Transformational Priors Over Grammars

Jason Eisner

Johns Hopkins University

July 6, 2002 — EMNLP

The Big Concept

- Want to parse (or build a syntactic language model).
- Must estimate rule probabilities.
- **Problem:** Too many possible rules!
  - Especially with lexicalization and flattening (which help).
  - So it's hard to estimate probabilities.

The Big Concept

- **Problem:** Too many rules!
  - Especially with lexicalization and flattening (which help).
  - So it's hard to estimate probabilities.

- **Solution:** Related rules tend to have related probs
  - *POSSIBLE* relationships are given a priori
  - *LEARN* which relationships are strong in <u>this</u> language
    - *(just like feature selection)*

- Method has connections to:
  - Parameterized finite-state machines (Monday's talk)
  - Bayesian networks (inference, abduction, explaining away)
  - Linguistic theory (transformations, metarules, etc.)

Problem: Too Many Rules


```
26  NP → DT fund
24  NN → fund
 8  NP → DT NN fund
 7  NNP → fund
 5  S  → TO fund NP
 2  NP → NNP fund
 2  NP → DT NPR NN fund
 2  S  → TO fund NP PP
 1  NP →    DT JJ NN fund
 1  NP →    DT NPR JJ fund
 1  NP →    DT ADJP NNP fund
 1  NP →    DT JJ JJ NN fund
 1  NP →    DT NN fund SBAR
 1  NPR →   fund
 1  NP-PRD → DT NN fund VP
 1  NP →    DT NN fund PP
 1  NP →    DT ADJP NN fund ADJP
 1  NP →    DT ADJP fund PP
 1  NP →    DT JJ fund PP-TMP
 1  NP-PRD → DT ADJP NN fund VP
 1  NP →    NNP fund , VP ,
 1  NP →    PRP$ fund
 1  S-ADV →  DT JJ fund
 1  NP →    DT NNP NNP fund
 1  SBAR →  NP MD fund NP PP
 1  NP →    DT JJ JJ fund SBAR
 1  NP →    DT JJ NN fund SBAR
 1  NP →    DT NNP fund
 1  NP →    NP$ JJ NN fund
 1  NP →    DT JJ fund
```

[Want To Multiply Rule Probabilities]


```
26  NP → DT fund
24  NN → fund
 8  NP → DT NN fund
 7  NNP → fund
 5  S  → TO fund NP
 2  NP → NNP fund
 2  NP → DT NPR NN fund
 2  S  → TO fund NP PP
 1  NP →    DT JJ NN fund
 1  NP →    DT NPR JJ fund
 1  NP →    DT ADJP NNP fund
 1  NP →    DT JJ JJ NN fund
 1  NP →    DT NN fund SBAR
 1  NPR →   fund
 1  NP-PRD → DT NN fund VP
 1  NP →    DT NN fund PP
 1  NP →    DT ADJP NN fund ADJP
 1  NP →    DT ADJP fund PP
 1  NP →    DT JJ fund PP-TMP
...
 1  SBAR →  NP MD fund NP PP
 1  NP →    DT JJ JJ fund SBAR
 1  NP →    DT JJ NN fund SBAR
 1  NP →    DT NNP fund
 1  NP →    NP$ JJ NN fund
 1  NP →    DT JJ fund
```

$\mathbf{p(tree)} = ... \; p(\triangle \mid S) \times p(\triangle \mid TO) \times p(\triangle \mid NP) \times p(\triangle \mid SBAR) \times ...$
(oversimplified)

Too Many Rules …
But Luckily …


```
26  NP → DT fund
24  NN → fund
 8  NP → DT NN fund
 7  NNP → fund
 5  S  → TO fund NP
 2  NP → NNP fund
 2  NP → DT NPR NN fund
 2  S  → TO fund NP PP
 1  NP →    DT JJ NN fund
 1  NP →    DT NPR JJ fund
 1  NP →    DT ADJP NNP fund
 1  NP →    DT JJ JJ NN fund
 1  NP →    DT NN fund SBAR
 1  NPR →   fund
 1  NP-PRD → DT NN fund VP
 1  NP →    DT NN fund PP
 1  NP →    DT ADJP NN fund ADJP
 1  NP →    DT ADJP fund PP
 1  NP →    DT JJ fund PP-TMP
 1  NP-PRD → DT ADJP NN fund VP
 1  NP →    NNP fund , VP ,
 1  NP →    PRP$ fund
 1  S-ADV →  DT JJ fund
 1  NP →    DT NNP NNP fund
 1  SBAR →  NP MD fund NP PP
 1  NP →    DT JJ JJ fund SBAR
 1  NP →    DT JJ NN fund SBAR
 1  NP →    DT NNP fund
 1  NP →    NP$ JJ NN fund
 1  NP →    DT JJ fund
```

All these rules for <u>fund</u> –
& other, still unobserved rules –
are **connected** by the deep
structure of English.

Rules Are Related

- <u>fund</u> behaves like a typical singular noun ...

one fact!
though PCFG represents it as many apparently unrelated rules.

```
26  NP  → DT fund
24  NN  → fund
8   NP  → DT NN fund
7   NNP →  fund
5   S   →  TO fund NP
```
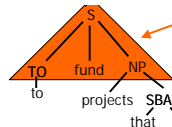
```
1   NP  →   DT NPR JJ fund
1   NP  →   DT ADJP NNP fund
1   NP  →   DT JJ JJ NN fund
1   NP  →   DT NN fund SBAR
1   NPR →   fund
1   NP-PRD → DT NN fund VP
1   NP  →   DT NN fund PP
1   NP  →   DT ADJP NN fund ADJP
1   NP  →   DT ADJP fund PP
1   NP  →   DT JJ fund PP-TMP
1   NP-PRD → DT ADJP NN fund VP
1   NP  →   NNP fund , VP ,
1   NP  →   PRP$ fund
1   S-ADV → DT JJ fund
1   NP  →   DT NNP NNP fund
1   NP  →   NP MD fund NP PP
1   NP  →   DT JJ JJ fund SBAR
1   NP  →   DT JJ NN fund SBAR
1   NP  →   DT NPR fund
1   NP  →   NPS JJ NN fund
1   NP  →   DT JJ fund
```
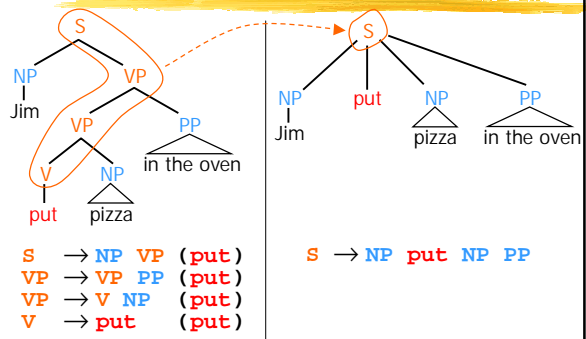
Rules Are Related

- <u>fund</u> behaves like a typical singular noun ...
- ... **or** transitive verb ...

one more fact!
even if several more rules.
Verb rules are **RELATED**.
Should be able to **PREDICT** the ones we haven't seen.

S
TO   fund   NP
to
projects   SBAR
that   ...

```
26  NP  → DT fund
24  NN  → fund
8   NP  → DT NN fund
7   NNP →  fund
5   S   →  TO fund NP
2   NP  → NNP fund
2   NP  → DT NPR NN fund
2   S   →  TO fund NP PP
1   NP  →  DT JJ NN fund
1   NP  →  DT NPR JJ fund
1   NP  →  DT ADJP NNP fund
1   NP  →  DT JJ JJ NN fund
1   NP  →  DT NN fund SBAR

1   NP  →  DT ADJP fund PP
1   NP  →  DT JJ fund PP-TMP
1   NP-PRD → DT ADJP NN fund VP
1   NP  →  NNP fund , VP ,
1   NP  →  PRP$ fund
1   S-ADV → DT JJ fund
1   NP  →  DT NNP NNP fund
1   SBAR →  NP MD fund NP PP
1   NP  →  DT JJ JJ fund SBAR
1   NP  →  DT JJ NN fund SBAR
1   NP  →  DT NNP fund
1   NP  →  NPS JJ NN fund
1   NP  →  DT JJ fund
```

Rules Are Related

- <u>fund</u> behaves like a typical singular noun ...
- ... **or** transitive verb ...
- ... but as noun, has an idiosyncratic fondness for purpose clauses ...

the ACL fund to put proceedings online
the old ACL fund for students to attend ACL
one more fact!
predicts dozens of unseen rules

```
26  NP  → DT fund
24  NN  → fund
8   NP  → DT NN fund
7   NNP →  fund
5   S   →  TO fund NP
2   NP  → NNP fund
2   NP  → DT NPR NN fund
2   S   →  TO fund NP PP
1   NP  →   DT JJ NN fund
1   NP  →   DT NPR JJ fund
1   NP  →   DT ADJP NNP fund
1   NP  →   DT JJ JJ NN fund
1   NP  →   DT NN fund SBAR

1   NP-PRD → DT NN fund VP
1   NP  →   DT NN fund PP
1   NP  →   DT ADJP fund PP
1   NP  →   DT JJ fund PP-TMP
1   NP-PRD → DT ADJP NN fund VP
1   NP  →   NNP fund , VP ,
1   NP  →   PRP$ fund
1   S-ADV → DT JJ fund
1   NP  →   DT NNP NNP fund
1   SBAR → NP MD fund NP PP
1   NP  →   DT JJ JJ fund SBAR
1   NP  →   DT JJ NN fund SBAR
1   NP  →   DT NNP fund
```

Rules Are Related

- <u>fund</u> behaves like a typical singular noun ...
- ... **or** transitive verb ...
- ... but as noun, has an idiosyncratic fondness for purpose clauses ...
- ... and maybe other idiosyncrasies to be discovered, like unaccusativity ...

```
26  NP  → DT fund
24  NN  → fund
8   NP  → DT NN fund
7   NNP →  fund
5   S   →  TO fund NP
2   NP  → NNP fund
?   NP  → DT NPR NN fund
```

NSF issued the grant
The grant issued today

⬇ ???

NSF funded the grant
The grant funded today

unlikely sentence, but if we do see it,
is unaccusativity **plausible**? (vs. other parse)

All This Is Quantitative!

- <u>fund</u> behaves like a typical singular noun ...
- ... **or** transitive verb ...
- ... but as noun, has an idiosyncratic fondness for purpose clauses ...
- ... and maybe other idiosyncrasies to be discovered, like unaccusativity ...

```
26  NP  → DT fund
24  NN  → fund
8   NP  → DT NN fund
7   NNP →  fund
5   S   →  TO fund NP
    NP  → NNP fund
2   NP  → DT NPR NN fund
    →   TO fund NP PP
```

how often?

and how does that tell us p(rule)?

Format of the Rules

S
NP
Jim
VP
VP
V
put
NP
pizza
PP
in the oven

S
NP
Jim
put
NP
pizza
PP
in the oven

```
S  → NP VP (put)
VP → VP PP (put)
VP → V NP  (put)
V  → put   (put)
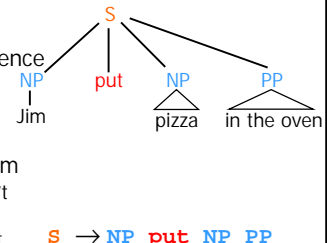```

```
S → NP put NP PP
```

Format of the Rules

Why use flat rules?
- Avoids silly independence assumptions: a win
  - Johnson 1998 →
  - New experiments
- Our method likes them
  - Traditional rules aren't systematically related
  - But relationships exist among wide, flat rules that express different ways of filling same roles

S (tree): NP [Jim], put, NP [pizza], PP [in the oven]
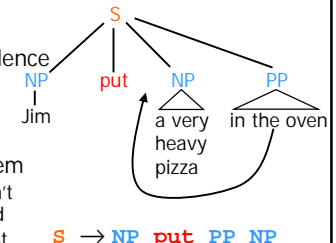
S → NP put NP PP

Format of the Rules

Why use flat rules?
- Avoids silly independence assumptions: a win
  - Johnson 1998 →
  - New experiments
- Our method likes them
  - Traditional rules aren't systematically related
  - But relationships exist among wide, flat rules that express different ways of filling same roles

S (tree): NP [Jim], put, NP [a very heavy pizza], PP [in the oven]

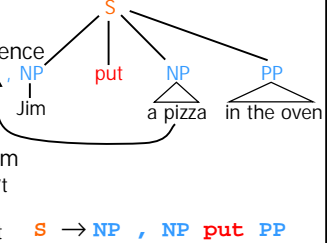**S → NP put PP NP**

Format of the Rules

Why use flat rules?
- Avoids silly independence assumptions: a win
  - Johnson 1998 →
  - New experiments
- Our method likes them
  - Traditional rules aren't systematically related
  - But relationships exist among wide, flat rules that express different ways of filling same roles

S (tree): , NP [Jim], put, NP [a pizza], PP [in the oven]

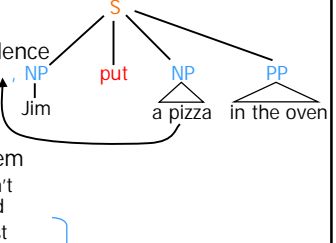**S → NP , NP put PP**

Format of the Rules

Why use flat rules?
- Avoids silly independence assumptions: a win
  - Johnson 1998 →
  - New experiments
- Our method likes them
  - Traditional rules aren't systematically related
  - But relationships exist among wide, flat rules that express different ways of filling same roles

S (tree): , NP [Jim], put, NP [a pizza], PP [in the oven]

in short, flat rules are the **locus of transformations**

Format of the Rules

Why use flat rules?
- Avoids silly indep. assumptions: a win
  - Johnson 1998 →
  - New experiments
- Our method likes them
  - Traditional rules aren't systematically related
  - But relationships exist among wide, flat rules that express different ways of filling same roles

flat rules are the **locus of exceptions**
(e.g., put is exceptionally likely to take a PP, but not a second PP)

in short, flat rules are the **locus of transformations**

Intuition: Listing is costly and hard to learn. Most rules are derived.

Hey – Just Like Linguistics!

Lexicalized syntactic formalisms: CG, LFG, TAG, HPSG, LCFG ...

- Grammar = set of "lexical entries" very like flat rules
- Exceptional entries OK

flat rules are the **locus of exceptions**
(e.g., put is exceptionally likely to take a PP, but not a second PP)

listed entries

derived entries

- Explain "coincidental" patterns of lexical entries: metarules/ transformations/lexical redundancy rules

in short, flat rules are the **locus of transformations**

- **Input:** Rule counts   *(from parses or putative parses)*
- **Output:** Probability distribution over rules
- **Evaluation:** Perplexity of held-out rule counts
  - That is, did we assign high probability to the rules needed to correctly parse test data?

- **Input:** Rule counts   *(from parses or putative parses)*
- **Output:** Probability distribution over rules
- **Evaluation:** Perplexity of held-out rule counts

Rule probabilities: $p(S \rightarrow$ NP put NP PP $\mid$ S,put$)$

Infinite set of possible rules; so we will estimate

$p(S \rightarrow$ NP Adv PP put PP PP NP AdjP S $\mid$ S, put$)$
= a very tiny number > 0

Grid of Lexicalized Rules

S → ...	encourage	question	fund	merge	repay	remove
To — NP						
To — NP PP						
To AdvP — NP						
To AdvP — NP PP						
To — PP						
To — S						
NP — NP .						
NP — NP PP .						
NP Md — NP						
NP Md — NP PPTmp						
NP Md — PP PP						
NP — SBar .						
(etc.)						

S → To **fund** NP PP
("to fund projects with ease")

S → To **merge** NP PP
("to merge projects with ease")

Training Counts

S → ...	encourage	question	fund	merge	repay	remove
To — NP	1	1	5	1	3	2
To — NP PP	1	1	2	2	1	1
To AdvP — NP						1
To AdvP — NP PP						1
NP — NP .		2				
NP — NP PP .	1					
NP Md — NP	1					
NP Md — NP PPTmp					1	
NP Md — PP PP						1
To — PP			1			
To — S	1					
NP — SBar .		2				
(other)						

Count of (word, frame)

Naive prob. estimates (MLE model)

S → ...	encourage	question	fund	merge	repay	remove
To — NP	200	167	714	250	600	333
To — NP PP	200	167	286	500	200	167
To AdvP — NP	0	0	0	0	0	167
To AdvP — NP PP	0	0	0	0	0	167
NP — NP .	0	333	0	0	0	0
NP — NP PP .	200	0	0	0	0	0
NP Md — NP	200	0	0	0	0	0
NP Md — NP PPTmp	0	0	0	0	200	0
NP Md — PP PP	0	0	0	0	0	167
To — PP	0	0	0	250	0	0
To — S	200	0	0	0	0	0
NP — SBar .	0	333	0	0	0	0
(other)	0	0	0	0	0	0

Estimate of p(frame | word) * 1000

TASK: counts → probs   *("smoothing")*

S → ...	encourage	question	fund	merge	repay	remove
To — NP	142	117	397	210	329	222
To — NP PP	77	64	120	181	88	80
To AdvP — NP	0.55	0.47	1.1	0.82	0.91	79
To AdvP — NP PP	0.18	0.15	0.33	0.37	0.26	50
NP — NP .	22	161	7.8	7.5	7.9	7.5
NP — NP PP .	79	8.5	2.6	2.7	2.6	2.6
NP Md — NP	90	2.1	2.4	2.0	24	2.6
NP Md — NP PPTmp	1.8	0.16	0.17	0.16	69	0.19
NP Md — PP PP	0.1	0.027	0.027	0.038	0.078	59
To — PP	9.2	6.5	12	126	10	9.1
To — S	98	1.6	4.3	3.9	3.6	2.7
NP — SBar .	3.4	190	3.2	3.2	3.2	3.2
(other)	478	449	449	461	461	482

Estimate of p(frame | word) * 1000

Smooth Matrix via LSA / SVD, or SBS?

S → ...	encourage	question	fund	merge	repay	remove
To — NP	1	1	5	1	3	2
To — NP PP	1	1	2	2	1	1
To AdvP — NP						1
To AdvP — NP PP						1
NP — NP .		2				
NP — NP PP .	1					
NP Md — NP	1					
NP Md — NP PPTmp				1		
NP Md — PP PP						1
To — PP				1		
To — S	1					
NP — SBar .		2				
(other)						

Count of (word, frame)

Smoothing via a Bayesian Prior

- Choose grammar to maximize
  p(observed rule counts | grammar)*p(grammar)

- grammar = probability distribution over rules

- **Our job:** Define p(grammar)
- **Question:** What makes a grammar likely,
  a priori?

- **This paper's answer:** Systematicity.
  Rules are mainly derivable from other rules.
  Relatively few stipulations ("deep facts").
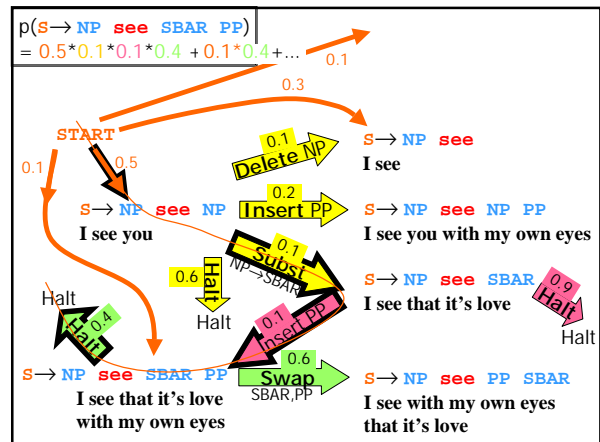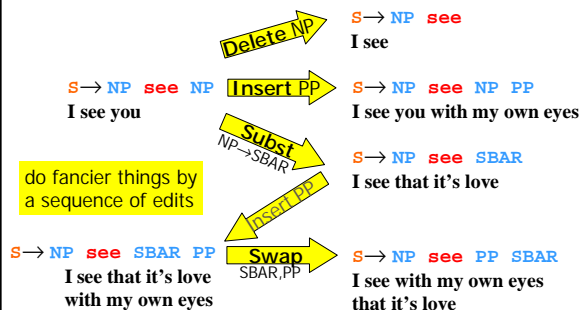

Only a Few Deep Facts

- <u>fund</u> behaves like a transitive verb 10% of time ...

- and noun 90% of time ...

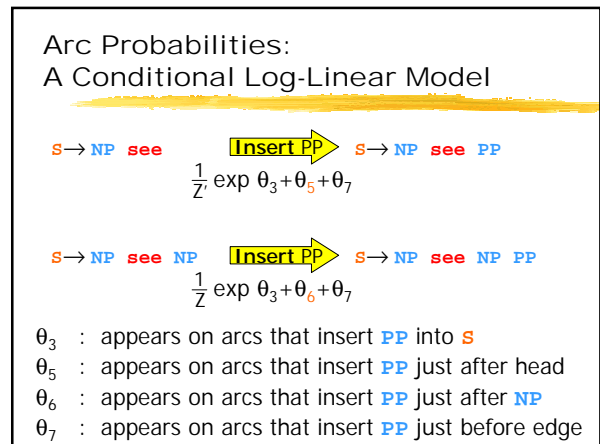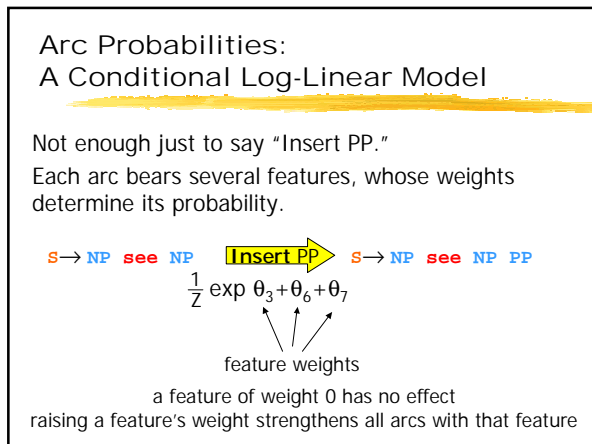- ... takes purpose clauses 5 times as often as typical noun.
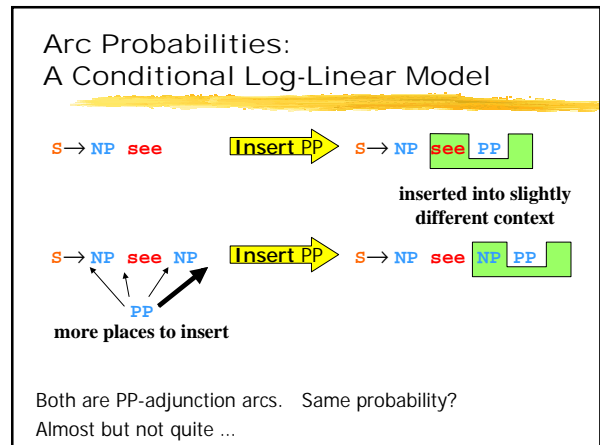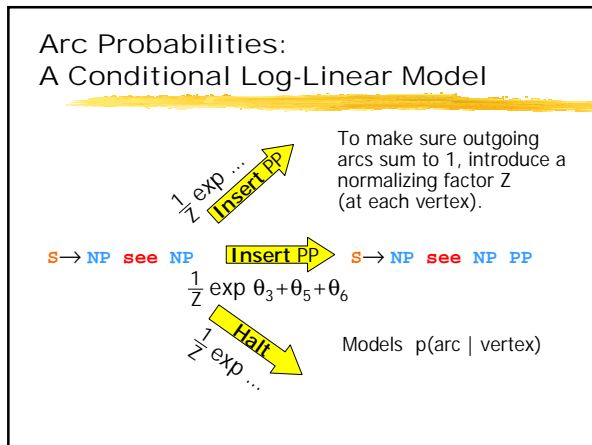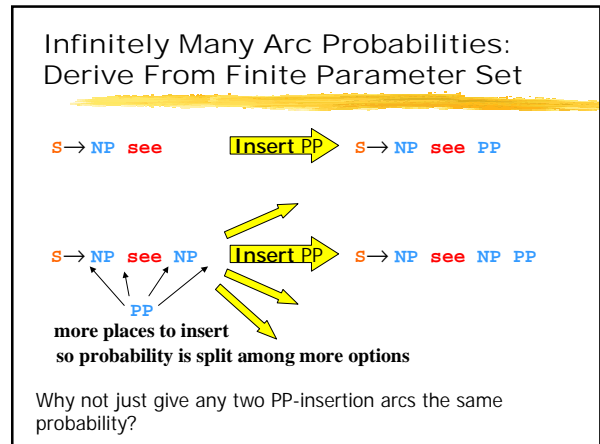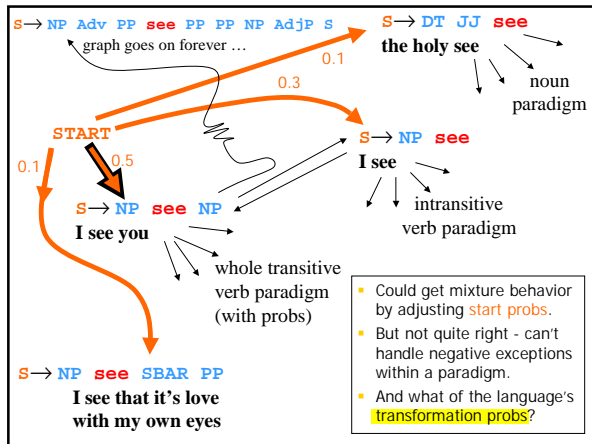
```
26  NP  → DT fund
24  NN  → fund
 8  NP  → DT NN fund
 7  NNP →  fund
 5  S   → TO fund NP
 2  NP  → NNP fund
 2  NP  → DT NPR NN fund
 2  S   → TO fund NP PP
 1  NP →         DT JJ NN fund
 1  NP →         DT NPR JJ fund
 1  NP →         DT ADJP NNP fund
 1  NP →         DT JJ JJ NN fund
 1  NP →         DT NN fund SBAR
 1  NPR →        fund
 1  NP-PRD →     DT NN fund VP
 1  NP →         DT NN fund PP
 1  NP →         DT ADJP NN fund ADJP
 1  NP →         DT ADJP fund PP
 1  NP →         DT JJ fund PP-TMP
 1  NP-PRD →     DT ADJP NN fund VP
 1  NP →         NNP fund , VP ,
 1  S-ADV →      DT JJ fund
 1  NP →         DT NNP NNP fund
 1  SBAR →       NP MD fund NP PP
 1  NP →         DT JJ JJ fund SBAR
 1  NP →         DT JJ NN fund SBAR
 1  NP →         DT NNP fund
 1  NP →         NP$ JJ NN fund
 1  NP →         DT JJ fund
```

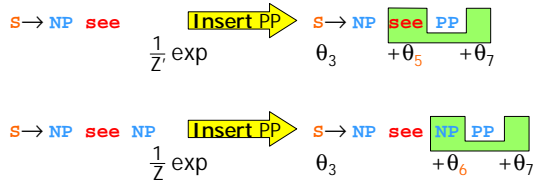## Smoothing via a Bayesian Prior

- Previous work (several papers in past decade):
  - Rules should be few, short, and approx. equiprobable
  - These priors try to keep rules **out of** grammar
  - Bad idea for lexicalized grammars ...

- This work:
  - Prior tries to get related rules **into** grammar
  - transitive ➜ passive at ≈1/20 the probability
    - NSF spraggles the project ➜ The project is spraggled by NSF
    - Would be weird for the passive to be missing, and prior knows it!
    - In fact, weird if p(passive) is too far from 1/20 * p(active)
  - Few facts, not few rules!

---

for now, stick to Simple Edit Transformations

5

Slide 1

S→ NP Adv PP **see** PP PP NP AdjP S
    graph goes on forever …

S→ DT JJ **see**
the holy see
    noun paradigm

START

0.1

0.3

0.1   0.5

S→ NP **see**
I see
    intransitive verb paradigm

S→ NP **see** NP
I see you

whole transitive verb paradigm (with probs)

S→ NP **see** SBAR PP
I see that it's love with my own eyes

- Could get mixture behavior by adjusting start probs.
- But not quite right - can't handle negative exceptions within a paradigm.
- And what of the language's transformation probs?

Slide 2

Infinitely Many Arc Probabilities: Derive From Finite Parameter Set

S→ NP **see**   **Insert** PP   S→ NP **see** PP

S→ NP **see** NP   **Insert** PP   S→ NP **see** NP PP

PP
more places to insert
so probability is split among more options

Why not just give any two PP-insertion arcs the same probability?

Slide 3

Arc Probabilities: A Conditional Log-Linear Model

$\frac{1}{Z}$ exp … **Insert** PP

To make sure outgoing arcs sum to 1, introduce a normalizing factor Z (at each vertex).

S→ NP **see** NP   **Insert** PP   S→ NP **see** NP PP

$\frac{1}{Z}$ exp $\theta_3 + \theta_5 + \theta_6$

$\frac{1}{Z}$ exp … **Halt**

Models p(arc | vertex)

Slide 4

Arc Probabilities: A Conditional Log-Linear Model

S→ NP **see**   **Insert** PP   S→ NP **see** PP

inserted into slightly different context

S→ NP **see** NP   **Insert** PP   S→ NP **see** NP PP

PP
more places to insert

Both are PP-adjunction arcs. Same probability?
Almost but not quite …

Slide 5

Arc Probabilities: A Conditional Log-Linear Model

Not enough just to say "Insert PP."

Each arc bears several features, whose weights determine its probability.

S→ NP **see** NP   **Insert** PP   S→ NP **see** NP PP

$\frac{1}{Z}$ exp $\theta_3 + \theta_6 + \theta_7$

feature weights

a feature of weight 0 has no effect
raising a feature's weight strengthens all arcs with that feature

Slide 6

Arc Probabilities: A Conditional Log-Linear Model

S→ NP **see**   **Insert** PP   S→ NP **see** PP

$\frac{1}{Z'}$ exp $\theta_3 + \theta_5 + \theta_7$

S→ NP **see** NP   **Insert** PP   S→ NP **see** NP PP

$\frac{1}{Z}$ exp $\theta_3 + \theta_6 + \theta_7$

θ_3 : appears on arcs that insert **PP** into **S**
θ_5 : appears on arcs that insert **PP** just after head
θ_6 : appears on arcs that insert **PP** just after **NP**
θ_7 : appears on arcs that insert **PP** just before edge

Arc Probabilities: A Conditional Log-Linear Model

S→ NP see **Insert PP** S→ NP see PP

$\frac{1}{Z}\exp$ θ_3 $+\theta_5$ $+\theta_7$

S→ NP see NP **Insert PP** S→ NP see NP PP

$\frac{1}{Z}\exp$ θ_3 $+\theta_6$ $+\theta_7$

θ_3 : appears on arcs that insert **PP** into **S**
θ_5 : appears on arcs that insert **PP** just after head
θ_6 : appears on arcs that insert **PP** just after **NP**
θ_7 : appears on arcs that insert **PP** just before edge

Arc Probabilities: A Conditional Log-Linear Model

S→ NP see **Insert PP** S→ NP see PP

$\frac{1}{Z}\exp$ θ_3 $+\theta_5$ $+\theta_7$

S→ NP see NP **Insert PP** S→ NP see NP PP

$\frac{1}{Z}\exp$ θ_3 $+\theta_6$ $+\theta_7$

These arcs share most features.
So their probabilities tend to rise and fall together.
To fit data, could manipulate them independently (via θ_5,θ_6).

Prior Distribution

- PCFG grammar is **determined** by $\theta_0, \theta_1, \theta_2, \ldots$

Universal Grammar

Instantiated Grammar

Prior Distribution

- Grammar is **determined** by $\theta_0, \theta_1, \theta_2, \ldots$
- Our prior: $\theta_i \sim N(0, \sigma^2)$, IID
- Thus: $-\log p(grammar) = c + (\theta_0^2 + \theta_1^2 + \theta_2^2 + \ldots)/\sigma^2$

- So good grammars have few large weights.
- Prior prefers one generalization to many exceptions.

Arc Probabilities: A Conditional Log-Linear Model

$S \rightarrow$ NP see **[Insert PP]** $S \rightarrow$ NP see PP

$$\frac{1}{Z'} \exp \quad \theta_3 \qquad +\theta_5 \quad +\theta_7$$

$S \rightarrow$ NP see NP **[Insert PP]** $S \rightarrow$ NP see NP PP

$$\frac{1}{Z} \exp \quad \theta_3 \qquad +\theta_6 \quad +\theta_7$$

To raise both rules' probs, cheaper to use θ_3 than both θ_5 & θ_6.
This generalizes – also raises other cases of PP-insertion!

Arc Probabilities: A Conditional Log-Linear Model

$S \rightarrow$ NP fund NP **[Insert PP]** $S \rightarrow$ NP fund NP PP

$$\frac{1}{Z''} \exp \quad \theta_3 \qquad +\theta_{82} +\theta_6 \quad +\theta_7$$

$S \rightarrow$ NP see NP **[Insert PP]** $S \rightarrow$ NP see NP PP

$$\frac{1}{Z} \exp \quad \theta_3 \qquad +\theta_{84} +\theta_6 \quad +\theta_7$$

To raise both probs, cheaper to use θ_3 than both θ_{82} & θ_{84}.
This generalizes – also raises other cases of PP-insertion!

Reparameterization

- Grammar is determined by $\theta_0, \theta_1, \theta_2, \ldots$
- A priori, the θ_i are normally distributed

- We've reparameterized!
- The parameters are feature weights θ_i, not rule probabilities
- Important tendencies captured in big weights
  - Similarly: Fourier transform – find the formants
  - Similarly: SVD – find the principal components
  - It's on this deep level that we want to compare events, impose priors, etc.
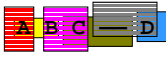

Other models of this string:
max-likelihood
n-gram
Collins arg/adj
hybrids

Simple Bigram Model (Eisner 1996)

- A parser assumes tree is probable if its component rules are:

- Try assuming rule is probable if its component bigrams are:

$p(A \mid \text{start}) \times p(B \mid A)$
$\times p(C \mid B) \times p(\text{——} \mid C)$
$\times p(D \mid \text{——}) \times p(\text{stop} \mid D)$

- Markov process, 1 symbol of memory; conditioned on L, w, side of ——
- One-count backoff to handle sparse data (Chen & Goodman 1996)

$p(L \rightarrow A\ B\ C\ \text{——}\ D \mid w) = p(L \mid w) \cdot p(A\ B\ C\ \text{——}\ D \mid L,w)$

Use "non-flat" frames?
Extra training info.
For test, sum over all bracketings.

Figure 8.7: A version of Fig. 8.3 if frame-internal brackets are retained at step 6 of data preparation (§8.3).

Perplexity: Predicting test frames

	basic	
	flat	non-flat[b]
Treebank	∞	∞
1-gram	1774.9	86435.1
2-gram	**135.3**	199.3
3-gram	136.5	177.4
Collins[c]	363.0	494.5
transformation	**108.6**	

20% further reduction

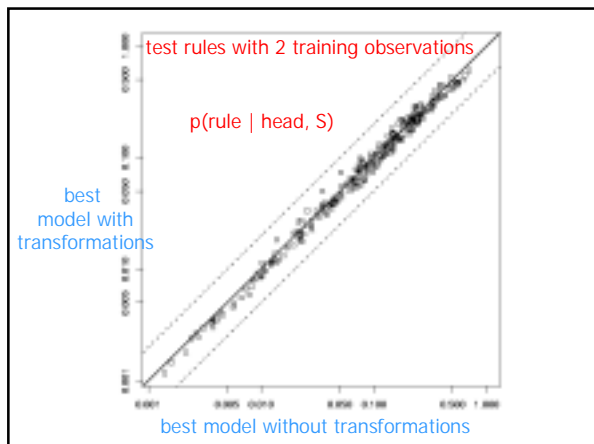Can get big perplexity reduction just by flattening.

from previous lit.

Perplexity: Predicting test frames

	basic		Treebank/Markov		
			Katz	one-count[a]	
	flat	non-flat[b]	flat	flat	non-flat
Treebank	∞	∞			
1-gram	1774.9	86435.1	340.9	160.0	193.2
2-gram	**135.3**	199.3	127.2	**116.2**	174.7
3-gram	136.5	177.4	132.7	123.5	174.8
Collins[c]	363.0	494.5	197.9		
transformation	**108.6**				
averaged[d]	**102.3**				

best model with transformations

best model without transformations

from previous lit

---

test rules with 0 training observations

p(rule | head, S)

best model with transformations

best model without transformations

---

test rules with 1 training observation

p(rule | head, S)

best model with transformations

best model without transformations

9

test rules with 2 training observations

p(rule | head, S)

best model with transformations

best model without transformations

Forced matching task

- Test model's ability to extrapolate novel frames for a word
- Randomly select **two** (word, frame) pairs from test data
  - ... ensuring that neither frame was ever seen in training
- Ask model to choose a matching:

| word 1 ——— frame A | word 1 ⤬ frame A |
| word 2 ——— frame B | word 2 ⤬ frame B |

  i.e., does frame A look more like word 1's known frames or word 2's?

- 20% fewer errors than bigram model

Graceful degradation

Twice as much data
But no transformations

Summary: Reparameterize PCFG in terms of deep transformation weights, to be learned under a simple prior.

- **Problem:** Too many rules!
  - Especially with lexicalization and flattening (which help).
  - So it's hard to estimate probabilities.

- **Solution:** Related rules tend to have related probs
  - *POSSIBLE* relationships are given a priori
  - *LEARN* which relationships are strong in <u>this</u> language
    (just like feature selection)

- Method has connections to:
  - Parameterized finite-state machines (Monday's talk)
  - Bayesian networks (inference, abduction, explaining away)
  - Linguistic theory (transformations, metarules, etc.)

FIN