What Constraints Should OT Allow?

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1. Why bother asking?

Suppose we had a set **Con** of core constraints for phonology—simple mechanisms that could be used to build up all the basic phonological phenomena. What would it look like?

(1) Identifying such core constraints is at the center of the OT program:
"The danger, therefore, lies in ... clinging to a conception of Universal Grammar as little more than a loose organizing framework for grammars. A much stronger stance, in close accord with the thrust of recent work, is available ... Universal Grammar can supply the very substance from which grammars are built: a set of highly general constraints, which, through ranking, interact to produce the elaborate particularity of individual languages." (Prince & Smolensky 1993, p. 198)

(see also Smolensky 1995, Green 1994)

- (2) Some clearly *bad constraints* (but what makes them bad?):
 - a. PALINDROMIC: The candidate reads the same backwards as forwards.
 - b. FTQUINT: Feet are quintary (5 syllables or moras).
 - c. MEMBEROF(a, aardvark, aardvarks, aardwolf, aardwolves, Aaron ...): Candidate must be in the specified set of surface forms.
 - d. MATCHESOUTPUTOFSPE: The output matches the result of applying Chomsky & Halle (1968) to the input.
- (3) Some clearly *okay constraints* (but what makes them okay?):
 - a. CLASH-ATR: Low vowels may not bear the ATR feature.
 - b. ONSET: Every syllable must start with a consonant.
- (4) Some questionable constraints, by the standards of derivational phonology:
 - a. FTBIN: Feet are binary (2 syllables or moras).
 - b. ALIGN-L(Foot, PrWd): The sum of all distances from left edges of feet to the left edge of the PrWd is minimized. (For consequences see (35).)
 - c. Half the constraints that first-year phonology students make up.

Reasons to try to formalize OT, rather than allowing ad hoc English constraints:

- (5) a. Results in an explicit, falsifiable theory of UG
 - b. Constrains linguistic description
 - c. Enables computational work (tools for linguists; algorithms for generation (Eisner, in preparation), parsing, acquisition; theorems on expressive power)
 - d. Exposes formal similarities among constraints (e.g., locality properties; "x projects y" = "y needed to license x" \approx "do not link x to -y segments"; "*[voiced, gl]" = "no implosives")
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- e. Clarifies predictions made by descriptive work (many constraints given informally in the literature, including GA, do not specify how to count violations in all circumstances)
- f. Aids descriptive work by providing well-motivated and well-formalized constraints and representations

The formalization sketched in this talk is called $\mathbf{OTP}\-\!\!\!\!\!-\!\!\!\!\mathrm{OT}$ with primitive constraints.

2. The search for core mechanisms

Ask: What formal devices are regularly used by constraints in the literature?

- (6) a. NASVOI (Itô, Mester, & Padgett 1996) "Every nasal segment must be linked to <u>some</u> voicing feature." b. ONSET ALIGN(σ , L, C, L) $\left. \begin{array}{c} (equivalent) \\ (equivalent) \\ (McCarthy & Prince 1993) \\ (McCarthy & consonant.") \\ (equivalent) \\ (mathematical with) come consonant." \\ (equivalent) \\ (mathematical with) \\ (math$
 - <u>"Every</u> syllable must begin with (be left-aligned with) <u>some</u> consonant."
 c. Common thread: "Every ... some."

 $\forall \alpha, \exists \beta$ such that α and β stand in such-and-such local relationship.

If we allow α and β to be edges (as one option), we only need one kind of local relationship—temporal coocurrence:

(7) The primitive implication family.

 $\alpha \rightarrow \beta$ means: $\forall \alpha, \exists \beta$ such that α and β coincide temporally.

(8) Rewrite (6):
a. nas → voi: ∀nas, ∃voi such that nas and voi coincide temporally.
b. σ[→ C[: ∀σ[, ∃C[such that σ[and C[coincide temporally.

Note that ONSET: $\sigma[\to _C[$, NOONSET: $\sigma[\to _V[$, CODA: $]_{\sigma} \to]_C$, and NOCODA: $]_{\sigma} \to]_V$ are all equally easy to express using this family. So as in other theories, UG must still state that ONSET and NOCODA are strongly preferred by human grammars. (The dispreferred constraints may still be possible: e.g., Hammond 1995 proposes a NOONSET constraint for stressless syllables. See Green 1994 on metaconstraints.)

Thus we can regard alignment as "edge licensing." (Or licensing is "feature alignment.") We can also mix references to edges and interiors:

(9) $F \rightarrow]_{\mu}$: Every foot must cross a mora boundary. (No degenerate feet.) (= MIN-2m: Green & Kenstowicz 1995)

McCarthy & Prince (1993) have previously noted that alignment plays a unifying role, and have suggested that it's *the* core mechanism for all of phonology:

(10) a. "These examples only hint at the generality of the phenomenon to be explored here, which extends to include all the various ways that constituents may be

enjoined to share an edge in prosody and morphology. Data like these have been given widely disparate treatments in the literature \dots " (p. 1)

b. "Taken together with X-like restrictions on immediate domination and interpreted within the appropriate theory of constraint satisfaction, GA provides a mechanism for completely specifying a class of formal languages that, when substantive parameters are set, ought to be all-but-coextensive with possible human languages." (p. 2)

A second constraint family:

Above, we unified feature licensing and alignment. The opposite of feature licensing is feature clash. The opposite of alignment is disalignment, i.e., edge clash.

- (11) a. *[low, ATR] (Cole & Kisseberth 1994) "Low features are incompatible with ATR features." b. NONFINALITY = *ALIGN(PrWd, R, F, R) (e.g., Buckley 1995)
 - "Prosodic words may not be right-aligned with feet."

(12) The primitive **clash** family.

(13) Rewrite (11):
a. low ⊥ ATR: All low and ATR features are temporally disjoint.
b. |_{PrWd} ⊥]_F: Each |_{PrWd} does not coincide with (fall on) any]_F.

Again, this formulation suggests we can mix edges and interiors, and we can:

(14) $F \perp_M$: A foot may not cross a morpheme boundary.

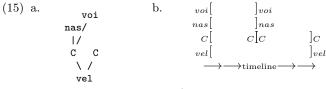
(= TAUTO-F, Crowhurst 1994) (In fact, (14) is more plausible than Crowhurst's formulation, $*_F[\sigma_M[\sigma]_F$. It would be surprising to find a language that crucially blocked $_M[$ only where Crowhurst states, while still allowing it to interrupt a syllable or a ternary foot.)

Null hypothesis: These two families of local primitive constraints — implication and clash—are the *only* ones needed.

 $\begin{array}{l} \alpha \ \rightarrow \ \beta \text{ says that } \alpha \text{'s attract } \beta \text{'s.} \\ \alpha \ \perp \ \beta \text{ says that } \alpha \text{'s repel } \beta \text{'s.} \end{array}$

3. What representations are being constrained?

The primitive constraints are easiest to interpret if we assume that ηk is represented as in (15b), not (15a). This representation is inspired by Optimal Domains Theory (Cole & Kisseberth 1994) and Correspondence Theory (McCarthy & Prince 1995).



(The timeline is really just an ordered set of edge brackets. Thus, only horizontal order matters in the drawing above. Ignore spacing and vertical order.)

- $(16)\;$ Key characteristics of the new representation:
 - a. Constituents float along a *timeline*. Example constituents: *nas* (autosegmental), μ (prosodic), **x** (stress mark), *Stem* (morphological), *H*-domain (feature domain)
 - b. The timeline is continuous, not divided into segments.
 - c. All constituents have width and edges. Thus we can refer naturally to the edges of syllables (or morphemes) whose segmental features are scattered across multiple tiers and perhaps shared with other syllables (cf. Itô & Mester 1994).
 - d. For autosegments with width, such as [nas], think of phonetic gestures. (15b), which begins with simultaneous $_{nas}[$ (= lower the velum) and $_{voi}[$ (= begin vibration of the vocal folds). The primitive constraints can only affect the *order* of bracket edges; it is up to the phonetic component to determine actual durations.
 - e. Association or Correspondence of two constituents is indicated by having them overlap. E.g., the velar gesture in candidate (15b) spans both consonants.
 - f. No need for faithfulness constraints on the insertion, deletion, or relocation of association lines (cf. Kirchner 1993, Myers 1994, Féry 1994).
 - g. No need for (inviolable) well-formedness constraints against gapping or crossing of associations (cf. Kirchner 1993, Féry 1994, Oostendorp 1995).
 - h. No need for Correspondence indices.
- (17) The behavior of **Gen**:
 - a. Gen places constituents *freely* along the continuous timeline. That is, as far as Gen is concerned, brackets may land anywhere. Conditions such as the prosodic hierarchy are enforced by undominated primitive constraints, not by Gen.
 - b. However, Gen requires that edge brackets come in matched pairs.
 - c. Gen also does not allow distinct constituents of the same type (e.g., two syllables or two *lab* autosegments) to overlap. (Elements on the same tier never link to each other.)
 - d. Gen is free only with regard to output material. It is forced to place a copy of the input material into every candidate, on its own tier, for purposes of I-O Correspondence. (Cf. Containment (Prince & Smolensky 1993), Strict Consistency Constraint (Polgardi 1995).)

For computational purposes, regard each candidate timeline as a total ordering over a set of edge brackets.

The lexicon provides an **underspecified timeline**—an ordering over a set of *input* edge brackets. In general this is only a partial ordering, so input constituents may be floating with respect to each other (e.g., floating tones, templatic morphemes). The candidate set consists of all possible fully specified versions of this underspecified timeline.

(18) Because the timeline is continuous rather than divided into segments, brackets can fall in mid-segment:

a. Contour tones: $H\begin{bmatrix} & \\ \\ H\end{bmatrix}H \qquad H$ $L\begin{bmatrix} \\ \\ \\ L\end{bmatrix}L \qquad \therefore \land L$ $V\begin{bmatrix} \\ \\ V\end{bmatrix}V \qquad \forall vowel$ b. Geminates (long vowels are similar): $\sigma\begin{bmatrix} & \\ \\ \sigma\end{bmatrix}\sigma \qquad \sigma \sigma$ $C\begin{bmatrix} \\ \\ \\ C\end{bmatrix}C \qquad C\begin{bmatrix} \\ \\ \\ V\end{bmatrix}V \qquad V\begin{bmatrix} \\ \end{bmatrix}V \qquad C \lor C \lor$

4. Formal definition of the constraints

(19) Formal statement of the primitive constraint families:
a. α → β: Each α temporally overlaps some β. Scoring: Each α without a β incurs one violation mark.
b. α ⊥ β: Each α temporally overlaps no β. Scoring: Each overlap incurs one violation mark.
(20) What can α and β be?
a. Edges such as low[or]low.
b. Interiors such as low. Denote only the interior of a constituent, without its edges. Thus, low and ATR do not overlap here: ATR[]ATR

I.e., the above candidate satisfies $low \perp ATR$ but violates $low \rightarrow ATR$. c. Conjunctions and disjunctions as in (21).

(Dispreferred in analyses, on grounds of their greater complexity—they refer to more features.)

- (21) Occasionally, must allow the following generalized forms of (19). I propose to limit conjunction/disjunction to these configurations only.
 - a. $(\alpha_1 \text{ and } \alpha_2 \text{ and } \dots) \rightarrow (\beta_1 \text{ or } \beta_2 \text{ or } \dots)$ Scoring: Violated once by each set of objects $\{A_1, A_2, \dots\}$ of types $\alpha_1, \alpha_2, \dots$ respectively that all overlap on the timeline and whose intersection does not overlap any object of type β_1, β_2, \dots
 - b. (α_1 and α_2 and ...) \perp (β_1 and β_2 and ...)
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Scoring: Violated once by each set of objects $\{A_1, A_2, \ldots, B_1, B_2, \ldots\}$ of types $\alpha_1, \alpha_2, \ldots, \beta_1, \beta_2, \ldots$ respectively that all overlap on the timeline.

(Could also be notated: $\alpha_1 \perp \alpha_2 \perp \cdots \perp \beta_1 \perp \beta_2 \perp \cdots$.)

Each violation mark is still triggered individually by a bad *local* condition in the candidate, e.g., a moment on the timeline when certain edges are present and others are not.

Note that some constraints require crisp alignment of edges $(x \to y)$, while others are weaker and require only overlap $(x \to y)$, allowing spreading. (Cf. the violable CRISPEDGE constraint of Itô & Mester (1994).)

5. Some further example constraints from the literature

This section illustrates how all the types of primitive constraints are ubiquitous across different areas of phonology.

My apologies in advance for any errors or mischaracterizations in these lists. Some of these translations to OTP are not exact, but appear to act correctly on the data in the papers cited. Also, note that sometimes there is more than one way to paraphrase a constraint.

("ROA" citations point to the Rutgers Optimality Archive at http://ruccs.rutgers.edu/roa.html; they are not further listed in the bibliography of this handout.)

Key to unfamiliar notation:

feat	version of feature on output tier
feat	version of feature on input tier (underline denotes "underlyin' " material)
μ_s	strong mora, containing onset and nucleus (Zec 1988).
μ_w	weak mora, containing coda if any (Zec 1988).
	(One could also use explicit constituents Ons, Nuc, Coda.)
x	a 2ndary stress mark over a stress-bearing unit (first layer of the grid)
Х	a word-primary stress mark (second layer of the grid)
Seg	segmental root node (alternatively, C or V), as distinguished
0	from morphological root <u>Root</u>

Some implication constraints from the literature.

(22) <u>"Same edge" implication:</u>

ALIGN[R][U]. Bradshaw ROA-93j.
ALIGN: Wd] = σ]. Myers, ROA-6.
IAMBIC QUANTITY: In a rhythmic unit (W S), S
is heavy. Hung, ROA-24.
ALIGN-H: Align $(PrWd, R, heavy syllable, R)$.
Kager, ROA-70.

4.	$\mathbf{x}[\rightarrow F[$	FOOT-FORM (trochaic): If there is a head, it is
		on the L. Hung, ROA-9. TROCHAIC: Align($\dot{\sigma}$, L,
		Foot, L). Kager, ROA-35.

- 5. $_{F}[\rightarrow \mathbf{x}[$ ALIGN(Ft, L; Head(Ft), L). Bermudez-Otero, ROA-136.
- 6.] $_{PrWd} \rightarrow$] $_{\mathbf{X}}$ FINAL-STR: Align(domain, R, $\acute{\sigma}$, R). Kager, ROA-35.
- 7. $]_F \rightarrow]_{\sigma}$ FILL: Respect the usual prosodic hierarchy, without catalexis. Inkelas, ROA-39. (Take catalexis to be $_F[\sigma[\cdots]_{\sigma}\cdots]_F$, and assume another constraint $]_F \perp \sigma$.)

c. Feature-prosody interaction

- 1. $_{F}[\rightarrow _{C}[$ ALIGN(Ft, L, Onset): The left edge of a foot must always be aligned to the onset of the first syllable in the foot. Goedemans, ROA-26. (Assume we also have $_{F}[\rightarrow _{\sigma}[.)]$
- 2. $\mathbf{x}[\rightarrow_V[$ NOONSET: Stressless syllables do not have onsets. Hammond, ROA-58.
- 3. $_{H}[\rightarrow _{PrWd}[$ 4. $]_{\mu_{s}} \rightarrow]_{son}$, et al. ALIGN(H tone, L, PWd, L). Myers, ROA-6. HNUC: A higher sonority nucleus is more harmonic than one of lower sonority. Féry, ROA-34, following P&S 1993.
- 5. $]_{\mu_s} \rightarrow]_V$ PROJECT $(\overline{\overline{\mathbb{N}}}, \mathbb{V})$: Nucleus must be a vowel. Oostendorp, ROA-84.
- 6. $\sigma[\rightarrow A_0 [$ STRONG ONSET: Syllables begin with a closure A_0 . Bakovic, ROA-96.
- 7. $(]_{\sigma} \text{ and }]_{hi} \rightarrow]_{back}$ 8. $(]_{low} \text{ and }]_{\sigma} \rightarrow]_{\mathbf{X}}$ 8. $(]_{low} \text{ and }]_{\sigma} \rightarrow]_{\mathbf{X}$
- 9. ($]_{hi}$ and $]_{\sigma}$) \rightarrow ($]_{\mathbf{x}}$ or $]_{back}$) No [i]: [i] is not allowed in unstressed open syllables. Kager, ROA-93a.

d. I-O relationships

u. 1-0	relationships	
1.	$_{H}[\rightarrow \underline{_{H}}[$	LEFT-HD: The leftmost tone bearer of a tone span
		must be a head. Myers, ROA-6.
2.	$]_{ATR} \rightarrow]_{ATRdom}$	BA-rt: Align(Anchor-s, R; [ATR]-domain, R).
		Cole & Kisseberth, ROA-22.
e. Mor	phophonology	

ROA-35; Bermudez-Otero, ROA-136.

-]_{Plural} →]_{son} SON]PL: Plurals end in a sonorant. Golston & Wiese, ROA-100.
 <u>M</u>[→_F[MORPHEME-FOOT-LEFT: Align(Morpheme, L, Foot, L), where "a single violation is assessed for every morpheme which does not meet this requirement." Crowhurst, ROA-19. See also Kager,
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3. Root[→ PrWd[ALIGN-WD: Align(root, Left; PrWd, Left). Cohn
& McCarthy, ROA-25.
4. Root[→
$$\sigma$$
[, etc. ALIGN(Root, σ ; L,R): "Align root morpheme
boundaries with syllable bondaries at both
edges." Yip, ROA-14.
5. Red[→ F[Red = Foot. ROA-16. Carleton & Myers, ROA-
,]_{Red} →]_F 16. (Also need $Red \perp F$ [.)
(23) "Opposite edge" implication:
a. Features
1.]_{lax} → μ_w [PROJECT(lax, \overline{N}): Lax vow-
els are followed by additional
weight (coda consonant or 2nd
half of a diphthong). Oosten-
dorp, ROA-84.
2. μ_w [→]_{lax} PROJECT(\overline{N} , lax): Only lax
vowels are followed by addi-
tional weight (as if tense vow-
els bore their own). Oosten-
dorp, ROA-84.
3. (]_{vel} and c [) → (]_{cont} or]_{voi}) No KC. Bradshaw, ROA-93j.
b. Prosody
1.]x → μ [RHYTHM: A stressed element must
be followed by an unstressed element.
Hung, ROA-9. (Also need]x \perp x[.)
2. (] σ and σ [) NOLAPSE: No adjacent unstressed sylla-
→ (]x or x[) bles. Anttila, ROA-63.
3. (] σ and σ [) LAPSE: Adjacent unstressed syllables are
→ (]x or x[or]_F or F[) separated by a foot boundary. Green,
ROA-45.
c. I-O relationships
1. μ [→] μ LOCAL: An output TBU bearing tone t must be
adjacent to [input] TBU b, where b [also] bears t.

Bickmore (credited to Myers), ROA-161. (Only right spreading actually appears. Note the variation $_{H}[\rightarrow (\underline{_{H}}[\text{ or }]_{\underline{H}}).)$

d. Morphophonology

1. $Affix[\rightarrow]_{PrWd}$ ALIGN-SFX: Align(Affix, L, PrWd, R). Mc-Carthy & Prince, ROA-7.

(24) "Interior" implication: a. Features

 $Round \rightarrow Back.$ Cole & Kisseberth, ROA-1. $rd \rightarrow back$ 98.

2.NASVOI. Itô, Mester, & Padgett, ROA-38; $nas \rightarrow voi$ Yip, ROA-81.

9		WCALL Alter (LTD) dame L. Ward L. (1-1-
3.	$V \rightarrow ATRdom$	WSA-lf: Align([ATR]-dom, L; Word, L). Cole & Kisseberth, ROA-22. (This gets the cor-
		rect, gradient effect of spreading as far as
		possible.)
4.	man Sea ota	- /
4.	$nas \rightarrow Seg, etc.$	Features like <i>nas</i> surface only if linked to a (faithful or epenthetic) segmental root. Zoll,
		ROA-143.
5.	$ATR \rightarrow ATRdom$	
5.	$AI h \rightarrow AI huom$	Not explicitly mentioned in Cole & Kisseberth, ROA-22, but clearly needed there.
6.	$\sigma \rightarrow (H \text{ or } L)$	MAX-ET: Every TBU must have a corre-
0.	$0 \rightarrow (\Pi \text{ of } L)$	spondent tone. McCarthy & Prince (1995).
		SPEC(Tone): Every TBU has a tone. Zoll,
		ROA-143, after Prince & Smolensky (1993).
7.	$V \rightarrow (front \text{ or } rou$	
1.	$v \rightarrow (from of rou)$	<i>nd</i> or <i>low</i>) COLOR: A vowel is [front] or [round] if it is [-low]. Kirchner, ROA-4.
8.	$C \rightarrow (cor \text{ or } lab \text{ or }$	
0.	$C \rightarrow (cor or rad or$	$C \rightarrow TC$. A [+cons] foot domi- nates a consonantal place feature.
		Oostendorp, ROA-84.
9.	(ATRdom and V)	
5.	(111 100000 and V)	Kisseberth, ROA-22.
Pros	sodv	Ribbeberun, 10011 22.
	•	: Every mora must be parsed into a syllable.
	Myers, 1	· · ·
2.		T-TO-STRESS: Heavy syllables are stressed.
	1	ROA-9 (following Prince 1990).
3.		ROOT): Every root node must be associated
	- (yllable or mora.
Feat	ure-prosody interac	ction
1.	$\sigma \rightarrow H$ Fill((σ) : A syllable must be asso-
	ciated	d with a [high tone. Myers,
	ROA	-6.
2.	$V \rightarrow Nuc \qquad V \rightarrow$	σ : A vowel must be a syllable
	head.	Green, ROA-8.
3.	$Nuc \rightarrow son \sigma \rightarrow$	R: A syllable head must be at
	least	a resonant. Green, ROA-8.
4.	$round \rightarrow (back \text{ or } s)$	stress) MAV(PRO) (Marked Vowel (Promi-
		nent)): Umlauted vowels fall in
		prominent syllables. Féry, ROA-34.
~		

5.	$\mathbf{x} \rightarrow (lo \text{ or } hi \text{ or } front \text{ or } back)$	prominent syllables. Féry, ROA-34. NON-HEAD(ə): Stressed schwa is
		prohibited. Cohn & McCarthy, ROA-25.

d. I-O relationships 1. $\underline{H} \rightarrow H$, etc.

b.

c.

- $\underline{H} \rightarrow H$, etc. PARSE(T): A tone must be parsed. Myers, ROA-6.
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2.	$\underline{lab} \rightarrow lab$, etc	2.	MAXPL: Parse underlying place features. Lombardi, ROA-105. MAX, McCarthy &
3.	$lab \rightarrow \underline{lab}, \mathrm{etc}$	2.	Prince 1995. *INS(F): Do not insert features. Kirchner, ROA-4. DEP, McCarthy & Prince 1995.
4.	$\underline{\mu} \rightarrow \mu$		WEIGHTIDENT: If an input vowel is bimoraic, then so is the correspondent output vowel. Pater, ROA-107. See also WEIGHTIDENT,
5.	$\underline{x} \rightarrow x$		Alderete, ROA-131. STRESSIDENT: Parse lexical stress. Pater, ROA-107. HEAD-MAX: Alderete, ROA-131 (from McCarthy 1995).
6.	$(\underline{\mathbf{x}} \text{ and } Affix)$	\rightarrow x	HEAD-MAX _{Affix} : Specializes HEAD-MAX to affixes. Alderete, ROA-131.
7.	$(Seg \text{ and } \mathbf{x})$	$\rightarrow \underline{Seg}$	HEAD-DEP: Every segment contained in a prosodic head in S_2 [output] has a correspondent in S_1 [input]. Roberts-Kohno, ROA-93k.
8.	$(\underline{nas} \text{ and } \mathbf{x})$	\rightarrow nas, etc.	HEADSYLL-MAX(F): No features are deleted from (parsed?) segments in the head syllable. Yip, ROA-159.
9.	$(\underline{\mu} \text{ and } \mathbf{x}) \rightarrow$	μ , etc.	HEAD-WT-IDENT: No lengthening or short- ening of stressed syllables. Alderete, ROA- 131.
10.	$H \rightarrow (\underline{H} \text{ or } \underline{H})$	<u>L</u>)	TPFAITH: Preserve tonal prominence profile. Tranel, ROA-72; Zoll, ROA-143.
e. Mor	phophonology		, , , ,
1.	$\underline{MWd} \rightarrow \mathbf{X}$	lexical head ery MWd o	$_{MWd}$ [Head(PWd)] _{MWd} . A must project a prosodic head: ev- constituent must include a stressed rengthened replacement for Lx \approx PR.) OA-139.
2.	$\underline{M} \rightarrow PrWd$		least one element of a morpheme is l into a prosodic word. Oostendorp,
3.	$\underline{Root} \rightarrow F$	Fт-Rooт: Buckley, RC	The root must overlap with a foot.)A-93c.
(25) "Mixed	l" implication:		
a. Feat			
1.	$upper \rightarrow \mu[$		Minimal Tone Association (MTA): [+upper] must be linked to more than one TBU. Bradshaw, ROA-93j.
~	(] , [)		

- 2. (]_{A0} and _{Af}[) \rightarrow pal NOAFF: Disallows non-palatal affricates. Bakovic, ROA-96. 3. (]_C and _C[) \rightarrow (cor or dors...) CONTACT: Coda should share place with the following Onset [if any]. Kenstowicz, ROA-30. 4. (]_{nas} and $_C[) \rightarrow voi$ *NC: No nasal – voiceless obstruent sequences. Pater, ROA-160.
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5.	$(voi \text{ and } _C[) \rightarrow]_{nas}$	≫	$\dots \gg$ No-NC-Link, Itô, Mester,
			& Padgett, ROA-38.

b. **Prosody**

1. $F \rightarrow \mu[$

2.
$$PrWd \rightarrow _{Seg}[$$

at least two moras. Green & Kenstowicz, ROA-101. DISYLL: The left and right edges of the PrWd, must coincide, respectively, with the left and right edges of *different* syllables. Kager, ROA-70. (Also need $P_{rWd}[\rightarrow Seg[,],]P_{rWd} \rightarrow]Seg.$)

MIN-2m: A metrical foot contains

3. ($]_{\sigma}$ and $_{\sigma}[) \rightarrow (]_{F}$ or $_{F}[$ or F) PARSE-2: One of two adjacent stress units should be parsed by a foot. Kager, ROA-35. PARSE-ADJ-SYLL. Alderete, ROA-94.

underlying tone. Myers, ROA-6.

c. Feature-prosody interaction

1.	$\left(F \left[\text{ and } \underline{Root} \right] \right) \rightarrow C$	[FTONSET $\{rt\}$: Align (Ft that is in
		root, L, C or Root, L). Buckley,
		ROA-56.
2.	$(V \text{ and } \mu_w[) \rightarrow low$	LOWER: Long vowels are low.
		$V_{\mu\mu} \rightarrow [Low]$. Cole & Kisseberth,
		ROA-98.
d. I-O	relationship	
1.	$(H \text{ and } \sigma[) \rightarrow]_{\underline{H}}$	T-BIN: A tone span can have at
		most one non-head (in a domain);
		limits spread to one syllable from

Some clash constraints from the literature.

· · ·	edge" clash:		
a. Pros	ody		
1.	$]_{\mathbf{x}} \perp]_{PrWd}$	*Final Stress. Anttila, ROA-63. Non-Fin($\dot{\sigma}$).	
		Cohn & McCarthy, ROA-25. Cf. RHYTHM, Hung,	
		ROA-9.	
2.	$]_F \perp]_{PrWd}$.	NONFINALITY: Feet should not be word-final.	
		Ní Chiosáin, ROA-89 (credited to Spaelti as	
		WEAKEDGE(P-Cat)), et al.	
b. Feature-prosody interaction			
1.	$\sigma [\perp nas]$	*ONS/N. Smolensky, ROA-86 (following Prince &	
		Smolensky 1993).	
2.	$]_{lax} \perp]_{\sigma}$	$PROJECT(lax, \overline{N})$: Lax vowels are followed by ad-	
		ditional weight (coda consonant or 2nd half of a	
		diphthong). Oostendorp, ROA-84.	
3.	$]_{obs} \perp]_{\mu w}$	*OBSNUC. Pater, ROA-107.	
	$\left(\begin{array}{c} c \end{array} \right)_{\alpha}$ and $\left[\sigma \right]_{\alpha}$		
	(]-]-)	have place features. Lombardi, ROA-105.	

c. I-O relations

C. I-O	relations			
1.	$H[\perp \underline{H}]$		*ALIGN(H,L)-I/O: High tone in output must not left-align with its position in input. Bickmore, ROA-161.	
2.	$(]_{PrWd}$ and $]_{\mu}$	$_w$) \perp] $_V$	FREE-V: <i>PrWd</i> -final vowels must not be parsed. So final heavy syllables are CVC, not CVV. Kager, ROA-70.	
d. Mor	phophonology		0 /	
1.		l· No low vo	owel in a morpheme-final open syl-	
	la	ble. Kager, l	ROA-93c.	
2.			Source Morpheme, L) with no vio- ance. Bickmore, ROA-161.	
(27) "Oppo	site edge" clas		,	
a. Feat				
	$]_H \perp _H[$	Ο	CP: *FF, where F is a parsed [output]	
]11 11[ature specification. "Furthermore, we	
			ill consider two tones to be adjacent	
			they are associated by parsed associa-	
			ons with adjacent tone bearers" (so do-	
			ains are unnecessary). Myers, ROA-6.	
2.	$]_{son} \perp voi[$		rg: No sonorant-voiced clusters. Ní	
2.]son ⊥ voi[hiosáin, ROA-89.	
3.	$(]_{nas}$ and $_C[)$			
J.	$(]_{nas}$ and $C[)$		NÇ: No nasal – voiceless obstruent se- uences. Pater, ROA-160.	
4.	$(]_{vel}$ and $]_{cont}$		NO VELCONT LAB: No sequence of a ve-	
	(Juei and John		lar continuant before a labial. Bradshaw,	
			ROA-93j.	
5.	$\left(\right]_{nas}$ and $_{C}\left[\right)$		NO-NC-LINK. Itô, Mester, & Padgett,	
	(]nus 0[)		ROA-38.	
b. Prosody				
1.		ASH: No ad	jacent strong beats on the grid.	
			. NoClash. Anttila, ROA-63.	
	-		ung, ROA-9.	
2.			ist not be adjacent. Kager, ROA-	
	35.			
(28) <u>"Inter</u>				
a. Features				
1.	$voi \perp gl$	*[voiced, g]	l]: No implosives. Buckley, ROA-57.	
2.	tense \perp low	-	bw: No tense low vowels. Benua, ROA-	
		74.		
3.	$phar \perp dor$	*Mid (no : ROA-94.	mid vowels): *[Phar, Dor]. Alderete,	
4.	$hi \perp low$		rence of +hi and +low. Kirchner,	
4.	100 1 000	ROA-4.	ence of the and thow. Recence,	
5.	$Seg \perp Word$		RE(Root). Myers, ROA-6.	

^{6.} $H \perp Word$ Struct(A): There must be no association. Myers, ROA-6.

7.	low \perp Word *[low].	Oostendorp, ROA-84 (following Prince &
		nsky 1993).
b. Pros		
1.	ter. Nos	CLLABICITY: The fewer syllables, the bet- ske, ROA-109. *STRUC(σ): No syllables.
T (Zoll, RO	
	ure-prosody interaction	
1.		CODA-h: A /h/ may only occur in an onset. Oos- tendorp, ROA-84.
(29) <u>"Mixee</u>	<u>d" clash:</u>	
a. Feat		
1.	$hi \perp_{Seg}[, lo \perp_{Seg}[$	*MULT-HEIGHT: No multiply linked height features. Kirchner, ROA-4.
2.	$front \perp \underline{front}[, \text{ etc.}]$	*Spread: Do not insert association lines.
3.	$RdDom \perp_{HiDom}[, etc$	main must be monotonic: high or low. Cole & Kisseberth, ROA-98. (Cf. para-
4.	$(]_V$ and $_V[) \perp hi$, et	sitic harmony.) tc. NOLONGVOWEL: Two adjacent vocalic roots may not be linked to the same ma- terial (but diphthongs are allowed). Oos- tendorp, ROA-84.
b. Pros	sody	
1.	$F \perp M$	TAUTOMORPHEMIC-FOOT: $*_F[\sigma_M[\sigma]_F.$
	(Crowhurst, ROA-19.
2.	$\mu_s \perp_{Seg}[$	^k BRANCH(S) μ . Walker, ROA-142.
3.	$F \perp \sigma[, \text{ etc.} $ t	UNARITY: A prosodic category p contains no more than one of the next lower prosodic category p-1. A. Green, ROA-115.
4.		SYLLINT: Syllable integrity (violable). Everett,
	•	ROA-163.
5.	$\sigma \perp$ (] _C and _C [) *	COMPLEX: Only one element can be in onset or coda position.
c. Feat	ure-prosody interaction	
		EMINATE: No geminate consonants. Oosten-
1.		rp, ROA-84.
2.	$\sigma \perp_{H}[, \text{etc.} *C$	COMPLEX(T): A tone-bearer must not be asso- ated with more than one tone. Myers, ROA-6.
2		DCOMPLEXONSETORRHYME. Noske, ROA-109.
J. 4		
4.		COMPLEX: No complex onset or coda. Kenstow-
5.	$rime \perp_{nas}[, etc. RI min$	z, ROA-103. HYME HARMONY: All segments in the rhyme ust share any nasal specification. Yip, ROA-81, DA-135.
d. Mor	phophonology	
1.		oot. Carleton & Myers, ROA-16. (Also
	., 1	

 $Red \perp_{F}[, RED = Foot. Carleton & Myers, ROA-16. (Also need __Red[\rightarrow_{F}[,]_{Red} \rightarrow]_{F}.)$

I-O Correspondence (between input and output features): Signaled by alignment between input and output tiers.

Note that when Gen constructs a candidate, it is constrained to place specified lexical material on the input tier, although the position of floating lexical material may be freely chosen.

Correspondence relations with and without spreading:

(30)	a.	voi[<u>voi</u> [Perfect faithfulness
	b.	<u>voi</u> [] <u>voi</u>		Violates Max-IO (Parse): $\underline{voi} \rightarrow voi$
	c.	voi[$]_{voi}$		Violates DEP-IO (FILL): $voi \rightarrow voi$
	d.	voi[<u>voi</u> [] <u>voi</u>]voi	Like (a), this spread version satisfies PARSE & FILL, which only require overlap. Spreading may be required to satisfy some other constraint. On the other hand, various constraints can be invoked against spreading: either $voi \perp]_{voi}$ or $]_{voi} \rightarrow]_{voi}$ or $]_{voi} \rightarrow]_{voi}$ could be used to block (d). (Cf. Yip, 1994:21,fn. 11, on MSEG vs. *Insert Structure)

Thus, the timeline mechanism unifies Correspondence relations with autosegmental associations. Both are encoded by overlap on the constituent timeline. This fleshes out a proposal of McCarthy & Prince (1995):

(31) "The re-casting of autosegmental association in terms of correspondence relations may be expected to have consequences for the analysis of tonal, harmonic, and related phenomena. We do not explore these ideas here, though they are clearly worth developing." (p. 22)

Epenthesis and syncope rely on the fact that the input specifies only a weak partial order of edge brackets—input brackets are ordered with \leq at best. This makes (32) and (33) possible.

(32) Epenthesis ($\underline{CC} \Rightarrow CVC$): the \underline{C} 's are pushed apart.

$$\begin{array}{c|c} v[&]v\\ c[&]c & c[&]c\\ \underline{c}[&]\underline{c} & \underline{c}[&]\underline{c} \end{array}$$

(33) Syncope $(\underline{CVC} \Rightarrow CC)$: the \underline{V} is crushed to zero width so the C's can be adjacent (as encouraged by]_{Segment} \rightarrow _{Segment}[and expected by assimilation constraints).

(Only on the input tier may constituents have zero width.)

$$\begin{array}{c|c} c[& [c &]c \\ \underline{c}[& \underline{c} &]c \\ & \underline{v}[]\underline{v} \end{array}$$

6. How about measuring distance?

Two important differences between $_{F}[\rightarrow PrWd[$ and ALIGN(F, L, PrWd, L):

- The \rightarrow family doesn't measure distance.
- E.g., $(\dot{\sigma}\sigma)(\dot{\sigma}\sigma)(\dot{\sigma}\sigma)\sigma$ violates $_{F}[\rightarrow P_{rWd}]$ twice, once for each non-initial foot.
- The \rightarrow family isn't only used for edges.

Interestingly, Zoll (1996:137–38) has independently argued that licensing has just those properties (leading to her constraint COINCIDE(X,Y)):

"There are two properties of licensing which distinguish it from the cases of affixation discussed [in M&P (1993)].

"First, licensing of marked structure never involves an injunction to be as close to a strong position as possible. Rather, licensing *always* constitutes an all-or-nothing proposition whereby marked structures are licit in licensed positions but ill-formed everywhere else."

"The second important difference is that licensing does not strictly involve coincidence of edges or distance from an edge, but is concerned rather with membership in a constituent which may be peripheral ... [e.g.] heavy syllables belong to the first foot."

Q: Is this local version of alignment powerful enough?

A: Perhaps so. For cases where it's really necessary to measure distance, for example to control the width of a feature domain:

(34) a. $\sigma \rightarrow XDom$: X-domain should be as wide as possible (contain many σ 's). b. $\sigma \perp XDom$: X-domain should be as narrow as possible (contain few σ 's).

Note that this trick, unlike GA, automatically specifies the units of measurement.

Q: Is Generalized Alignment too powerful?

A: Probably. It's a family of non-local constraints that do addition. That lets us express very non-local, unattested phenomena.

Example of unwarranted power: The GA constraint in (35) wants the floating tone to anchor as close to the <u>center of the word</u> as possible (subject to higher-ranked constraints).

(35) Notes:

- 1. $\dot{}$ denotes tone, not stress.
- 2. The n^{th} column records the degree of misalignment of the n^{th} syllable, at least if GA measures this in syllables rather than segments (or moras: see Mester & Padgett (1993)).

$\sigma\sigma\sigma\sigma\sigma\sigma\sigma\sigma + [H]$	ALIGN(σ	, R, <i>H</i> , F	R): each	syll m	ust align	with the	e floating	tone
a. <i>όσσσσσσ</i>	0	*	**	***	****	****	*****	= 21
b. <i>σόσσσσσ</i>	*	0	*	**	***	****	****	= 16
c. σσόσσσσ	**	*	0	*	**	***	****	= 13
♡ d. σσσόσσσ	***	**	*	0	*	**	***	= 12
e. σσσσόσσ	****	***	**	*	0	*	**	= 13
f. σσσσσσσσ	****	****	***	**	*	0	*	= 16
g. σσσσσσσ	*****	****	****	***	**	*	0	= 22
8		\searrow						\smile
		↑					candidate	e's total 🖡

violations contributed by 2nd syllable's misalignment

If there were two floating tones, they'd want to anchor at 1/4 and 3/4 of the way through the word.

This kind of non-local behavior via GA is unattested to my knowledge. It is also beyond the power of known computational OT methods, in particular the finite-state method of Ellison (1995) and the context-free method of Tesar (1996). The primitive constraints are provably incapable of producing such behavior.

7. How to handle non-local phenomena?

Since OTP uses only the primitive constraints of §4, it claims that all phonology is local.

Some apparently non-local phenomena can be reanalyzed:

- *Metrical stress.* Most non-local constraints in the literature concern metrical stress, which has received both local and non-local analyses in the past.
 - Local: Non-OT, iterative accounts (e.g., Prince 1983, Halle & Vergnaud 1987, Kager 1993, Hayes 1985, 1995).
 - Non-local: McCarthy & Prince (1993) propose using Generalized Alignment constraints to measure the distance from each foot to the edge of the word.
 - Non-local: Less powerful alternatives to GA are possible. Could use directional "greedy" versions of primitive constraints like $PARSE(\sigma)$ or FILL(Root), in which early violations count as decisively worse than later ones. (Cf. Kager (1994), who argues for a greedy ALIGN evaluated "foot by foot.")
 - Local: Eisner (in press) gives an OTP typology of metrical stress.
 This paper uses a small set of primitive constraints, which are freely reranked to get attested systems. This gives a unified fine-grained account of the following phenomena described by Hayes (1995).

- 1. asymmetric foot shape typology
- 2. iambic lengthening
- 3. unbounded stress
- 4. simple word-initial and word-final stress
- 5. LR and RL footing, but no clear cases of RL iambs
- 6. syllable and foot extrametricality
- 7. no cases of final-syllable extrametricality for LR trochees
- 8. strong and weak prohibitions on degenerate feet
- 9. word-level stress, including prominence-based systems

The asymmetries above are reduced to (i) the universal onset-coda asymmetry and (ii) the universal tendency of extrametricality to be final.

• Intervocalic phenomena (e.g., lenition). A constraint like *VsV (Green & Kenstowicz 1995) appears non-local, since [s] must look to both sides to decide whether it can surface as s or must become z. However, a local reanalysis is possible.

Sample reanalysis: For *VsV, say that /s/ always wants to surface as [z], but only succeeds in the VsV context. For instance: (*cor* and *cont*) \rightarrow *voi* rules out [s] in favor of [z]. It is outranked by $]_z \rightarrow (]_{voi}$ or $_V[$), which says that any surface [z] not underlyingly voiced is followed by a vowel, and also by the mirror image of this, so that such a [z] must also be preceded by a vowel. Here $]_z$ abbreviates ($]_{cor}$ and $]_{cont}$ and $]_{voi}$).

However, *reduplication* occupies a special role in phonology, in that it is inherently non-local; it cannot be reanalyzed as local.

Therefore, to handle reduplication in OTP we need a representational trick (similar to Clements 1985). Translate the Correspondence account of McCarthy & Prince (1995) into OTP as follows:

- a. As for all relations, OTP can enforce Correspondence only locally, so Correspondent elements must always overlap on the timeline,
- b. Thus, I-B faithfulness requires I and B to occupy the same portion of the timeline. (on separate input and output tiers)
- c. B-R faithfulness apparently requires R and B to occupy the same portion of the timeline. But this would rule out B-R juncture effects. which require B to precede R or vice-versa. (e.g., enforcement of *VhV in Javanese)
- d. So instead require R (on the output tier) and a <u>copy</u> of B (on its own special tier) to occupy the same portion of the timeline.
- e. Gen produces only candidates in which this copy of B is perfect. Thus, Gen must know how to do reduplication of morphemes, not just affixation.
- f. Now all the non-locality is handled within Gen; the violable constraints remain local.
- (36) Some candidates produced by Gen on RED(*b*)*dah*)-e. In Javanese, first candidate wins.

\mathbf{a} .	$\underline{badah-e}$	Input tier (used for I-B faithfulness)
	bəda bəda <u>-e</u>	Output tier: passed to phonetics (here violates MAX-IO)
	[Red][Base][Af]	Morphemic tier: mentioned by some constraints
	<u>bəda</u> 🖌	Exact copy of base (used for B-R correspondence)

b.	<u>bədah-e</u>	
	bədahbədah <u>-e</u>	Satisfies MAX-IO, but violates surface constraint $*VhV$
	[Red][Base][Af]	
	<u>bədah</u> ∠	Exact copy of this candidate's base (enforced by Gen)
	, , ,	
c.	$\underline{badah-e}$	
	bədahbəda <u>-e</u>	Satisfies MAX-IO & * <i>VhV</i> , but not DEP-BR, i.e., $C \rightarrow \underline{C}$
	[Red][Base][Af]	—
	bəda 🖌	Exact copy of this candidate's base (enforced by Gen)
d.	bədah-e	
	bəda bədah-e	Satisfies MAX-IO & * <i>VhV</i> , but not MAX-BR, i.e, $\underline{C} \rightarrow C$
	[Red][Base][Af]	
	,	
	<u>bədah</u> ∠	Exact copy of this candidate's base (enforced by Gen)

In a language also requiring I-R faithfulness (McCarthy & Prince's (1995) Full Model), Gen must put two copies on the input tier: bədah bədah-e.

Haplology is a related example that may also be intrinsically non-local. (Yip 1995)

8. What role do the primitive constraints play in OT?

Three kinds of constraints:

• Primitive: the implication and clash families.

• Compound: Expressible as a monolithic block of primitive constraints in fixed order. (Kennedy (1996) uses blocks of Align constraints.)

• Complex: Any constraint not expressible in this restricted framework.

The balance among these remains to be seen. It is not yet clear what compound or complex constraints are actually needed (and which of the primitive constraints are *not* needed!).

We must also discover which of the formally possible primitive constraints are favored in real languages (on phonetic or other grounds), and what rankings are favored. OTP claims that languages use only local constraints; but it does not say *which* local constraints.

Meanwhile,

• Primitive constraints are "safe to use." They're simple, radically local, and ubiquitous.

• The restricted version of OT allowing *only* primitive constraints—called OTP— is easy to reason within and is computationally tractable.

• OTP is the simplest explanation that stands a chance. Let's refine it against the data, adding new core constraints only as we're forced to.

• If OTP is close to correct, it may be fruitful to reanalyze languages and typologies within OTP. (For concreteness, see Eisner (in press) for a detailed reanalysis of stress typology that has some empirical benefits.)

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