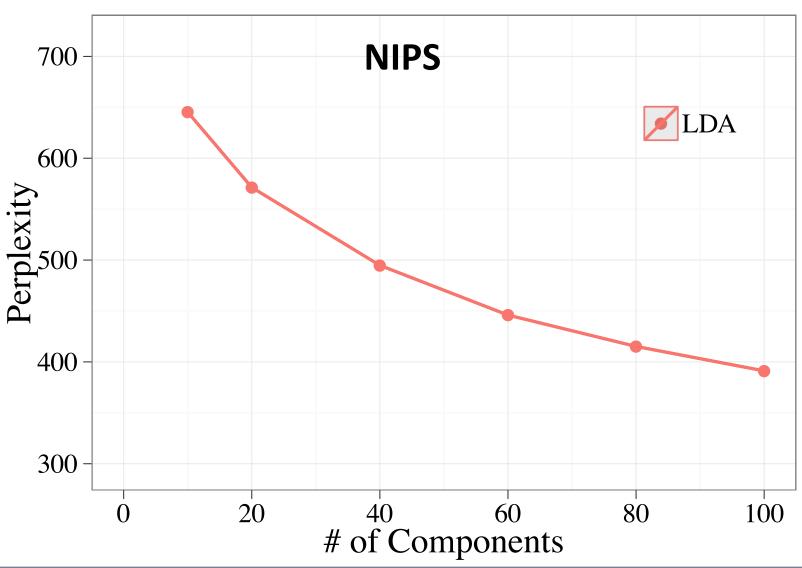


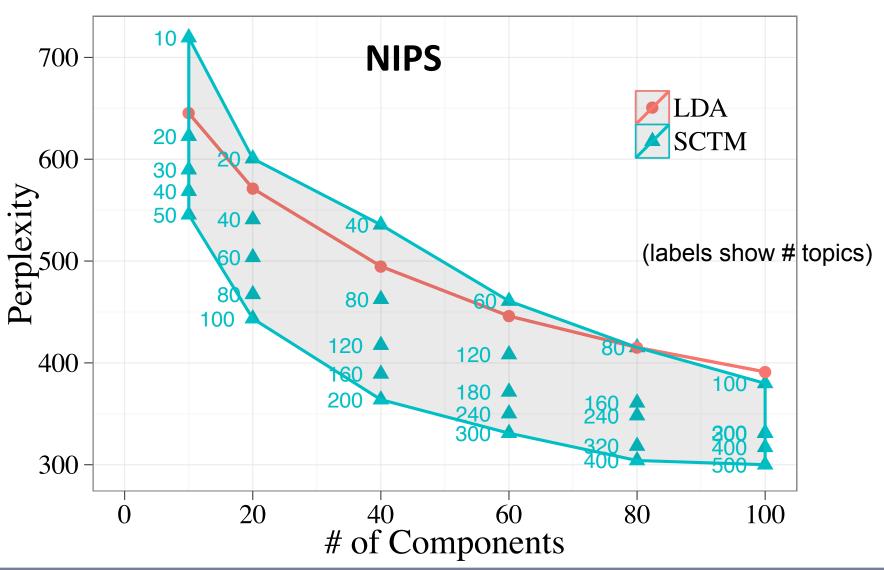










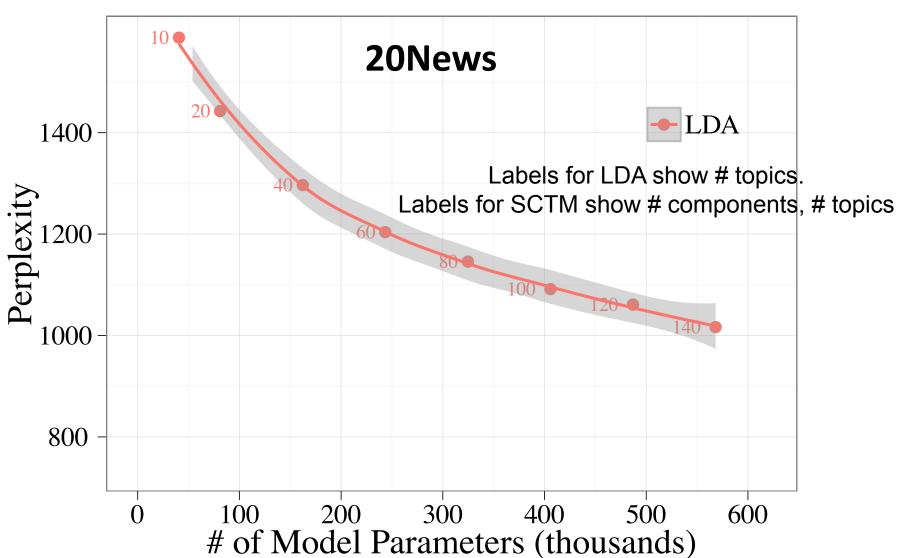


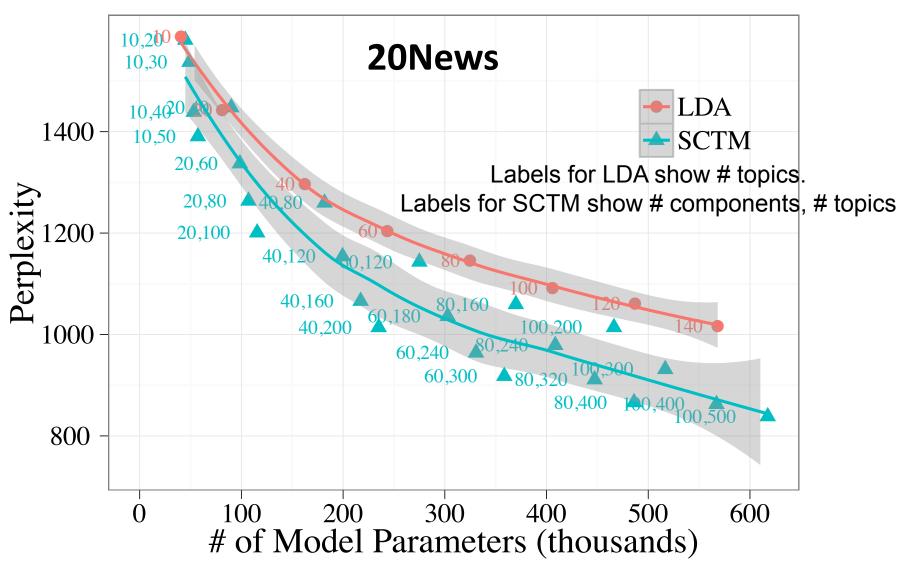
#### Experiments:

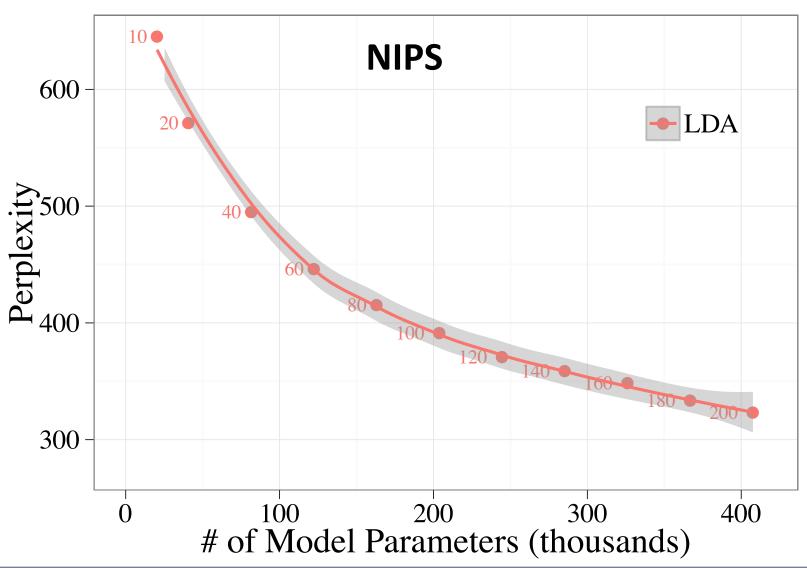
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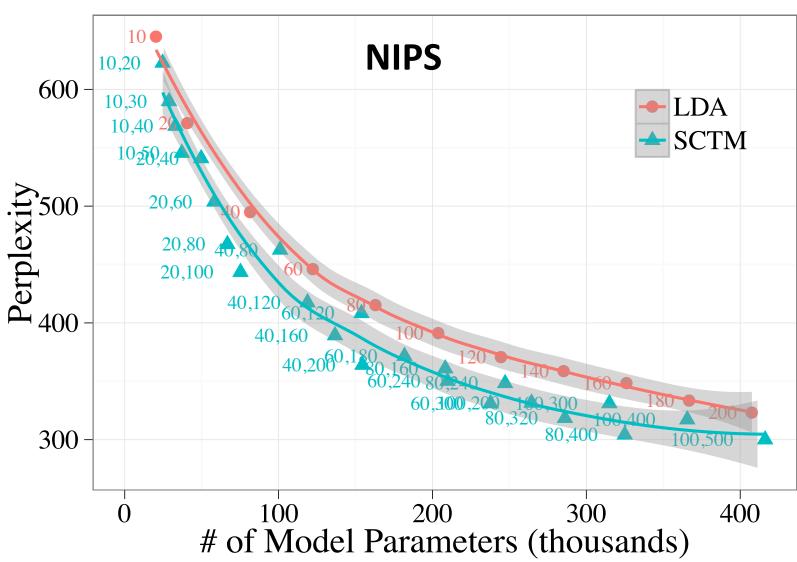
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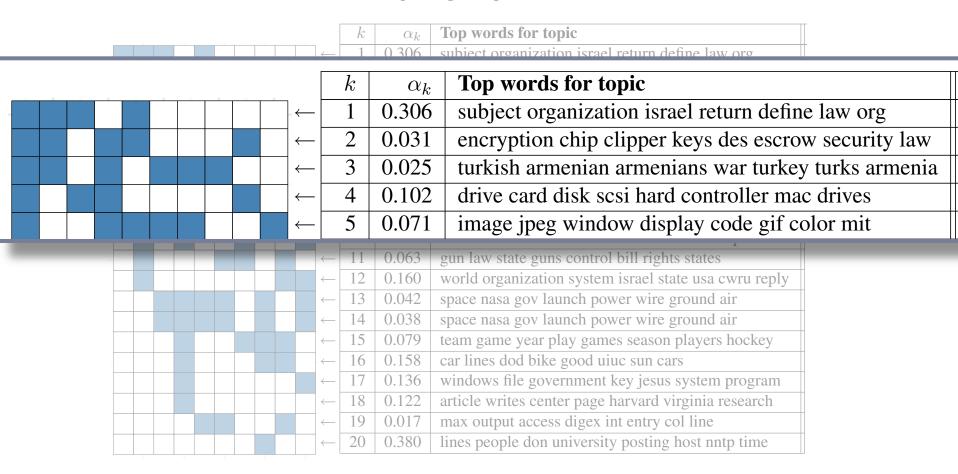
### What does SCTM learn?

#### 20News

|  |   |  |   |       |   |  |  |  |  |              | k  | $\alpha_k$ | Top words for topic                                    |  |
|--|---|--|---|-------|---|--|--|--|--|--------------|----|------------|--|--|
|  | ← |  | 1 | 0.306 | subject organization israel return define law org |  |  |  |  |              |    |            |  |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 2  | 0.031      | encryption chip clipper keys des escrow security law   |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 3  | 0.025      | turkish armenian armenians war turkey turks armenia    |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 4  | 0.102      | drive card disk scsi hard controller mac drives        |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 5  | 0.071      | image jpeg window display code gif color mit           |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 6  | 0.018      | jews israeli jewish arab peace land war arabs          |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 7  | 0.074      | org money back question years thing things point       |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 8  | 0.106      | christian bible church question christ christians life |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 9  | 0.011      | administration president year market money senior      |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 10 | 0.055      | health medical center research information april       |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 11 | 0.063      | gun law state guns control bill rights states          |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 12 | 0.160      | world organization system israel state usa cwru reply  |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 13 | 0.042      | space nasa gov launch power wire ground air            |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 14 | 0.038      | space nasa gov launch power wire ground air            |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 15 | 0.079      | team game year play games season players hockey        |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 16 | 0.158      | car lines dod bike good uiuc sun cars                  |  |
|  |   |  |   |       |   |  |  |  |  | ←            | 17 | 0.136      | windows file government key jesus system program       |  |
|  |   |  |   |       |   |  |  |  |  | ←            | 18 | 0.122      | article writes center page harvard virginia research   |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 19 | 0.017      | max output access digex int entry col line             |  |
|  |   |  |   |       |   |  |  |  |  | $\leftarrow$ | 20 | 0.380      | lines people don university posting host nntp time     |  |

### What does SCTM learn?

#### 20News



### What does SCTM learn?

#### 20News

|                  | k               | $\alpha_k$  | Top words for topic                                    |         |
|------------------|-----------------|---|--|---------|
|                  | <b>-</b> 1      | 0.306   | subject organization israel return define law org      |         |
| ÷                | _ 2             | 0.031   | encryption chip clipper keys des escrow security law   |         |
| <b>←</b>         | - 3             | 0.025   | turkish armenian armenians war turkey turks armenia    |         |
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|                  | 12              | 0.160   | world organization exetem ignal state use every ronly  |         |
| $\leftarrow$     | 13              | 0.042 space nasa gov launch power wire ground air |  |         |
| $\leftarrow \c $ | ← 14            |   | space nasa gov launch power wire grou                  | ind air |
|                  | - 13            | 0.077   | wani game year piay games season piayers nockey        |         |
| ÷                | <del>- 16</del> | 0.158   | car lines dod bike good uiuc sun cars                  |         |
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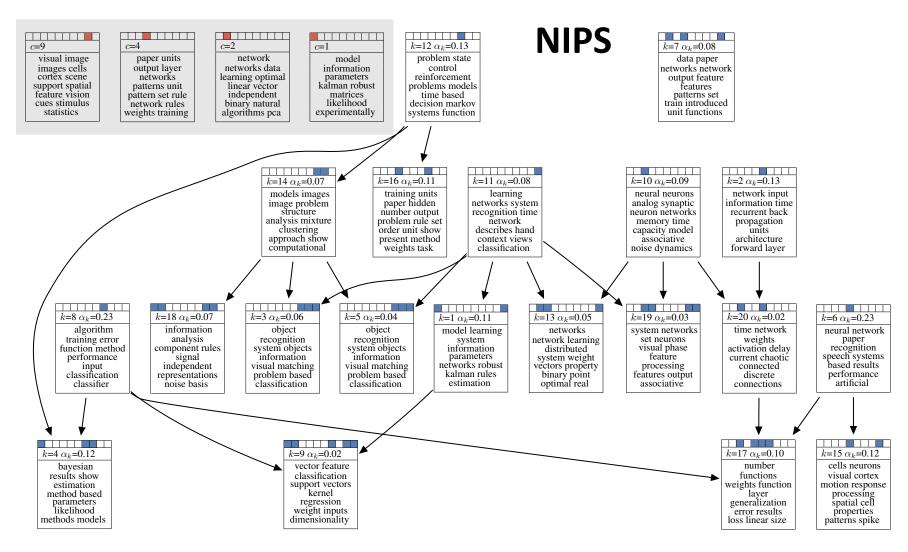
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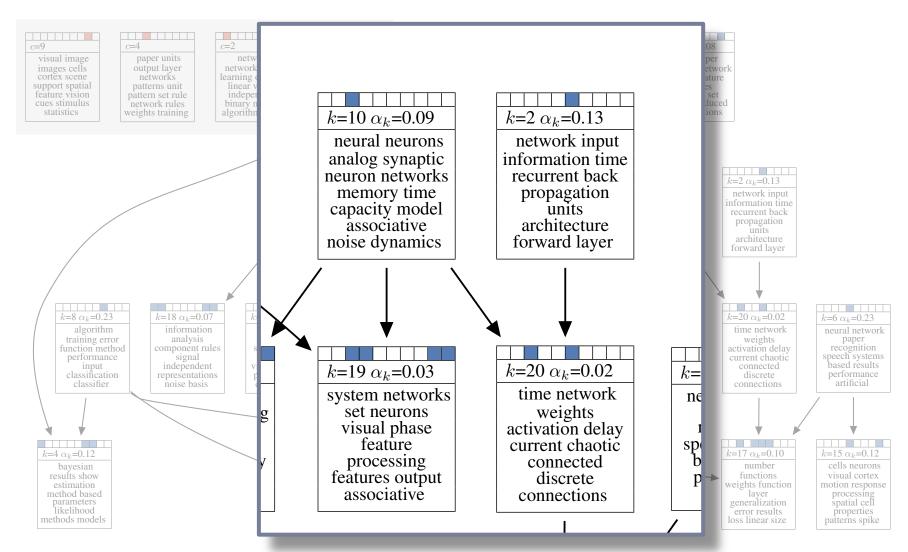
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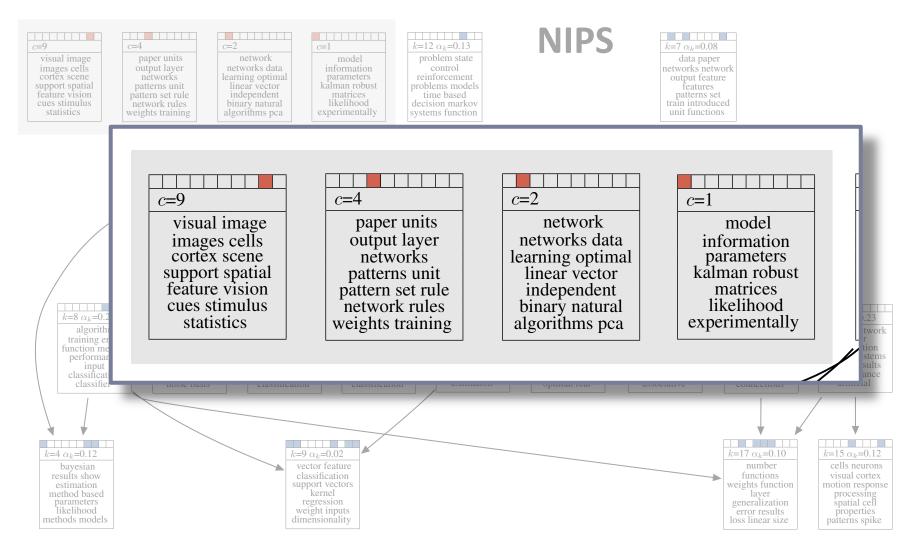
## SCTM: Hasse Diagram over Topics



# SCTM: Hasse Diagram over Topics



## SCTM: Hasse Diagram over Topics



#### Experiments:

- For the same number of components (multinomials),
   SCTM achieves lower perplexity than LDA
- Non-square SCTM achieves lower perplexity than LDA with a more compact model

#### Analysis:

- SCTM learns diverse LDA-like topics
- Components are usually only interpretable when they also appear as a topic
- SCTM learns an implicit Hasse diagram defining subsumption relationships between topics

### Summary

#### Shared Components Topic Model (SCTM):

- 1. Generate a pool of "components" (proto-topics)
- 2. Assemble each topic from some of the components
  - Multiply and renormalize ("product of experts")
- 3. Documents are mixtures of topics (just like LDA)
- So the wordlists of two topics are not generated independently!
- Fewer parameters

### **Future Work**

- Improve inference for SCTM
- Topics as products of components in other applications
  - Selectional preference: components could correspond to semantic features that intersect to define semantic classes
  - Vision: topics are classes of objects, the components could be features of those objects

# Thank you!

Questions, comments?