



Volume Rendering

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Volume Rendering

Creating 2D images of volume data

**Voxels (volume elements) typically stored
in regular lattice**

Voxel lattice represents 3D scalar field

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Types of 3D Scalar Fields

X-ray absorption

Flow velocity (speed)

Temperature

Solidity (CSG, etc.)

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Generating 3D Scalar Fields

May be measured or simulated

Measured with CT scan or MRI

CFD simulation of flow and temperature

Sampling of CSG hierarchy

Conversion from B-Rep to Solid

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Field Reconstruction

Tri-linear interpolation

Quadratic or cubic splines

Convolution with filter kernel

- **Each voxel's contribution to a point, p , measured by value in kernel, which is centered at p**

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Mapping Values to Appearance

Often only a single value at each voxel

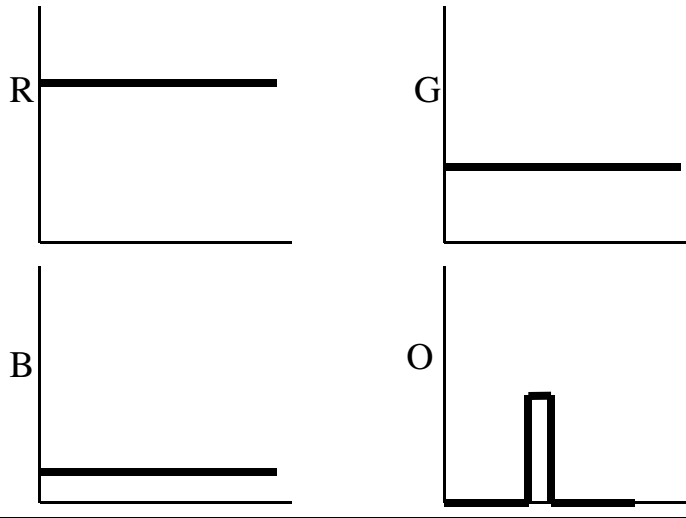
Want mapping to color and opacity

**May emphasize certain value ranges or give
all ranges equal emphasis in final image**

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



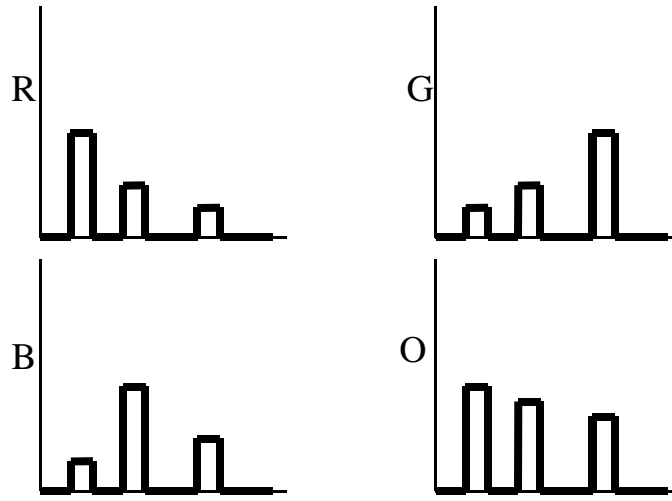
Emphasizing a Single Isosurface



Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



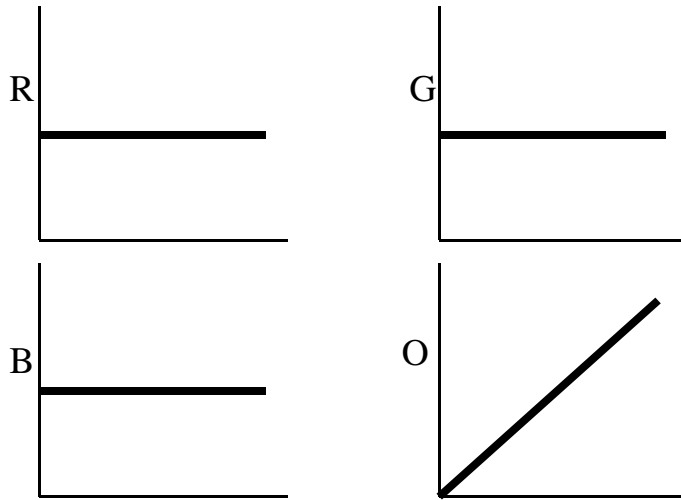
Emphasizing 3 Isosurfaces



Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Visualizing Values as Opacity



Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Methods of Rendering

Solid texturing

Isosurface extraction

Image-space accumulation (ray casting)

Object-space accumulation (splatting)

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Marching Cubes Algorithm

Performs isosurface extraction from voxel data

Creates a B-Rep, typically a set of triangles

B-Rep then rendering using standard rendering techniques

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Finding/Creating the Surface

Assume linear interpolation between data, stored at voxel corners

Mark corners as inside or outside surface

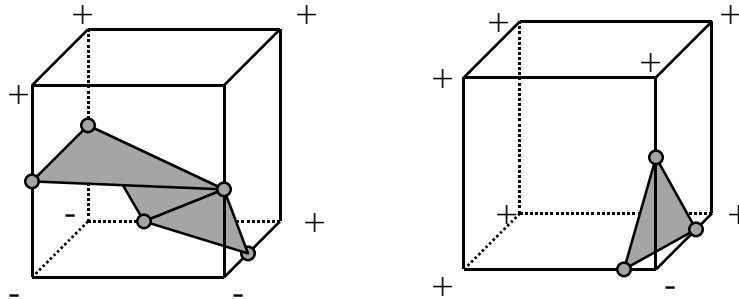
Find surface intersections along voxel edges

Construct triangles connecting intersections

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Marching Cubes Illustrations



- $2^8 = 256$ possible configurations (only 16 unique)
- Store all cases in table, including number and connectivity of triangles
- Must connect properly along voxel sides for continuity

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Rendering Isosurfaces

**One or more isosurfaces may be rendered
as totally opaque or partially transparent**

**Clipping planes may be used to illustrate
interior surfaces**

(see Figure 15 in Watt's *3D Computer Graphics*)

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Volume Ray Casting

Loop over pixels, generating rays

- at least one per pixel, typically

Trace each ray through the voxel grid

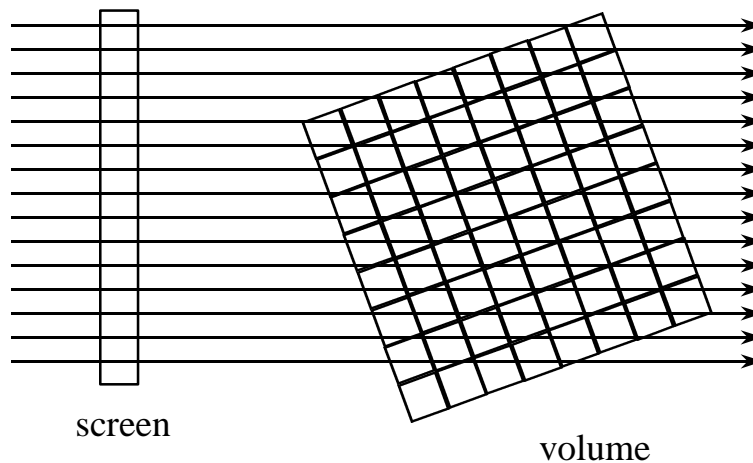
Accumulate color and opacity along ray

Stop when ray exits grid or reaches full opacity

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Ray Casting Illustration



Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Volume Splatting

Traverse voxels in front to back order

- traverse each voxel in plane, then move to next plane

For each voxel, accumulate color and opacity to each pixel it covers

- like throwing snowballs at the screen

Voxel projection covers hexagonal footprint

Smoother interpolation possible by applying kernel with fall-off away from sample point

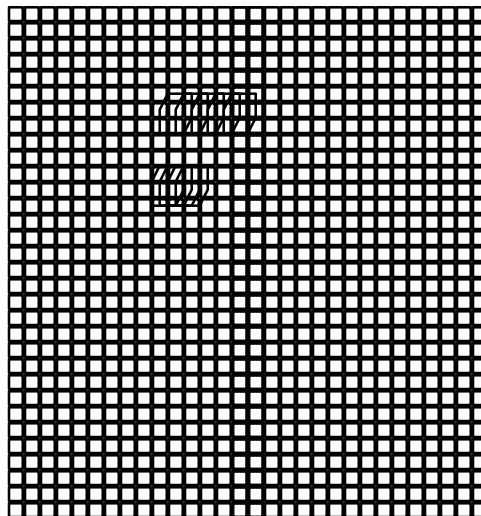
Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Volume Splatting Illustration



footprint



screen

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Ray Casting vs. Splatting

Ray Casting

- Point samples
- Random data access
- Easy for parallel or perspective projection

Splatting

- Area samples
- Ordered data access
- More difficult for perspective projection

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Color/Opacity Accumulation

Assume that each voxel emits a single color and filters colors by its opacity

$$C' = C * \alpha$$

$$C'_{out} = C'_{in} + C'_{voxel} * (1 - \alpha_{in})$$

$$\alpha_{out} = \alpha_{in} + \alpha_{voxel} * (1 - \alpha_{in})$$

$$C_{out} = C'_{out} / \alpha_{out}$$

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



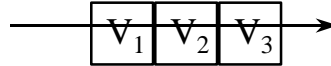
Accumulation Example

Suppose ray passes through 3 voxels (r,g,b,a):

$$V_1 = (.3, .1, .1, .2)$$

$$V_2 = (.1, .3, .1, .3)$$

$$V_3 = (.1, .3, .1, .3)$$



Premultiply colors by opacity:

$$V_1' = (.06, .02, .02, .2)$$

$$V_2' = (.03, .09, .03, .3)$$

$$V_3' = (.03, .09, .03, .3)$$

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Accumulation Example (cont.)

After passing through V_1 , we have

$$(0,0,0,0) + (.06,.02,.02,.2)*(1-0) = (.06,.06,.02,.2)$$

After passing through V_2 , we have

$$(.06,.02,.02,.2) + (.03,.09,.03,.3)*(1-.2) =$$
$$(.084,.092,.044,.44)$$

After passing through V_3 , we have

$$(.084,.092,.044,.44) + (.03,.09,.03,.3)*(1-.44) =$$
$$(.1008,.1424,.0608,.608)$$

Dividing by the final alpha, we get

$$(.17, .23, .1, 1)$$

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Volume Illumination

Several possible models

- identify surfaces within voxels
- allow not only voxel emission, but attenuation of incoming light and surface reflection
- model as particle clouds of various densities

Drebin et al. 98 models voxels as mixtures of materials

- all measurements continuous, not discrete
- measure surface “strength” based on differences in material densities
- measure surface normals as value gradients

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Parallel vs. Perspective Projection

Parallel

- Even sampling
- Regular access
- Simple footprints

Perspective

- Uneven sampling
- Irregular access
- Complex footprints

Johns Hopkins Department of Computer Science
Course 600.456: Rendering Techniques, Professor: Jonathan Cohen