



Volume Rendering

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Course 600.456: Rendering Techniques, Professor: Jonathan Cohen



Volume Rendering

Creating 2D images of volume data

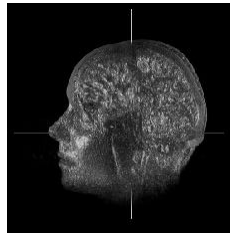
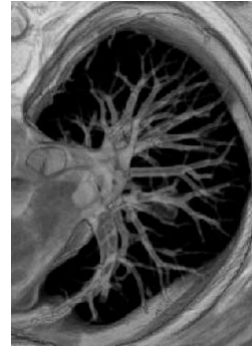
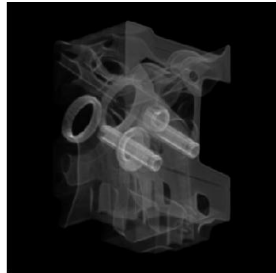
**Voxels (volume elements) typically stored
in regular lattice**

Voxel lattice represents 3D scalar field

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Examples



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Types of 3D Scalar Fields

X-ray absorption

Flow velocity (speed)

Temperature

Solidity (CSG, etc.)

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Generating 3D Scalar Fields

May be measured or simulated

Measured with CT scan or MRI

CFD simulation of flow and temperature

Sampling of CSG hierarchy

Conversion from B-Rep to Solid

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Field Reconstruction

Tri-linear interpolation

Quadratic or cubic splines

Convolution with filter kernel

- **Each voxel's contribution to a point, p , measured by value in kernel, which is centered at p**

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Mapping Values to Appearance

Often only a single value at each voxel

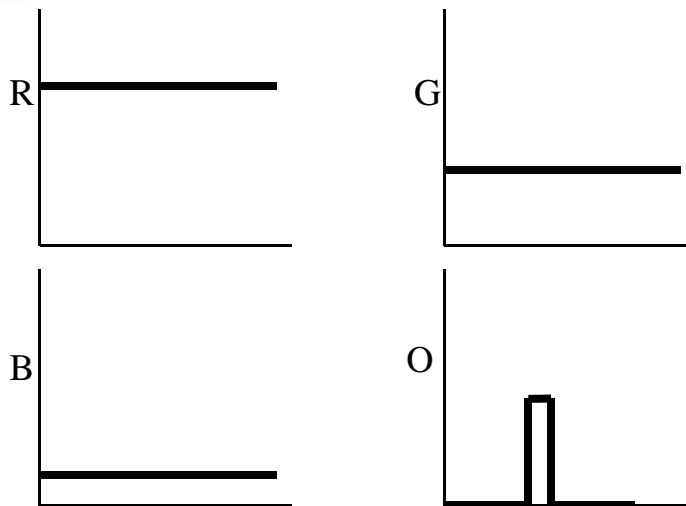
Want mapping to color and opacity

**May emphasize certain value ranges or give
all ranges equal emphasis in final image**

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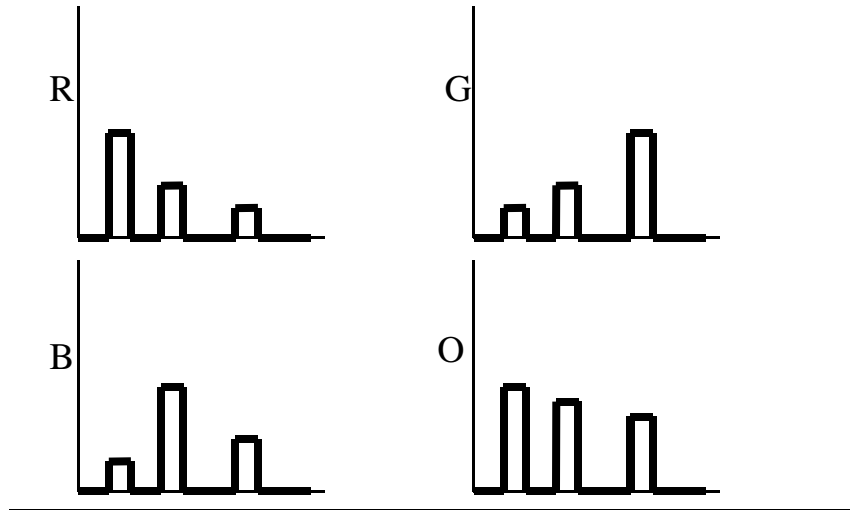
Emphasizing a Single Isosurface



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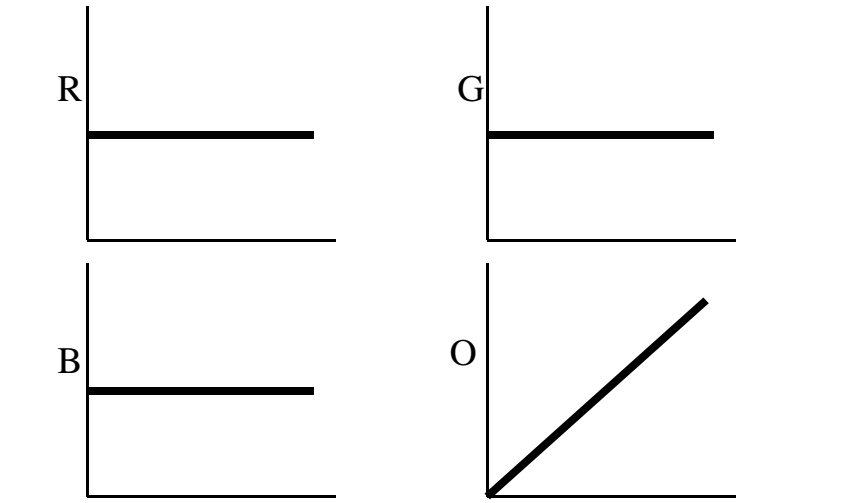
Emphasizing 3 Isosurfaces



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Visualizing Values as Opacity



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Methods of Rendering

Solid texturing

Isosurface extraction

Image-space accumulation (ray casting)

Object-space accumulation (splatting)

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Marching Cubes Algorithm

Performs isosurface extraction from voxel data

Creates a B-Rep, typically a set of triangles

B-Rep then rendering using standard rendering techniques

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Finding/Creating the Surface

**Assume linear interpolation between data,
stored at voxel corners**

Mark corners as inside or outside surface

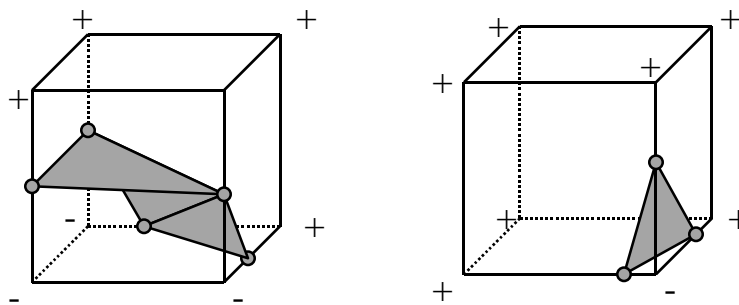
Find surface intersections along voxel edges

**Construct triangles connecting
intersections**

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Marching Cubes Illustrations



- $2^8 = 256$ possible configurations (only 16 unique)
- Store all cases in table, including number and connectivity of triangles
- Must connect properly along voxel sides for continuity

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Rendering Isosurfaces

**One or more isosurfaces may be rendered
as totally opaque or partially transparent**

**Clipping planes may be used to illustrate
interior surfaces**

(see Figure 15 in Watt's *3D Computer Graphics*)

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Volume Ray Casting

Loop over pixels, generating rays

- at least one per pixel, typically

Trace each ray through the voxel grid

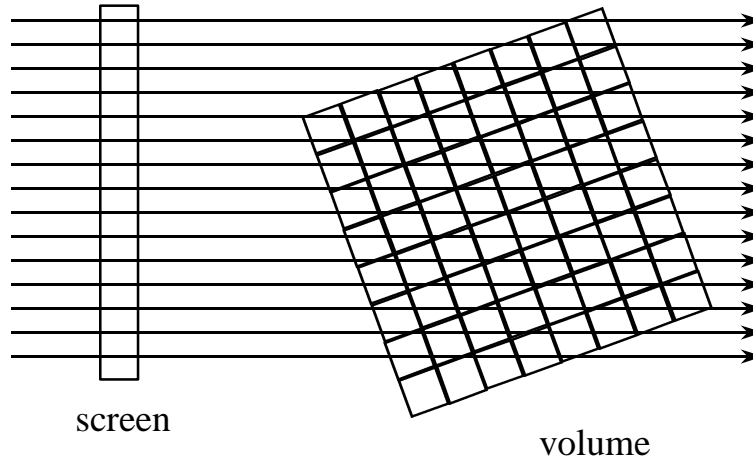
Accumulate color and opacity along ray

**Stop when ray exits grid or reaches full
opacity**

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Ray Casting Illustration



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Volume Splatting

Traverse voxels in front to back order

- traverse each voxel in plane, then move to next plane

For each voxel, accumulate color and opacity to each pixel it covers

- like throwing snowballs at the screen

Voxel projection covers hexagonal footprint

Smoother interpolation possible by applying kernel with fall-off away from sample point

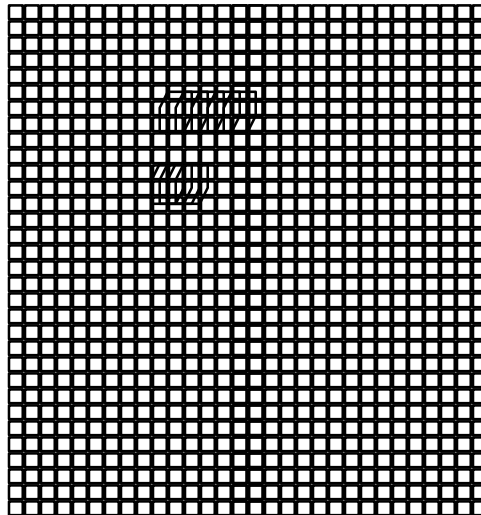
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Volume Splatting Illustration



footprint



screen

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Ray Casting vs. Splatting

Ray Casting

- **Point samples**
- **Random data access**
- **Easy for parallel or perspective projection**

Splatting

- **Area samples**
- **Ordered data access**
- **More difficult for perspective projection**

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Color/Opacity Accumulation

Assume that each voxel emits a single color and filters colors by its opacity

$$C' = C * \alpha$$

$$C'_{out} = C'_{in} + C'_{voxel} * (1 - \alpha_{in})$$

$$\alpha_{out} = \alpha_{in} + \alpha_{voxel} * (1 - \alpha_{in})$$

$$C_{out} = C'_{out} / \alpha_{out}$$

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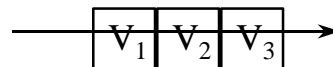
Accumulation Example

Suppose ray passes through 3 voxels (r,g,b,a):

$$V_1 = (.3, .1, .1, .2)$$

$$V_2 = (.1, .3, .1, .3)$$

$$V_3 = (.1, .3, .1, .3)$$



Premultiply colors by opacity:

$$V'_1 = (.06, .02, .02, .2)$$

$$V'_2 = (.03, .09, .03, .3)$$

$$V'_3 = (.03, .09, .03, .3)$$

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Accumulation Example (cont.)

After passing through V_1 , we have

$$(0,0,0,0) + (.06,.02,.02,.2)*(1-0) = (.06,.06,.02,.2)$$

After passing through V_2 , we have

$$(.06,.02,.02,.2) + (.03,.09,.03,.3)*(1-.2) =$$
$$(.084,.092,.044,.44)$$

After passing through V_3 , we have

$$(.084,.092,.044,.44) + (.03,.09,.03,.3)*(1-.44) =$$
$$(.1008,.1424,.0608,.608)$$

Dividing by the final alpha, we get

$$(.17, .23, .1, 1)$$

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Volume Illumination

Several possible models

- identify surfaces within voxels
- allow not only voxel emission, but attenuation of incoming light and surface reflection
- model as particle clouds of various densities

Drebin et al. 98 models voxels as mixtures of materials

- all measurements continuous, not discrete
- measure surface “strength” based on differences in material densities
- measure surface normals as value gradients

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Parallel vs. Perspective Projection

Parallel

- **Even sampling**
- **Regular access**
- **Simple footprints**

Perspective

- **Uneven sampling**
- **Irregular access**
- **Complex footprints**